

Consider the function  $y = f(x) = \frac{x-1}{x^2}$  with  $f'(x) = \frac{2-x}{x^3}$  and  $f''(x) = \frac{2(x-3)}{x^4}$

a. Find the domain  $\mathbb{R} - \{0\}$

b. Find the asymptotes if any exist.

Horizontal:  ~~$x \rightarrow \pm\infty$~~   $\rightarrow \lim_{x \rightarrow \pm\infty} f(x) = 0 = \lim_{x \rightarrow \pm\infty} \frac{x-1}{x^2}$   $y = 0$

Vertical:  $x = 0$   $\lim_{x \rightarrow 0^-} f(x) = -\infty$ ,  $\lim_{x \rightarrow 0^+} f(x) = +\infty$

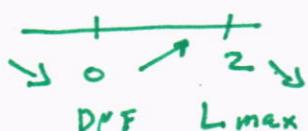
Slant: None

c. Find the critical numbers.  $x = 0, 2$

0  $f'$  DNE

2  $f' = 0$

d. Find intervals where the function is increasing and those where it is decreasing.



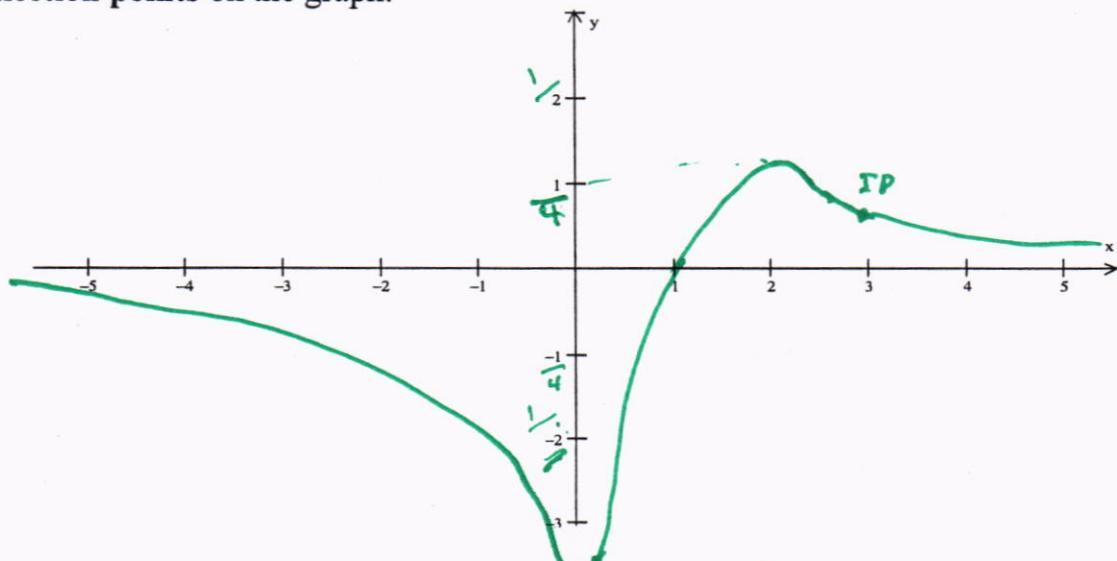
e. Find the local maximum and minimum of the function.

(2,  $\frac{1}{4}$ ) L max

f. Discuss the concavity of the function and find the inflection points.



g. Sketch the graph of the function. Clearly indicate the **critical numbers**, **extrema** and **inflection points** on the graph.



h. Find the absolute extrema of the function if exist.

Abs Max  $(2, \frac{1}{4})$  value  
point