## KFUPM Department of Mathematics and Statistics

MATH 302-4

Quiz 6, Term 101 Saturday January 1, 2011

**Exercise 1.** Let f(z) = u(x, y) + iv(x, y) be a complex function defined on  $\mathbb{C}$  and satisfying Cauchy Riemann Equations. Suppose that  $\operatorname{Re}(f(z)) = v(x, y) = 0$ , for all  $(x, y) \in \mathbb{R}^2$ . Show that there exists  $\alpha \in \mathbb{R}$  such that  $f(z) = \alpha$ , for each  $z \in \mathbb{C}$ .

**Exercise 2.** Let f(z) be the complex function defined by  $f(z) = e^{2x}(\cos(2y) + i\sin(2y))$ , for z = x + iy. Show that f satisfies Cauchy Riemann Equations and that f'(z) = f(z).