## COE 200, Term 042

## Fundamentals of Computer Engineering

HW\# 5
Q.1. For each of the following simplified expressions; determine the number of Essential Prime Implicants (EPIs) and the number of minterms in each EPI:
(i) $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z})=\mathrm{XY}+\mathrm{Z}$
(ii) $\mathrm{F}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D})=\mathrm{D}\left(\mathrm{A}^{\wedge}+\mathrm{B}\right)$
(iii) $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z})=\mathrm{X}^{\prime}\left(\mathrm{Y}^{`}+\mathrm{Z}^{`}\right)+\mathrm{YZ}$
(iv) $F(X, Y, Z)=X^{\prime}\left(Y^{`}+Z^{\prime}\right)+X Z$
(v) $\mathrm{F}(\mathrm{A}, \mathrm{B}, \mathrm{C})=\mathrm{A}^{\prime}$
(vi) $\mathrm{F}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E})=1$
(vii) $\mathrm{F}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}, \mathrm{G}, \mathrm{H})=0$
Q.2. Using K-maps, simplify the following expressions for both; POS and SOP formats:
(i) $\quad \mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z})=\sum(0,2,4)$
(ii) $\mathrm{F}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D})=\Pi(1,7,9,13,15)$
(iii) $\mathrm{F}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D})=\sum(0,1,2,3,4,8,10)$
(iv) $\mathrm{F}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E})==\mathrm{D}\left(\mathrm{A}^{\prime}+\mathrm{B}\right)+\mathrm{EA}+\mathrm{D}^{`} \mathrm{E}^{`} \mathrm{CB}+\mathrm{A}^{`} \mathrm{C}^{\prime} \mathrm{B}+\mathrm{B}^{`}$
Q.3. The following Boolean expression: $\mathrm{BE}+\mathrm{B}^{`} \mathrm{DE}^{\prime}$ is a simplified version of the expression: $\mathrm{A}^{`} \mathrm{BE}+\mathrm{BCDE}+\mathrm{BC}^{`} \mathrm{D}^{`} \mathrm{E}+\mathrm{A}^{`} \mathrm{~B}^{`} \mathrm{DE}+\mathrm{B}^{`} \mathrm{C}^{\prime} \mathrm{DE}^{`}$. Are there any don$t$ care conditions? If so, what are they?
Q.4. Using K-maps, simplify the following expressions using the specified don't care conditions for both; POS and SOP formats:
(i) $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z}, \mathrm{W})=\sum(0,1,2,3,4,8,10) \quad, \quad \mathrm{d}(\mathrm{X}, \mathrm{Y}, \mathrm{Z}, \mathrm{W})=\sum(7,11,15)$
(ii) $\mathrm{F}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D})=\sum(1,7,9,13,15) \quad, \quad \mathrm{d}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D})=\sum(2,3,5,6)$
(iii) $F(X, Y, Z)=\sum(0,3,5,6) \quad, \quad d(X, Y, Z)=\sum(1,2,4,7)$
(iv) $\mathrm{F}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D})=\sum(0,1,4,8,12) \quad, \quad \mathrm{d}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D})=\sum(3,6,7)$

