

Name: KEY

1) Choose the correct answer:

The modulating frequency in frequency modulation is increased from 10 kHz to 20 kHz. The bandwidth is :

- a) doubled    b) halved    (c) increased by 20 kHz    d) increased tremendously    e) not affected

2) What is the main disadvantage with direct method of frequency modulation?

Frequency instability.

3) What are the main two blocks in a band-pass limiter?

hard limiter + Bandpass filter

4) A single-tone FM signal is given by  $\phi_{FM}(t) = 10 \cos(16\pi \times 10^6 t + 20 \sin(2\pi \times 10^3 t))$

a) Find the modulation index and estimate the bandwidth of the signal.

B = 1 kHz  
 f

$$\omega_c = 16\pi \times 10^6 + 4\pi \times 10^4 \cos(2\pi \times 10^3 t)$$

$$f_c = 8 \times 10^6 + 2 \times 10^4 \cos(2\pi \times 10^3 t)$$

Bandwidth =

$$\Delta f_{max} = 20 \text{ kHz}$$

$$2(\Delta f + B) = \boxed{42 \text{ kHz}}$$

$$\beta = \frac{\Delta f}{B} = \frac{20 \text{ k}}{1 \text{ k}} = \boxed{20}$$

3 b) if  $k_f = 10/\pi$  kHz/V, what is the message  $m(t)$ . Hint: check the units for  $k_f$

$$\frac{10 \text{ k}}{\pi} \times 2\pi \equiv k_f = 20 \text{ km/s/V}$$

$$\phi_{FM}(t) = 10 \cos(16\pi \times 10^6 t + 20 \sin(2\pi \times 10^3 t))$$

$$\phi(t) = A \cos(\omega_c t + k_f a(t))$$

$$20 \sin(2\pi \times 10^3 t) = 20 k a(t)$$

differentiate both sides

$$m(t) = \frac{2\pi \times 10^3}{10} \cos(2\pi \times 10^3 t) = \boxed{2\pi \cos(2\pi \times 10^3 t)} \text{ V}$$