

**King Fahd University of Petroleum and Minerals**  
**Prep-Year Math Program**  
**Math (002)-Term (172)**  
**Recitation (2.8)**

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**Question 1:** Which one of following functions has an inverse?

- (a)  $f(x) = x^2 + 5$
- (b)  $f(x) = |x + 1| - 2, x \geq -2$
- (c)  $f(x) = \sqrt{1 - x^2}$
- (d)  $f(x) = (x + 3)^2 - 5, x \geq -3$

**Question 2:** For the following functions, find  $f^{-1}(x)$  and state its domain and range

- (a)  $f(x) = -\sqrt{4 - x^2}$  for  $-2 \leq x \leq 0$
- (b)  $f(x) = 2 + \sqrt{3 + x}$  for  $x \geq -3$
- (c)  $f(x) = \frac{2x+3}{x-1}$

**Question 3:** If  $f(x) = -x^2 + 4x, x \leq 2$ , then  $f^{-1}(x)$  is

- (a)  $y = 2 \pm \sqrt{4 - x}, x \leq 4$
- (b)  $y = 2 - \sqrt{x - 4}, x \geq 4$
- (c)  $y = 2 - \sqrt{4 - x}, x \leq 4$
- (d)  $y = 2 + \sqrt{4 - x}, x \leq 4$
- (e)  $y = 2 + \sqrt{x - 4}, x \geq 4$

**Question 4:** Let  $f(x) = \frac{3x-k}{x-2}$  and  $f^{-1}(x)$  exists. If  $f^{-1}(-2) = 1$ , then the value of  $k =$

- (a) -1
- (b) 1
- (c) -2
- (d) 2

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**Recitation (4.1&4.2)**

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**Question 1:** If the function  $y = 4^{x+2} - 5$  is written as  $y = k \left(\frac{1}{2}\right)^{bx} + c$ , then  $k + b + c =$

- (a) 11            (b) 7            (c) 9            (d) 13            (e) 12

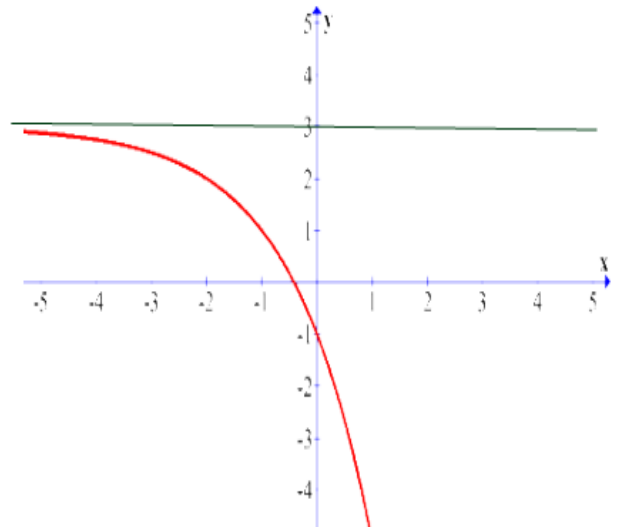
**Question 2:** Find the intersection points of the graphs of  $y = \left(\frac{1}{3}\right)^{2x+5}$  and  $y = 27$

**Question 3:** Graph the function. State the domain, range, and asymptote:

- a)  $y = 3 - 10^{-x}$   
b)  $f(x) = e^{-|x|} - 1$

**Question 4:** The adjacent figure represents the graph of:

- (a)  $y = -\left(\frac{1}{2}\right)^{x+2} + 3$   
(b)  $y = \left(\frac{1}{2}\right)^{x+2} - 3$   
(c)  $y = -(2)^{x+2} + 3$   
(d)  $y = (2)^x + 3$   
(e)  $y = (2)^{x-2} + 3$



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**Recitation (4.3)**

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**Question 1:** Use the definition of the logarithmic function to find  $x$ .

a)  $\log_x 25 = 2$

b)  $\log_7 \frac{1}{49} = 3x$

**Question 2:** Find the domain of the following functions:

a)  $f(x) = \ln x + \ln(2 - x)$

b)  $f(x) = \log_3 \left( \frac{(x-1)^2}{\sqrt{x^2+6x+9}} \right)$

**Question 3:** Graph the function. State the domain, range, and asymptote:

a)  $y = 1 - \log_{10} x$

b)  $y = |\ln x|$

**Question 4:** The graph of  $y = \log_3 |x - 3| - 1$  is below the x-axis on the intervals

(a)  $(2, 3) \cup (3, 4)$

(b)  $(-\infty, 0) \cup (6, \infty)$

(c)  $(-1, 0) \cup (0, 1)$

(d)  $(0, 3) \cup (3, 6)$

(e)  $(-\infty, 2) \cup (3, \infty)$

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**Recitation (4.4)**

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**Question 1:**

1) If  $\log_{10} 2 = 0.30$ ,  $\log_{10} 3 = 0.48$ , then  $\log_{10} \left(\frac{9}{25}\right) =$

- (a)  $-0.24$       (b)  $-0.44$       (c)  $0.36$       (d)  $-0.32$       (e)  $-0.28$

2) If  $\log 2 = c$ , then  $\log_8 \sqrt[3]{10} =$

- (a)  $\frac{1}{9c}$       (b)  $\frac{2}{3c}$       (c)  $\frac{c}{9}$       (d)  $\frac{1}{c}$       (e)  $\frac{3c}{2}$

**Question 2:** Find the value of

- (a)  $\log_{1/2} \sqrt[3]{32} + \log_3 \frac{1}{\sqrt{27}}$       (b)  $\left(\frac{1}{25}\right)^{1-2\log_5 2}$

**Question 3:** Use the Laws of Logarithms to expand the following expression.

$$\log \left( \sqrt{\frac{x^2 + 4}{(x^2 + 1)(x^3 - 7)^2}} \right)$$

**Question 4:** Use the Laws of Logarithms to combine the following expression.

$$\frac{1}{3} \log(x + 2)^3 + \frac{1}{2} [\log x^4 - \log(x^2 - x - 6)^2]$$

**Question 5:** If  $a > 0$ ,  $a \neq 1$ ,  $x > 0$ ,  $x \neq 1$ , then simplify the expression

$$(\log_{\sqrt{10}} 1000)(\log_a \sqrt{x})(\log_{x^3} a)$$

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**Recitation (4.5)**

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**Question 1:** Solve the following equations:

- a)  $4^x + 2^{1+2x} = 50$
- b)  $e^x + 15e^{-x} - 8 = 0$
- c)  $x^2e^x + xe^x = e^x$
- d)  $\log_2(\log_3 x) = 4$

**Question 2:** The sum of all solutions to the equation  $\log_2 \sqrt{x} = \sqrt{\log_2 x}$  is

- (a) 10                      (b) 17                      (c) 21                      (d) 24                      (e) 12

**Question 3:** The number of solutions of the equation  $\log(x^3) = (\log x)^2 + 2$  is equal to:

- (a) 2                      (b) 3                      (c) 1                      (d) 0                      (e) 4

**Question 4:** Find the inverse function of  $f$ .

- a)  $f(x) = 3^{x+1}$
- b)  $f(x) = \log_2(x - 1)$

**Question1.**

Find the least positive angle that is coterminal with the given angle.

- a)  $-800^\circ$
- b)  $1270^\circ$
- c)  $\frac{51\pi}{2}$
- d) 10

**Question2**

If the arc length  $\frac{4\pi}{3}$  cm subtends a central angle  $\theta$  in a circle with diameter 12 cm, find the degree measure of the angle  $\theta$ .

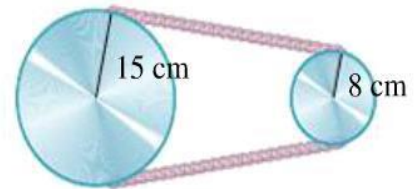
**Question3**

Each tire of a car has a radius of 40 cm. If the tires are rotating at 500 revolutions per minute, find the speed of the car in kilometers per hour.

**Question4**

Two pulleys in the figure have radii of 15cm and 8 cm respectively. If the larger pulley rotates 50 times in a minute, then the angular speed of the smaller pulley in radians per second is

- A)  $\frac{75\pi}{4}$       B)  $\frac{25\pi}{8}$       C)  $\frac{75\pi}{8}$       D)  $\frac{25\pi}{4}$       E)  $\frac{375\pi}{2}$



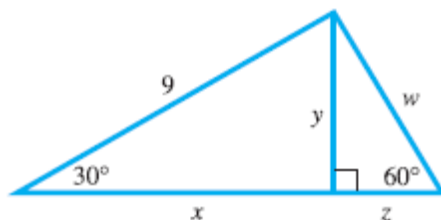
**Question5**

A hard disk in a computer rotates at 300 revolutions per minute. Through how many degrees does a point on the edge of the disk move in 3 seconds?

- A)  $7200^\circ$
- B)  $6400^\circ$
- C)  $10800^\circ$
- D)  $5400^\circ$
- E)  $1800^\circ$

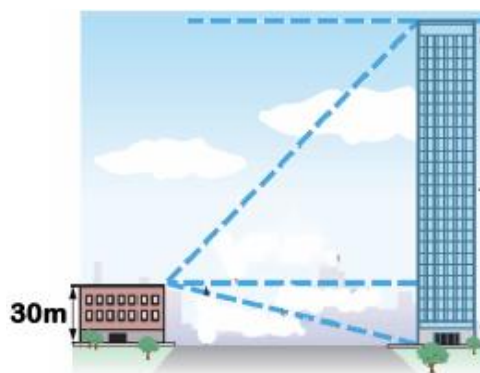
**Question1:** Find the value of  $\left(\sin \frac{\pi}{3} \cos \frac{\pi}{4} - \sin \frac{\pi}{4} \cos \frac{\pi}{3}\right)^2$

**Question2:** Find the exact value of each labeled part with a variable in the following figure



**Question3** The angle of elevation from the top of a small building to the top of a taller building is  $60^\circ$ , while the angle of depression to the bottom is  $30^\circ$ . If the shorter building is 30 m high, then the height of the taller building is

- A)  $(30 + 60\sqrt{3})$ m
- B) 150m
- C)  $100\sqrt{3}$  m
- D) 120m
- E)  $90\sqrt{3}$  m



**Question4**

If from the top of a tower 200 feet high, the angles of depression of the top and bottom of a building opposite to the tower are observed to be  $30^\circ$  and  $60^\circ$ , respectively, then the height of the building is

- A)  $\frac{200\sqrt{3}}{3}$
- B)  $\frac{400}{3}$
- C)  $100\sqrt{3}$
- D)  $\frac{350}{3}$
- E)  $\frac{400\sqrt{3}}{3}$

**Question1:** Find the reference angle for the given angle

- a)  $810^\circ$       b)  $-105^\circ$       c)  $\frac{5\pi}{7}$       d) 20

**Question2:**

Suppose that the terminal side of the angle  $\theta$  in the standard position is defined by  $3x + 2y = 0$ ,  $x \leq 0$ , then find  $\sec \theta$ .

**Question3:**

Let  $\theta$  be an acute angle satisfying  $4 \sin \theta = 5 \cos \theta$ , then find  $4 \tan \theta + \sec \theta$ .

**Question4:**

If  $\cot^2 \theta = 16$  and  $\theta$  terminates in the third quadrant, then  $\sec \theta =$

- A)  $\sqrt{17}$       B)  $\frac{\sqrt{17}}{4}$       C)  $-\frac{\sqrt{17}}{4}$       D)  $-\frac{4}{\sqrt{17}}$       E)  $-\sqrt{17}$

**Question6:**

Find the exact value of the following expressions:

$$\cos\left(\frac{-7\pi}{6}\right) + \sin\left(\frac{17\pi}{3}\right) + 3 \tan\left(\frac{5\pi}{4}\right)$$

**Question6:** If  $\cos \theta = -\frac{2}{7}$  and  $\tan \theta < 0$ , find  $\csc \theta + \tan \theta$



**Question1:** Find the exact value of the following:

1.  $\cos\left(\frac{-7\pi}{6}\right)$       2-  $\sin\left(\frac{-7\pi}{4}\right)$       3-  $\cot\left(\frac{-5\pi}{6}\right)$       4-  $\sec\left(\frac{11\pi}{6}\right)$

**Question2:** If  $\cos 3 = a$  and  $\sin 3 = b$ , then  $a - b =$

- A) a positive real number.
- B) a negative real number.
- C) zero.
- D) undefined.

**Question3:** Write the first expression in terms of the second

- 1-  $\tan x$ ,  $\sin x$       where  $x$  is in Quadrant IV
- 2-  $\tan x$ ,  $\sec x$       where  $x$  is in Quadrant III

**Question4:** Determine whether the function  $f(x) = \cos(\sin x)$  is even, odd, or neither.

**Question5:**

If  $-\frac{\pi}{4} < \theta < \frac{\pi}{4}$ , then which one of the following is **TRUE?**

- a)  $\sin\left(\theta + \frac{\pi}{4}\right) < 0$  and  $\sec\frac{\theta}{2} > 0$       b)  $\sin\left(\theta + \frac{\pi}{4}\right) > 0$  and  $\sec\frac{\theta}{2} < 0$
- c)  $\sin\left(\theta + \frac{\pi}{4}\right) > 0$  and  $\sec\frac{\theta}{2} > 0$       d)  $\sin\left(\theta + \frac{\pi}{4}\right) < 0$  and  $\sec\frac{\theta}{2} < 0$
- e)  $\tan \theta < 0$  and  $\cos \theta > 0$

**Question1:** Graph the following functions:

a)  $f(x) = |\sin x|$

b)  $f(x) = 1 + \cos\left(3x + \frac{\pi}{2}\right)$

**Question2:** Find the amplitude, period, and the horizontal shift of the graph of following function

$$y = \frac{1}{2} - \frac{1}{2} \cos\left(\pi x + \frac{\pi}{2}\right)$$

**Question3:**

If  $A$  is the amplitude,  $P$  is the period,  $M$  is the maximum value and  $m$  is the minimum value of the function  $f(x) = -3 \sin(2\pi x - 1) + 5$ , then  $\frac{A+P}{M+m} =$

A) 3

B)  $\frac{2}{5}$

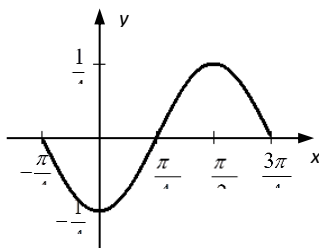
C)  $\frac{11}{10}$

D)  $\frac{7}{10}$

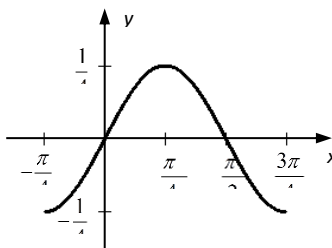
E)  $\frac{9}{5}$

**Question4:** Which one of the following is the graph of  $y = \frac{1}{4} \cos 2\left(x + \frac{\pi}{4}\right)$  over one period?

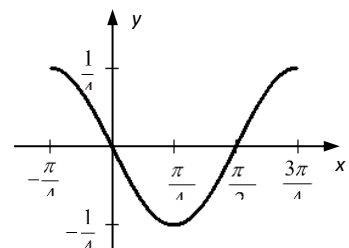
a



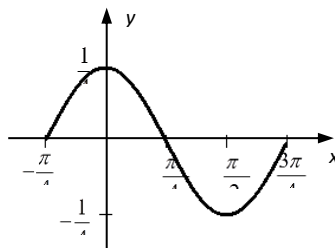
b



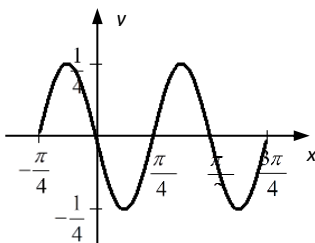
c



d



e



**Question1:**

Graph the following functions:

a)  $y = 4 \tan(4x - 2\pi)$

b)  $y = \frac{1}{2} \sec(2\pi x - \pi)$

**Question2:**

Find the number of vertical asymptotes of the graph of the function

$y = \frac{1}{2} \cot(2x - 3\pi)$  in the interval  $[\frac{\pi}{4}, \frac{7\pi}{4}]$ .

**Question3:**

The intersection point(s) between the graph of  $y = \cot(2x + \frac{\pi}{3})$  and the x-axis

over the interval  $(\frac{\pi}{12}, \frac{4\pi}{3})$  :

A)  $\frac{7\pi}{12}$

B)  $\frac{13\pi}{12}$

C)  $\frac{\pi}{12}, \frac{7\pi}{12}$

D)  $\frac{7\pi}{12}, \frac{13\pi}{12}$

E)  $\frac{\pi}{12}, \frac{13\pi}{12}$

**Question4:**

The graph below can be represented by the trigonometric function

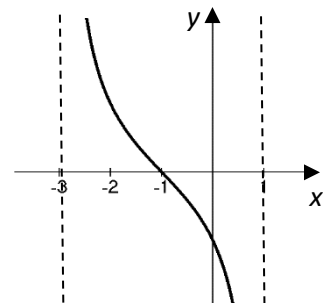
A)  $f(x) = -2 \tan\left(\frac{\pi}{4}x + \frac{\pi}{4}\right)$

B)  $f(x) = 2 \tan\left(\frac{\pi}{4}x + \frac{\pi}{4}\right)$

C)  $f(x) = 2 \cot\left(\frac{\pi}{4}x + 1\right)$

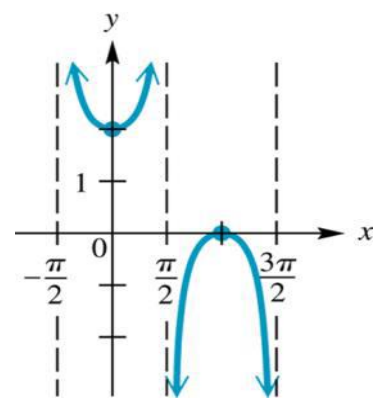
D)  $f(x) = -2 \tan(x + 1)$

E)  $f(x) = 2 \cot(x + 1)$



**Question5**

Write an equation of a function for the given graph





**Question1**

Find the exact value of each expression:

a)  $\cos^{-1}\left(-\frac{\sqrt{3}}{2}\right)$

b)  $\sin^{-1}\left(\frac{\sqrt{2}}{2}\right)$

c)  $\tan^{-1}(-1)$

**Question2**

Find the exact value of

a)  $\cos^{-1}\left(\cos\frac{3\pi}{5}\right)$     b)  $\sin^{-1}\left(\cos\frac{5\pi}{4}\right)$     c)  $\tan^{-1}\left(\tan\frac{4\pi}{3}\right)$     d)  $\sin^{-1}\left[\sin\frac{3\pi}{5}\right]$ .

