## COE 202, Term 052

## Fundamentals of Computer Engineering

## Quiz\# 2

Date: Monday, March 6, 2006
Q.1. Prove the identity of each of the following Boolean functions using algebraic manipulation:
a. $\mathbf{A B C}+\mathbf{A}^{\prime} \mathbf{B}+\mathbf{A}^{\prime} \mathbf{C}^{\prime}=\mathbf{B} \mathbf{C}+\mathbf{A}^{\prime} \mathbf{C}^{\prime}$
$=\mathrm{ABC}+\mathrm{A}^{\prime} \mathrm{B}+\mathrm{BC}+\mathrm{A}^{\prime} \mathrm{C}^{\prime} \quad\left\{\right.$ Consensus on A of the 1 st $\& 2^{\text {nd }}$ term $\}$
$=A^{\prime} B+B C+A^{\prime} C^{\prime} \quad\left\{\right.$ First term absorbed by $3^{\text {rd }}$ term $\}$
$=B C+A^{\prime} C^{\prime} \quad\left\{\right.$ Consensus on C of the $2^{\text {nd }}$ and $3^{\text {rd }}$ term $\}$
$=$ RHS
b. $\mathbf{A B C}+\mathbf{A}^{\prime} \mathbf{B}^{\prime} \mathbf{C}^{\prime}+\mathbf{A} \mathbf{B}^{\prime}+\mathbf{A} \mathbf{C}^{\prime}+\mathbf{A}^{\prime} \mathbf{B}+\mathbf{A}^{\prime} \mathbf{C}=\mathbf{1}$
$=A\left[B C+B^{\prime}+C^{\prime}\right]+A^{\prime}\left[B^{\prime} C^{\prime}+B+C\right] \quad\{$ Distributive law $\}$
$=A\left[B C+(B C)^{\prime}\right]+A^{\prime}\left[(B+C)^{\prime}+B+C\right] \quad\{D e m o r g a n ' s l a w\}$
$=A[1]+A^{\prime}[1]$
$=A+A^{\prime}$
$=1=$ RHS

