

Name: _____

ID #: _____

Section #: _____

- 1) [3pts] Use Lagrange multiplier to find the absolute maximum and minimum values of $f(x, y) = 4x + 6y$ on the circle $x^2 + y^2 = 13$.

Solution:

- 2) [4pts] Calculate the iterated integrals

(a)
$$\int_0^1 \int_1^2 \frac{xe^x}{y} dy dx =$$

(b)
$$\int_0^1 \int_{x^2}^x (1 + 2y) dy dx =$$

- 3) [3pts] Solve *one* of the following questions

- (a) Find the average value of $f(x, y) = x \sin y$ on the region D enclosed by the curve $y = x^2$ and the lines $y = 0$, $x = 1$.
- (b) Evaluate (change the order of the integration)

$$\int_0^1 \int_{3y}^3 e^{x^2} dx dy$$

Solution:

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1) [4pts] Calculate the following integrals

(a) $\int_0^1 \int_0^1 (u - v)^5 du dv =$

(b) $\iint_D x^3 dA, D = \{(x, y) | 1 \leq x \leq e, 0 \leq y \leq \ln x\}$

2) [3pts] Solve *one* of the following questions

- (a) Find the average value of $f(x, y) = e^y \sqrt{x + e^y}$ over $R = [0, 4] \times [0, 1]$.
(b) Evaluate (change the order of the integration)

$$\int_0^8 \int_{\sqrt[3]{y}}^2 e^{x^4} dx dy$$

Solution:

3) [3pts] Use Lagrange multiplier to find the absolute maximum and minimum values of $f(x, y) = 4x + 6y$ on the circle $x^2 + y^2 = 13$.

Solution: