Assignment \#4 (solve in the space provided) - Submission Deadline: Wed. May 6, 2015

1. [2 pts.] At KFUPM, $5 \%$ of all students play football and basketball, $32 \%$ of all students play football. What is the probability that a student plays basketball given that he plays football?
2. [ 3 pts.] Compute the probability that the number 3 appears 5 times when a fair die is rolled 7 times.
3. Let $E$ be the event "exactly 2 heads appear when a fair coin is flipped four times" and $F$ be the event "the first flip from the four flips is a head".
(a) [3 pts.] Compute the conditional probability $P(E \mid F)$. In your solution, show the sample space for the events $E, F$ and $E \cap F$.
(b) [2 pts.] Are the events $E$ and $F$ independent? Justify your answer.
4. Consider a die in which the outcome 1 is twice as likely to occur as any other outcome. Let $X$ be the random variable that is the outcome of rolling this die.
(a) [3 pts.] Compute the expected value of $X$ and variance of $X$.
(b) [2 pts.] Let $Z$ be the random variable that is the sum of the outcomes when the die is rolled 10 times. Use Linearity of Expectation to compute the expected value of $Z$.
