Name:

1) [3pts] Find the volume of the solid enclosed by the hyperboloid $-x^2 - y^2 + z^2 = 1$ and the plane z = 2.

Solution:

2) [4pts] Evaluate the integrals

(a)
$$\iint_{D} xy \ dA$$
, *D* is the disk with center the origin and radius 3

(b)
$$\int_0^{\sqrt{\pi}} \int_0^x \int_0^{xz} x^2 \sin y \, dy dz dx =$$

3) [3pts] Evaluate

$$\iiint_E \sqrt{x^2 + y^2} \, dV,$$

where E is the region that lies inside the cylinder $x^2 + y^2 = 16$ and between the planes z = -5 and z = 4.

Solution:

Name:

1) [4pts] Evaluate the integrals

(a)
$$\iint_{D} \sqrt{4 - x^2 - y^2} \, dA$$
, $R = \{(x, y) | x^2 + y^2 \le 4, x \ge 0\}$

(b)
$$\iiint_E yz \cos(x^5) \, dV, \quad E = \{(x, y, z) | \ 0 \le x \le 1, \ 0 \le y \le x, \ x \le z \le 2x\}$$

2) [3pts] Find the volume of the solid enclosed by the hyperboloid $-x^2 - y^2 + z^2 = 1$ and the plane z = 2.

Solution:

3) [3pts] Evaluate the integral by changing to cylindrical coordinates

$$\int_{-3}^{3} \int_{0}^{\sqrt{9-x^2}} \int_{0}^{9-x^2-y^2} \sqrt{x^2+y^2} \, dz \, dy \, dx$$

Solution: