

Problem 1: Determine whether the sequence is convergent or divergent. If it converges, find its limit.

(a) $\left\{ \frac{2n}{n+1} \tan^{-1} n \right\}_{n=1}^{\infty}$

(b) $a_n = (-1)^n (\sqrt{n+2} - \sqrt{n}), \quad n = 1, 2, 3, \dots$

(c) $a_n = \frac{\sin n}{n^2 + 1}, \quad n = 1, 2, 3, \dots$

Problem 2: Determine whether the series is convergent or divergent. If it converges, find its sum.

(a)
$$\sum_{n=1}^{\infty} \frac{3^n + 2^{2n}}{4^n}$$

(b)
$$\sum_{n=1}^{\infty} \frac{1}{4n^2 + 4n}$$

(c)
$$\sum_{n=1}^{\infty} \left(1 + \frac{1}{n}\right)^n$$