

Name:-

ID:-

Q1. Find the limit if exist $\lim_{x \rightarrow 0} \cos\left(\frac{\pi x}{\sin x}\right)$.

$$\cos \lim_{x \rightarrow 0} \frac{\pi x}{\sin x} = \cos \lim_{x \rightarrow 0} \pi \left(\frac{x}{\sin x} \right) = \cos \lim_{x \rightarrow 0} \pi = \cos \pi = -1$$

l. Hospital

Also

$$\cos \lim_{x \rightarrow 0} \frac{\pi}{-\cos x} = \cos \frac{\pi}{1} = -1$$

Q2. Find the limit if exist $\lim_{x \rightarrow 1} \left(\frac{x}{\ln x} - \frac{1}{x \ln x} \right)$.

$$\lim_{x \rightarrow 1} \frac{x^2 - 1}{x \ln x} \left(\frac{0}{0} \right) \text{ l. Hospital}$$

$$= \lim_{x \rightarrow 1} \frac{2x}{\ln x + 1} \left(\frac{0}{0} \right) = \lim_{x \rightarrow 1} \frac{2}{\frac{1}{x}} = 2$$