

COE 405, Term 181

Design & Modeling of Digital Systems

Assignment# 2

Due date: Saturday, Oct. 13

- Q.1.** Consider the given FSM that has 7 states, one input (X) and one output (Z), represented by the following state table:

Present State	Next State		Output (Z)	
	X=0	X=1	X=0	X=1
S0	S3	S1	0	1
S1	S3	S2	1	0
S2	S6	S5	0	1
S3	S0	S4	0	1
S4	S0	S5	1	0
S5	S1	S2	0	1
S6	S0	S2	1	0

- (i) Determine the equivalent states.
- (ii) Reduce the state table into minimum number of states and show the reduced state table.
- Q.2.** Consider the given FSM that has 5 states, one input (X) and one output (Z), represented by the following state table:

Present State	Next State, Z	
	X=0	X=1
S0	S1, 1	S2, 1
S1	S2, 0	S3, 0
S2	S2, 1	S3, 1
S3	S3, 0	S4, 0
S4	S3, 1	S4, 1

- (i) Implement the FSM using the following state assignment: S0=000, S1=001, S2=100, S3=010 and S4=101.
- (ii) Implement the FSM using the following state assignment: S0=010, S1=101, S2=111, S3=001 and S4=011.
- (iii) Compare the area of the two resulting circuits.

Q.3. It is required to design a sequential circuit using Mealy model that computes the equation $Z=3*X-4$, where X is an unsigned number that will be fed serially. Assume that the circuit has an asynchronous Reset input that resets the machine to the reset state.

- (i) Draw the state diagram for your sequential circuit. Make sure that your state machine is minimal and that it does not have any redundant state.
- (ii) Derive minimized equations for the output Z and next state variables.
- (iii) Write a structural Verilog model for modeling your sequential circuit.
- (iv) Write a Verilog test bench to test the correctness of your design for the following input values: $\{X=0\}$, $\{X=1\}$, $\{X=2\}$ $\{X=3\}$ and $\{X=4\}$.

This assignment can be solved based on a group of two students. The solution should be well organized. Submit a soft copy of your solution in a zip file including your Verilog models. Your solution should be submitted in a PDF file that contains the following items:

- i. Your name and ID
- ii. Assignment number
- iii. Problem statement
- iv. Your solution
- v. Include snapshots of simulation output to illustrate the correctness of your models.