

EE200 DIGITAL LOGIC CIRCUIT DESIGN

The material covered in this class will be as follows:

- ⇒ Boolean functions
- ⇒ Algebraic manipulation
- ⇒ Complement of a function
- ⇒ Canonical and standard forms

Boolean Functions

The following Boolean functions are represented in the truth table.

$$F_1 = xyz'$$

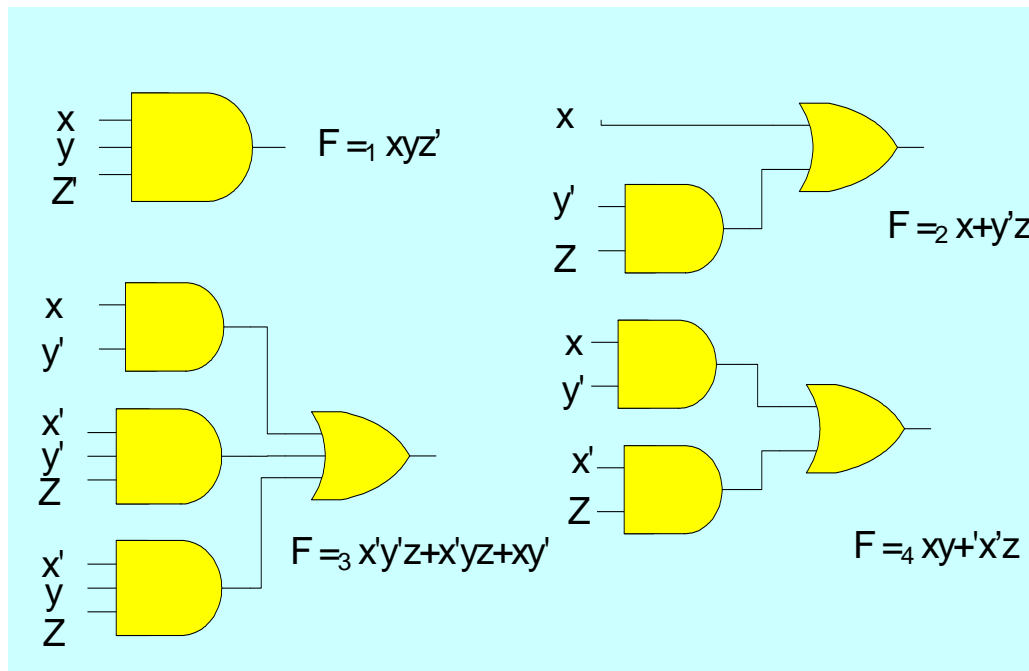
$$F_2 = x + y'z$$

$$F_3 = x'y'z + x'yz + xy'$$

$$F_4 = xy' + x'z$$

x	y	z	F_1	F_2	F_3	F_4
0	0	0	0	0	0	0
0	0	1	0	1	1	1
0	1	0	0	0	0	0
0	1	1	0	0	1	1
1	0	0	0	1	1	1
1	0	1	0	1	1	1
1	1	0	1	1	0	0
1	1	1	0	1	0	0

The functions can be implemented, using the basic logic gates, as shown in the following logic diagrams.



Algebraic Manipulation

Boolean functions are made up of terms. Each term consists of a number of literals. A **literal** is a variable or the complement of a variable. Each term is represented by a logic gate and each literal represents an input to a logic gate. By reducing the number of terms, the number of literals, or both, a simpler logic circuit can be used to implement the Boolean function.

Reduction of the number of terms and/or number of literals is done by algebraic manipulation.

Examples

1. $x(x' + y) = xx' + xy = 0 + xy = xy$
2. The dual of (1) is \rightarrow
 $x + x'y = (x + x')(x + y) = 1.(x + y) = x + y$

3. $(x + y)(x + y') = x + yy' = x + 0 = x$
 $xy + x'z + yz = xy + x'z + (x + x')yz$
 $= xy + xyz + x'z + x'yz$
4. $= xy(1 + z) + x'z(1 + y)$
 $= xy.1 + x'z.1 = xy + x'z$
5. $(x + y)(x' + z)(y + z) = (x + y)(x' + z) \rightarrow$ by duality.

Complement of a Function

The complement of a Boolean function may be obtained by either one of two methods:

1. Repetitive application of DeMorgan's theorem.
2. Taking the dual of the function and complementing each literal.

Example:

Find the complement of $F = x'yz' + x'y'z$

First method
$$F' = (x'yz' + x'y'z)' = (x'yz')' \cdot (x'y'z)'$$

$$= (x + y' + z)(x + y + z')$$

Second method

dual of F $\rightarrow F^{dual} = (x' + y + z')(x' + y' + z)$

then complement each literal

$$F' = (x + y' + z)(x + y + z')$$

Canonical and Standard Forms

Minterms and Maxterms

			Minterms		Maxterms	
x	y	z	Term	Designation	Term	Designation
0	0	0	$x'y'z'$	m_0	$x + y + z$	M_0
0	0	1	$x'y'z$	m_1	$x + y + z'$	M_1
0	1	0	$x'yz'$	m_2	$x + y' + z$	M_2
0	1	1	$x'yz$	m_3	$x + y' + z'$	M_3
1	0	0	$xy'z'$	m_4	$x' + y + z$	M_4
1	0	1	$xy'z$	m_5	$x' + y + z'$	M_5
1	1	0	xyz'	m_6	$x' + y' + z$	M_6
1	1	1	xyz	m_7	$x' + y' + z'$	M_7