

Steps to reduce a matrix to Row Echelon Form:

1. Find if there is any element = 1 in the first column; if it occurs in row i then $R_i \leftrightarrow R_1$. If not, look at any non-zero element in the first column and if it is in row i then $R_i \leftrightarrow R_1$.
2. If all elements in the first column are zeros, move to the second column and apply step 1 as above.
3. If a_{11} now is 1, go to the next step. If $a_{11} \neq 1$ then divide R_1 by a_{11} .
4. Try to make all entries under $1 = a_{11}$ to be zeros.
5. Ignore R_1 and repeat the same steps for the matrix obtained by deleting R_1 till you have some thing like:

$$\begin{bmatrix} 1 & * & * & * & * & * \\ 0 & 1 & * & * & * & * \\ 0 & 0 & 0 & 1 & * & * \\ 0 & 0 & 0 & 0 & 1 & * \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

Now the matrix is in **Row Echelon Form**.

If the matrix to be reduced to **Reduced Row Echelon Form** then

6. In each column containing a leading entry 1, all the other entries must be zeros.

Example:

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 3 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

RREF