

Show all necessary steps for full marks.

Question 1: (9 points): Let U be the universal set, where

$$U = \{\text{all whole numbers less than } 11\}$$

$$A = \{\text{all even natural numbers less than or equal to } 8\}, \text{ and let}$$

$$B = \{y \mid y = x^2 + 2x \text{ where } x \text{ is an integer such that } 0 \leq x < 3\},$$

Answer the following statements as TRUE or FALSE.

(a) $U = ?$

(b) $A = ?$

(c) $A' = ?$

(d) $U' = ?$

(e) $\emptyset' = ?$

(f) $B = ?$

(g) $B' = ?$

(h) $A' \cap B' = ?$

(i) $\emptyset \cap B = \emptyset$

Solution:

(a) $U = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

(b) $A = \{2, 4, 6, 8\}$

(c) $A' = \{0, 1, 3, 5, 7, 9, 10\}$

(d) $U' = \emptyset$

(e) $\emptyset' = U$

(f) $B = \{0, 3, 8\}$

(g) $B' = \{1, 2, 4, 5, 6, 7, 9, 10\}$

(h) $A' \cap B' = \{1, 5, 7, 9, 10\}$

(i) $\emptyset \cap B = \emptyset$

Question 2: (8 points): Answer the following:A. Which is smaller $\frac{8}{11}$ or $\frac{7}{9}$? Why?

Answer: $\frac{8}{11}$ because $\frac{8}{11} = \frac{8(9)}{11(9)} = \frac{72}{99}$ and $\frac{7}{9} = \frac{7(11)}{9(11)} = \frac{77}{99}$

B. Express $\frac{1205}{40}$ as a decimal number.

$$\begin{array}{r} 30.125 \\ 40 \overline{) 1205} \\ \underline{120} \\ 50 \\ \underline{40} \\ 100 \\ \underline{80} \\ 200 \\ \underline{200} \\ 0 \end{array}$$

Answer: $\frac{1205}{40} = 30.125$

C. Express 0.62 as a fraction in its lowest terms.

Answer: $0.62 = \frac{31}{50}$ because $0.62 = \frac{0.62}{1} = \frac{62}{100} = \frac{2(31)}{2(50)} = \frac{31}{50}$

D. Find reciprocal of the mixed number $-2\frac{3}{5}$

Answer: $-\frac{5}{13}$ because $-2\frac{3}{5} = -\left(2\frac{3}{5}\right) = -\left(2 + \frac{3}{5}\right) = -\frac{13}{5}$

Question 3: (4 points):

If $x < -1$, then write expression $|2x| + |-4x| + ||6x||$ without absolute value notation.

Solution:

$$\begin{aligned} |2x| + |-4x| + ||6x|| &= |2x| + |4x| + |6x| \\ &= -2x - 4x - 6x \\ &= -12x \end{aligned}$$

If $x < -1$, then the expression $|2x| + |-4x| + ||6x||$ is equal to

(a) $-12x$

(b) $12x$ (d) $8x$

(c) $-4x$ (e) $4x$

Question 4: (4 points):

If $x = -\frac{3}{4}$ then find the value of the expression $-17 + 3[8x - 4(3x - 2)] = ?$

Solution:

$$\begin{aligned} -17 + 3[8x - 4(3x - 2)] &= -17 + 3[8x - 12x + 8] \\ &= -17 + 3[-4x + 8] \\ &= -17 + 3\left[(-4)\left(-\frac{3}{4}\right) + 8\right] \\ &= -17 + 3[3 + 8] \\ &= -17 + 33 \\ &= 16 \end{aligned}$$

Another Method:

$$\begin{aligned} -17 + 3\left[8\left(-\frac{3}{4}\right) - 4\left(3\left(-\frac{3}{4}\right) - 2\right)\right] &= -17 + 3\left[-6 - 4\left(-\frac{9}{4} - 2\right)\right] \\ &= -17 + 3[-6 + 9 + 8] = -17 + 3(11) = 33 - 17 = 16 \end{aligned}$$