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Chahrazade BAKKARI

CONTENUS, POLYNÔMES GAUSSIENS ET PROPRIÉTÉS DE PRÜFER

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Prof. S. Bazzoni	Univ. di Padova	Italy	Membre
Prof. A. Bouvier	Haut Conseil de l'Educ.	France	Président
Prof. M. Fontana	Univ. di Roma III	Italy	Membre
Prof. S. Glaz	Univ. of Connecticut	USA	Membre Rapporteur
Prof. S. Kabbaj	KFUPM	KSA	Membre
Prof. T. Lucas	Univ. of North Carolina	USA	Membre Rapporteur
Prof. N. Mahdou	FST Univ. Fez	Morocco	Directeur de Thèse
Prof. A. Mimouni	KFUPM & Univ. Fez	KSA & Morocco	Membre Rapporteur
Prof. M. Sobrani	FST Univ. Fez	Morocco	Membre Rapporteur

CONTENT, GAUSSIAN POLYNOMIAL
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Author's papers involved in this thesis:

1. C. Bakkari and N. Mahdou, *Gaussian polynomials and content ideal in pullbacks*, Comm. Algebra, **vol. 34**, No. 8, pp. 2727- 2732, (2006).
2. C. Bakkari, N. Mahdou, and H. Mouanis, *Prüfer-like conditions in subrings retract and applications*, accepted for publication in Comm. Algebra.
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5. C. Bakkari and N. Mahdou, *Prüfer-like conditions in pullbacks*, in preparation.

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2. C. Bakkari and N. Mahdou, *On Armendariz rings*, submitted for publication.
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