**Question3**Find the range of  $y = -\cos^{-1}(2 - 7x) + \pi$ .**Question4**The domain of  $y = 2\sin^{-1}\frac{x}{3} =$ 

a)  $[-1,1]$     b)  $[-2,2]$     c)  $[-3,3]$     d)  $[-6,6]$     e)  $\left[-\frac{1}{3},\frac{1}{3}\right]$

**Question5**

$\tan\left[2\cos^{-1}\left(-\frac{4}{5}\right)\right] =$

a)  $\frac{-24}{7}$     b)  $\frac{-25}{24}$     c)  $\frac{25}{24}$     d)  $\frac{7}{24}$     e)  $\frac{24}{7}$

## Recitation (7.1)

**Question1:** Verify the following identities:

$$a) \frac{\sin x + \cos x}{\sec x + \csc x} = \sin x \cos x$$

$$b) \frac{1}{\sec x + \tan x} + \frac{1}{\sec x - \tan x} = 2 \sec x$$

$$c) \frac{\cos^2 x + \tan^2 x - 1}{\sin^2 x} = \tan^2 x$$

**Question2**

If  $A = 2\sin^2 2x + 2\cos^2 2x$  and  $B = 3[\sec^2(-x) - \tan^2(-x)]$ , find  $A + B$ .

**Question3**

If  $\frac{\sin x + \csc x \cos^2 x + 1}{\sec x \csc x - \tan x} = A \sec x + B \tan x$ , find the value of  $A + B$ .

**Question4**

If  $\alpha = \frac{\sin \theta}{1 - \cot \theta}$  and  $\beta = \frac{\cos \theta}{1 - \tan \theta}$  then  $\alpha + \beta =$

- a)  $\sin \theta + \cos \theta$       b)  $\sin \theta - \cos \theta$       c)  $\sec \theta + \csc \theta$   
 d)  $\sec \theta - \csc \theta$       e)  $\tan \theta + \cot \theta$

**Question5:**

If  $\tan(37^\circ) = t$ , then  $\tan 863^\circ + \tan 307^\circ =$

- A) zero    B)  $\frac{t^2+1}{t}$     C)  $-\frac{(t^2+1)}{t}$     D)  $\frac{(t^2-1)}{t}$     E)  $\frac{(1-t^2)}{t}$

**Question1**

Find the value of

- a)  $\sin(-15^\circ)$                       b)  $\cos(\frac{13\pi}{12})$                       c)  $\tan(\frac{17\pi}{12})$   
 d)  $\frac{\tan 70^\circ + \cot 10^\circ}{1 - \tan 80^\circ \cot 20^\circ}$

**Question2:** Verify the following identities:

- a)  $\cot(x + y) = \frac{\cot x \cot y - 1}{\cot x + \cot y}$   
 b)  $\frac{\sin(x+y) - \sin(x-y)}{\cos(x+y) + \cos(x-y)} = \tan y$

**Question3**

If  $\alpha$  and  $\beta$  are two angles in standard position with

$$\sin\alpha = \frac{4}{5}, \quad \frac{\pi}{2} < \alpha < \pi \quad \text{and} \quad \cos\beta = \frac{-5}{13}, \quad \pi < \beta < \frac{3\pi}{2}$$

Then the terminal side of  $(\alpha + \beta)$  is in the quadrant(s)

- a) *I*      b) *II*      c) *IV*      d) *I or II*      e) *II or III*

**Question4**

Graph the following function:

$$f(x) = \cos 2x + \sqrt{3} \sin 2x$$

**Question1:** Verify the following identities:

a)  $\cos^2 x - \sin^2 x = \cos 2x$

b)  $\tan\left(\frac{x}{2}\right) + \cos x \tan\left(\frac{x}{2}\right) = \sin x$

c)  $\frac{1+\sin 2x}{\sin 2x} = 1 + \frac{1}{2} \sec x \csc x$

**Question2**

If  $\frac{\sin^3 x + \cos^3 x}{\sin x + \cos x} = 1 + n \sin(mx)$ , find  $m + n$ .

**Question3**

If  $\cos 3x = A \cos^3 x + B \cos x$ , find  $2A - B$ .

**Question4**

If  $A = \sqrt{\frac{1+\cos 320^\circ}{2}}$  and  $B = \sqrt{\frac{1-\cos 320^\circ}{2}}$ , then  $A + B =$

a)  $\cos 160^\circ - \sin 160^\circ$

b)  $-\cos 160^\circ + \sin 160^\circ$

c)  $\cos 160^\circ + \sin 160^\circ$

d)  $-\cos 160^\circ - \sin 160^\circ$

e) 0

**Question5**

$\cos 13^\circ \cos 9.5^\circ - \sin 13^\circ \sin 9.5^\circ =$

a)  $\frac{1}{2}\sqrt{2 + \sqrt{2}}$

b)  $\frac{1}{2}\sqrt{2 - \sqrt{2}}$

c)  $\frac{1}{2}\sqrt{\sqrt{2} - 2}$

d)  $\frac{-1}{2}\sqrt{2}$

e)  $\frac{1}{2}\sqrt{2}$



**Question1** Solve the following equations:

- a)  $3 \sin^2 \theta - 7 \sin \theta + 2 = 0$
- b)  $\sin 2 \theta + \cos \theta = 0$
- c)  $\tan \frac{\theta}{2} - \sin \theta = 0$

**Question2**

The sum of all solution(s) of the equation

$$\sin x = \cos \frac{x}{2} \text{ in the interval } [0^\circ, 270^\circ) \text{ is}$$

- a)  $\pi$
- b)  $3\pi$
- c)  $\frac{4\pi}{3}$
- d)  $\frac{\pi}{3}$
- e)  $\frac{8\pi}{3}$

**Question3**

The number of solution(s) of  $\sin x - \sqrt{3} \cos x = 1, 0 \leq x < 2\pi$ , is

- a) 1
- b) 2
- c) 3
- d) 4
- e) 5

**Question1**

Are the vectors  $\vec{u} = \langle 2\cos 85^\circ, 2\sin 85^\circ \rangle$  and  $\vec{v} = 3 \langle \cos 25^\circ, \sin 25^\circ \rangle$  orthogonal?

**Question2**

Let  $\vec{u} = 2i - 4j$  and  $\vec{w} = 3i - 3j$

- Find a unit vector in the opposite direction of  $\vec{u}$ .
- Find a vector of magnitude 2 in the direction of  $\vec{w}$ .

**Question3**

Find the value of  $k$  such that the two vectors  $\vec{u} = \langle 3, 4 \rangle$  and  $\vec{v} = \langle 2, k \rangle$  have the same direction.

**Question4**

If  $\vec{u} = \langle -2, 7 \rangle$ , then a nonzero vector that is perpendicular to  $\vec{u}$  is:

- a)  $\langle 14, 4 \rangle$    b)  $\langle -1, 1 \rangle$    c)  $\langle 2, -7 \rangle$    d)  $\langle 1, -1 \rangle$    e)  $\langle 7, -2 \rangle$

**Question1** Solve the following systems:

a) 
$$\begin{cases} x - y = 4 \\ 2x + y = 2 \end{cases}$$

b) 
$$\begin{cases} -\frac{1}{3}x - \frac{1}{6}y = -1 \\ \frac{2}{3}x + \frac{1}{6}y = 3 \end{cases}$$

c) 
$$\begin{cases} -\frac{1}{10}x + \frac{1}{2}y = 4 \\ 2x - 10y = -80 \end{cases}$$

**Question2**

If the following system is dependent, find  $a + b$ .

$$\begin{cases} \frac{3}{2}x - \frac{1}{3}y = \frac{b}{7} \\ \frac{a}{4}x - y = 2 \end{cases}$$

**Question3**

If the system of linear equations

$$\begin{cases} -4x + 4y + 3 = 0 \\ 2x - ky + 2 + k = 0 \end{cases}$$

is inconsistent, then  $k =$

- a) 2      b) 3      c) 4      d) 5      e) 6

## Prep-Year Math Program

### Math 002 - Term 172

#### Recitation (10.4)

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##### Question1

The following system of non-linear equations

$$\begin{cases} 5x^2 + 3y^2 = 23 \\ x^2 - y^2 = 3 \end{cases}$$

has:

- a) No solutions b) One solution c) Two solutions d) Three solutions e) Four solutions

##### Question2

Solve the following system

$$\begin{cases} 2x^2 + xy + y^2 = 4 \\ 3x^2 + 2xy + y^2 = 4 \end{cases}$$

##### Question3

Find the point(s) of intersection of the circle  $(x - 1)^2 + (y - 2)^2 = 8$  and the line  $y = 2x + 2$ .

##### Question4

Find the solution set of the system

$$\begin{cases} \frac{2}{x} - \frac{3}{y} = 1 \\ \frac{7}{y} - \frac{4}{x} = 1 \end{cases}$$

Question5 Solve the following system

$$\begin{cases} x + \sqrt{y} = 0 \\ y^2 - 4x^2 = 12 \end{cases}$$

**Question1** Determine whether the following system is independent, inconsistent or dependent

$$i) \begin{cases} x - 2y + z = 1 \\ y + 2z = 5 \\ x + y + 3z = 8 \end{cases}$$

$$ii) \begin{cases} x + y + z = 2 \\ y - 3z = 1 \\ 2x + y + 5z = 0 \end{cases}$$

$$iii) \begin{cases} x + 2y + z = 1 \\ 5x + 2y + 3z = 4 \\ 3x - 2y + z = 2 \end{cases}$$

**Question2:** Use the Gauss Jordan method to solve the following linear system

$$\begin{cases} x + y + 6z = 3 \\ x + y + 3z = 3 \\ x + 2y + 4z = 7 \end{cases}$$

**Question3**

If the echelon form of the linear system

$$\begin{cases} x - 3y + z = 8 \\ 2x - 5y - 3z = 6 \\ x - 6y + 7z = -7 \end{cases} \quad \text{is} \quad \left[ \begin{array}{ccc|c} 1 & -3 & 1 & 8 \\ 0 & 1 & m & n \\ 0 & 0 & 1 & p \end{array} \right], \quad \text{then } (m, n, p) =$$

- a)  $(-5, -10, 5)$       b)  $(3, -6, -3)$       c)  $(-5, 10, -3)$       d)  $(-2, 7, -1)$   
 e)  $(-3, 6, -2)$

**Question1**

If  $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 4 \end{bmatrix}$ , and  $B = \begin{bmatrix} 2 & 3 & 5 \\ 0 & -4 & 2 \\ 0 & 0 & -3 \end{bmatrix}$ , then find

- $A + B$
- $BA$
- $B^2$

**Question2** If  $A, B$  and  $C$  are square matrices and  $I_n$  is the identity matrix, which one of the following statement is True?

- $(A + B)(A^2 - AB + B^2) = A^3 + B^3$
- $(A + I_n)(A - I_n) = A^2 - I_n$
- $(A - B)^2 = A^2 - 2AB + B^2$
- $AB = 0$  implies  $A = 0$  or  $B = 0$
- $I_n A = I_n$

**Question3**

If  $A = \begin{bmatrix} 1 & 3 & 4 \\ -2 & 2 & 5 \\ 1 & 3 & 2 \end{bmatrix}$ ,  $B = \begin{bmatrix} 6 & 0 & 2 \\ 0 & 1 & 3 \\ -1 & 2 & 5 \end{bmatrix}$ , and  $C = AB$ ,  
then  $c_{32} + c_{13} =$

- a) 52    b) 11    c) 38    d) -15    e) 9

**Question4**

If  $A = \begin{bmatrix} 1 & 2 & 4 \\ -1 & 0 & 5 \end{bmatrix}$  and  $B = \begin{bmatrix} 0 & 2 & 1 \\ 3 & -1 & 2 \end{bmatrix}$ , then find the matrix  $X$  that satisfies  $4X + B = 2X + 3A$ .

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**Question1**

Find the inverse of the matrix if it exists

(a)  $A = \begin{bmatrix} 2 & 4 & 1 \\ -1 & 1 & -1 \\ 1 & 4 & 0 \end{bmatrix}$

(b)  $B = \begin{bmatrix} 3 & 2 \\ 6 & 4 \end{bmatrix}$ .

**Question2**

Use the inverse of the coefficient matrix to solve the following system

$$\begin{cases} 2x + y = -7 \\ 3x + 2y = 19 \end{cases}$$

**Question3**

Given that  $M = \begin{bmatrix} 2 & 9 \\ 1 & 5 \end{bmatrix}$  and  $N = \begin{bmatrix} -1 & -1 \\ 4 & 3 \end{bmatrix}$ , find the sum of the elements in the second column of  $(MN)^{-1}$ .

**Question4**

If A and B are 3x3 matrices such that  $|A| = 5$  and  $|B| = -2$ , then  $|3(A B^2)^{-1}| =$

- a) 27/20    b) 15/10    c) -30/4    d) 10/27    e) 540

**Question1**

$$\text{If } A = \begin{bmatrix} 2 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \\ 1 & 6 & 2 & 2 \\ 1 & 1 & -2 & 3 \end{bmatrix} \text{ and } B = \begin{bmatrix} 2 & 1 & 2 & 1 \\ 3 & 0 & 1 & -1 \\ -1 & 2 & -2 & 1 \\ -3 & 2 & 3 & 2 \end{bmatrix}, \text{ then}$$

- a) Find the sum of the cofactors of  $A_{23}$  and  $B_{44}$  .  
 b) Find  $|A|$ .

**Question2**

Evaluate the following determinants

$$\begin{array}{lll} \text{a) } \begin{vmatrix} 3 & 5 \\ 2 & 4 \end{vmatrix} & \text{b) } \begin{vmatrix} 2 & 0 & 0 \\ 4 & 1 & 0 \\ 7 & 3 & -2 \end{vmatrix} & \text{c) } \begin{vmatrix} 3 & 0 & 0 \\ 2 & 1 & 1 \\ 1 & 2 & 2 \end{vmatrix} \\ \text{d) } \begin{vmatrix} 4 & 0 & 2 & 1 \\ 5 & 0 & 4 & 2 \\ 2 & 0 & 3 & 4 \\ 1 & 0 & 2 & 3 \end{vmatrix} & & \text{e) } \begin{vmatrix} 5 & -13 & -3 \\ -2 & 5 & 1 \\ -2 & 6 & 2 \end{vmatrix} \end{array}$$

**Question3** Let  $A$  and  $B$  be  $4 \times 4$  invertible matrices. Which one of the following statement is false

- a)  $|A^2| = |A|^2$   
 b)  $|2B| = 16|B|$   
 c)  $|A \cdot B| = |A| \cdot |B|$   
 d)  $|A + B| = |A| + |B|$   
 e)  $|I_n| = 1$

**Question4**

$$\text{If } \det(M - xI) = 0, \quad M = \begin{bmatrix} 2 & -1 \\ 1 & 0 \end{bmatrix} \text{ and } I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \text{ then } x =$$

- a) 1            b) 2            c) 3            d) -1            e) -1/2



**Question1**

Which one of the following is the equation in standard form of the parabola with directrix  $y = 7$  and focus  $(1,3)$

a)  $y - 5 = -\frac{1}{8}(x - 1)^2$

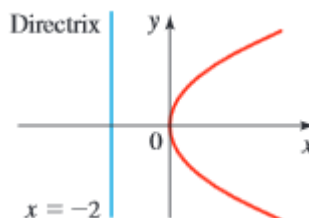
b)  $x - 5 = -\frac{1}{8}(x - 1)^2$

c)  $y - 5 = \frac{1}{8}(x - 1)^2$

d)  $x - 1 = \frac{1}{8}(y - 4)^2$

e)  $y - 5 = \frac{1}{4}(x - 1)^2$

**Question2** Find an equation of the parabola from the given graph



**Question3**

Find the vertex, focus, and directrix of the parabola given by the equation:

$$3x^2 - 12x - y + 14 = 0$$

**Question4**

Which of the following points lies on the parabola that has vertex  $(2, 1)$  and focus  $(2, 3)$ ?

A)  $(4, 2)$

B)  $(6, 3)$

C)  $(5, 3)$

D)  $(1, -3)$

E)  $(-1, 3)$

**Question1**

Find the center, the vertices, foci, and eccentricity of the ellipse given by the equation

- a)  $3x^2 + 2y^2 - 6x + 12y = -15$
- b)  $3y^2 + 2x^2 - 6y + 12x = -15$

**Question2**

- 1) Find the equation of the ellipse that has vertices at (3,8) and (3,-2), and foci at (3,6) and (3,0).
- 2) Find the equation in standard form, of the ellipse with foci at (-1,2) and (3,2) that passes through the point (3,5).

**Question3**

Find the points of intersection of the ellipse  $\frac{(x+1)^2}{16} + \frac{(y-2)^2}{9} = 1$ , and the hyperbola  $\frac{(x+1)^2}{16} - \frac{(y-2)^2}{9} = 1$ .

**Question4**

Find the eccentricity of the hyperbola with asymptotes  $y = \pm \frac{4}{5}x + 5$  and one vertex at (5,5).

- a)  $\frac{\sqrt{41}}{5}$
- b)  $\frac{\sqrt{35}}{5}$
- c)  $\frac{3}{2}$
- d)  $-\frac{5}{2}$
- e)  $\frac{1}{3}$

**Question5**

Find the equation in standard form of the hyperbola with vertices (-1,0) and (-1,-4), and eccentricity  $e = \frac{\sqrt{5}}{2}$ .

**Question6**

Write the following equations in standard form and identify the corresponding conics

- a)  $x^2 - 4x + y^2 + 2y + 2 = 0$
- b)  $2x^2 - 8x - 2y^2 - 4y = 0$
- c)  $27x^2 + 36y^2 + 18x + 36y - 96 = 0$