| Name: | ID #: | Section $#$ : |
|-------|-------|---------------|
|       |       |               |

Q1) [2.5pts] Find  $\lim_{(x,y)\to(0,0)} \frac{xy\cos y}{3x^2+y^2}$ , if it exists, or show that the limit does not exist.

Solution:

**Q2**) [2.5pts] If 
$$w = \frac{x}{y+2z}$$
, find  $\frac{\partial^3 w}{\partial z \partial y \partial x}$  and  $\frac{\partial^3 w}{\partial x^2 \partial y}$   
Solution:

**Q3**) [2.5pts] Find an equation of the tangent plane to the surface  $z = y \ln x$  at the point (1, 4, 0).

## Solution:

**Q4**) [2.5pts] Let  $M = xe^{y-z^2}$ , x = 2uv, y = u - v, z = u + v. Find  $\frac{\partial M}{\partial u}$  and  $\frac{\partial M}{\partial v}$  when u = 3 and v = -1.

## Solution:

Name:

Quiz 4 - B

Q1) [3pts] Determine the set of point at which the function is continuous:

$$f(x,y) = \begin{cases} \frac{x^2y^3}{2x^2+y^2}, & (x,y) \neq (0,0) \\ 1, & (x,y) = (0,0) \end{cases}$$

Solution:

**Q2**) [2pts] Find all second partial derivatives of  $v = \frac{xy}{x-y}$ . Solution:

Q3) [3pts] Find linearization L(x, y) of  $f(x, y) = \sqrt{x + e^{4y}}$  at the point (3,0). Solution:

**Q3**) [2pts] If 
$$yz = \ln(x+z)$$
, find  $\frac{\partial z}{\partial x}$  and  $\frac{\partial z}{\partial y}$ .  
Solution: