## **COE 405, Term 041**

## **COE 561 Digital System Design and Synthesis**

## HW# 3

## Due date: Tuesday, Nov. 23

**Q.1.** Consider the logic network defined by the following expressions:

$$x = a d' + a' b' + a' d' + b c + b d' + a c$$
  

$$y = a + b$$
  

$$z = a' c' + a' d' + b' c' + b' d' + e$$
  

$$u = a' c + a' d + b' d + e'$$

- (i) Substitute y into  $f_x$  by performing the algebraic division  $f_x/f_y$ . Show all steps. Determine the number of literals saved. Compare your solution with the result obtained by running the sis command *resub* –*d* (resubstitute without complement).
- (ii) Compute all kernels and co-kernels of z and u. Extract a multiple-cube subexpression common to  $f_z$  and  $f_u$ . Show all the steps. Determine the number of literals saved. Compare your solution with the result obtained by running the sis command *gkx*.
- **Q.2.** Consider the logic network defined by the following expressions:

x = a b c f + e f c + d ey = a c d e f + b d e fz = b c d + a c f

- (i) Determine the cube-variable matrix and all prime rectangles.
- (ii) Determine the minimum-literal network that can be derived by cube extraction. Determine the number of literals saved. Compare your solution with the result obtained by running the sis command *gcx*.
- **Q.3.** Consider the following function:

$$x = b d + c d + b e + c e + a f d + a f e + a b g + a c g + a f g$$

- (i) Find a quick factor of x by using the first level-0 kernel found. Assume that input variables are sorted in lexicographic order. Determine the number of literals obtained. Compare your solution with the result obtained by running the sis commands *factor* qx; *print\_factor*; *print\_stats f*.
- (ii) Find a good factor of x based on using the best kernel. Determine the number of literals obtained. Compare your solution with the result obtained by running the sis commands *factor –g x*; *print\_factor; print\_stats –f*.

- (iii) Decompose x using quick decomposition based on using the first level-0 kernel found. Determine the number of literals obtained. Compare your solution with the result obtained by running the sis commands *decomp* -q. Compare your solution to the factored solution obtained in (i).
- (iv) Decompose *x* using good decomposition based on using based on using the best kernel. Determine the number of literals obtained. Compare your solution with the result obtained by running the sis commands *decomp* −*g*. Compare your solution to the factored solution obtained in (ii).
- (v) Run the sis command fx and compare the solution obtained to that obtained in (iii) and (iv).
- Q.4. Consider the logic network defined by the following expressions::

$$x = a'b'c d + a'b'c'd' + acd' + ac'd + bcd' + bc'd$$
$$y = a'b'c + a'b'd + ac'd' + bc'd'$$

- (i) Compute all double-cube divisors of x and y along with their bases.
- (ii) Apply the fast extraction algorithm based on extracting double-cube divisors along with complements or single-cube divisors with two-literals. Show all steps of the algorithm. Determine the number of literals saved. Compare your solution with the result obtained by running the sis commands fx.
- (iii) Run the sis commands gkx followed by gcx and compare the solution obtained to that obtained in (ii).
- **Q.5.** Consider the logic network defined by the following expressions:

$$d = b'$$
  

$$f = (a+d)'$$
  

$$e = (c a)'$$
  

$$x = f e$$
  

$$y = d \oplus e$$

Inputs are  $\{a, b, c\}$  and output are  $\{x, y\}$ .

- (i) Assume  $CDC_{in} = abc'$ . Compute  $CDC_{out}$ .
- (ii) Compute the ODC sets for all internal and input vertices, assuming that the outputs are fully observable.
- **Q.6.** Consider the logic network defined by the following expressions:

$$u = a b' + b c$$
$$x = a u + b$$
$$y = a'u' + c'$$

Inputs are  $\{a, b, c\}$  and outputs are  $\{x, y\}$ .

- (i) Compute the SDC set and ODC set for node *u*.
- (ii) Simplify *u* using its ODC set.

- (iii) Simplify *x* and *y* using the SDC set.
- (iv) Apply the sis command *full\_simplify* and compare the solution obtained to what you obtained as a result of applying steps (ii) and (iii).
- **Q.7.** Consider the logic network defined by the following expressions:

$$o = e g$$
$$e = (a + b)'$$
$$g = d + c$$
$$d = a b$$

Inputs are  $\{a, b, c\}$  and output is  $\{o\}$ .

- (i) Consider the network perturbation replacing d by 0, i.e.  $\delta = a \ b \oplus 0 = a \ b$ . Determine if this perturbation is feasible or not.
- (ii) Is the fault *d* stuck-at-0 testable. If it is testable find all tests detecting the fault. If the fault is untestable optimize the network by eliminating redundancy.
- (iii) Is the fault *e stuck-at-1* testable. If it is testable find all tests detecting the fault. If the fault is untestable optimize the network by eliminating redundancy.