# King Fahd University of Petroleum and Minerals <br> College of Computer Science and Engineering Computer Engineering Department 

COE 202: Digital Logic Design (3-0-3)
Term 132 (Spring 2013-2014)
Major Exam 1
Saturday March 1, 2014

## Time: 90 minutes, Total Pages: 11

Name: $\qquad$ ID: $\qquad$ Section: $\qquad$

## Notes:

- Do not open the exam book until instructed
- No Calculators are allowed (basic, advanced, cell phones, etc.)
- Answer all questions
- All steps must be shown
- Any assumptions made must be clearly stated

| Question | Maximum Points | Your Points |
| :---: | :---: | :---: |
| 1 | 13 |  |
| 2 | 12 |  |
| 3 | 15 |  |
| 4 | 15 |  |
| 5 | 10 |  |
| Total | 65 |  |

## Question 1.

Perform the following number base conversion with fraction precision of 3-digit where needed. Show your work in the "Work/ Scratch Area"

| Required Conversion | Work / Scratch Area |  |
| :--- | :--- | :--- |
| a. (i) $(0.339)_{10}=(\quad)_{2}$. |  |  |
| (ii) Convert the above obtained binary result |  |  |
| back to decimal. $=($ | $)_{10}$ |  |
| (iii) What is the conversion loss in accuracy? |  |  |



## Question 2.

I. Compute the following arithmetic operations in the indicated bases

| a. $(\mathrm{A} 69 \mathrm{C}-3 \mathrm{~F})_{16}$ | b. $(255+127)_{8}$ |
| :--- | :--- |
|  |  |

II. What is the radix $r$ of the number system for which $(24+17=40)_{r}$.

## Question 3.

Use Boolean algebra to solve the following questions. Show clearly all your steps.
a. Give the simplest form of $\mathrm{F}=\mathrm{Y}(\mathrm{X}+\mathrm{Y})+\overline{(\mathrm{X}+\mathrm{Y})} \mathrm{Z}+\mathrm{YZ}$
b. Given that $\mathrm{C}=A \bar{B}+\bar{A} B$ show that $A \bar{C}+\bar{A} C=B$
c. Find the values of the 4 Boolean variables $A, B, C$, and $D$ by solving the following set of simultaneous Boolean equations:
i. $\bar{A}+B=0$
ii. $A B=A C$
iii. $A B+A \bar{C}+C D=\bar{C} D$
d. Without simplification, write out the complement and dual forms of the following expression:
$(x+\bar{y} \bar{z})(w \bar{x} z+\bar{w} y \bar{z}):$
(3 Points)

## Question 4.

I. The truth table of a digital circuit which has two inputs (A, B) and two outputs $(\mathrm{Y}, \mathrm{Z})$ is shown: (4 points)
a. Write the Boolean expressions of the circuit outputs (Y, Z).

| A | B | Y | Z |
| :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 0 |

b. Draw the logic diagram of this circuit (i.e., its gate-level implementation).
II. Given the Boolean function $F(X, Y, Z)=(X+Y)(X+Z)(\bar{X}+\bar{Z})$ :
a. Express F as a sum-of-minterms, $F=\sum m$.
b. Find the algebraic product-of-Maxterms expression for $F$.
III. Given $F(A, B, C)=\sum m(0,3,5,7)$ and $G(A, B, C)=\Pi M(1,2,4,7)$, express the function $F+\bar{G}$ as a sum-of-minterms.
IV. Given the following two circuits representing the functions F and G. Determine whether the two functions F and G are equivalent or not. Justify your answer.
(4 points)


## Question 5.

I. Assume that the propagation delay of a gate depends only on its number of inputs. Thus, the propagation delay of an Inverter is 1 ns , of a 2-input gate (AND or OR) is 2 ns , and of a 3 -input gate is 3 ns. For the circuit shown below;
a. What is the longest propagation delay from an input to the output?
b. If $\mathbf{A}=\mathbf{0}, \mathbf{B}=\mathbf{1}, \mathbf{C}=\mathbf{1}, \mathbf{D}=\mathbf{1}$, and $\mathbf{F}=\mathbf{0}$, draw the signal waveforms at points $\mathbf{G}, \mathbf{H}$, and $\mathbf{Y}$ due to the shown applied signal at $\mathbf{E}$ by completing the timing diagram given below. ( $\mathbf{3}$ points)


II. Given an inverter with the following parameters $\mathrm{V}_{\mathrm{OH}}=5 \mathrm{v} \mathrm{V}_{\mathrm{OL}}=0 \mathrm{v}, \mathrm{V}_{\mathrm{IH}}=2.8 \mathrm{v}, \mathrm{V}_{\mathrm{IL}}=1.6$, the noise margins $\mathrm{NM}_{\mathrm{H}}=$ $\qquad$ and $\mathrm{NM}_{\mathrm{L}}=$ $\qquad$ .
(2 points)
III. The Boolean function implemented by the circuit given below expressed as a sum-of-products is

$$
\mathrm{F}=
$$

$\qquad$ .


