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1 Find $\lim_{x \rightarrow -3^+} \frac{1}{|3+x|}$

when $x \rightarrow -3^+$

$$x = -3 + \delta$$

where δ is a small number

$$\Rightarrow \frac{1}{|3 - 3 + \delta|} = \frac{1}{|\delta|} = \frac{1}{\delta}$$

1 over small is large

$$\Rightarrow \lim_{x \rightarrow -3^+} \frac{1}{|3+x|} = \infty$$

and $\lim_{x \rightarrow 2^+} [[2x - 1]]$

$$x \rightarrow 2^+$$

$$x = 2 + \delta$$

$$\Rightarrow [[2(2 + \delta) - 1]]$$

$$= [[4 + 2\delta - 1]]$$

$$= [[3 + 2\delta]] = 3$$

$$\lim_{x \rightarrow 2^+} [[2x - 1]] = 3$$

2 Find $\lim_{x \rightarrow 1^-} \frac{|x^2 - 3x + 2|}{x^2 - 1}$

$$\lim_{x \rightarrow 1^-} \frac{|(x-1)(x-2)|}{(x-1)(x+1)}$$

Since $x \rightarrow 1^-$ ($x = 1 - \delta$) $\Rightarrow (x-1) < 0$

also $(x-2) < 0$

hence $(x-1)(x-2) > 0$

$$\Rightarrow \lim_{x \rightarrow 1^-} \frac{|(x-1)(x-2)|}{(x-1)(x+1)} = \lim_{x \rightarrow 1^-} \frac{(x-1)(x-2)}{(x-1)(x+1)}$$

$$= \lim_{x \rightarrow 1^-} \frac{(x-2)}{x+1} = \frac{-1}{2}$$