

**King Fahd University of Petroleum and Minerals**  
**Prep-Year Math Program**  
**Math (001)-Term (181)**  
**Recitation (3.3)**

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**Question 1:** When  $x^3 - 3x^2 - x - 1$  is divided by  $x - k$  and the remainder  $-4$ , then the sum of all values of  $k$  is:

- (a): 3            (b): 1            (c):  $-1$             (d): 0            (e): 2

**Answer:** (a): The sum is 3

**Question 2:** If  $P(x) = x^{105} - x^{10} - 2x + 1$  is divided by  $x + 1$ , then the remainder is:

- (a): 2            (b): 1            (c):  $-1$             (d): 0            (e):  $-2$

**Answer:** (b): 1

**Question 3:** If  $x + 2$  is a factor of polynomial  $P(x) = x^3 - kx^2 + 3x + 7k$ , then  $k$  is equal to

- (a):  $\frac{10}{3}$             (b):  $\frac{13}{3}$             (c):  $\frac{11}{3}$             (d):  $\frac{16}{3}$             (e):  $\frac{14}{3}$

**Answer:** (e):  $\frac{14}{3}$

**Question 4:** If  $P(x) = -x^3 + kx^2 - 5x - 20$  is divided by  $x + 2$ , then the set of all values of  $k$  which makes the remainder positive is

- (a):  $\left(\frac{9}{2}, \infty\right)$     (b):  $\left(\frac{19}{2}, \infty\right)$     (c):  $\left(\frac{11}{2}, \infty\right)$     (d):  $\left(\frac{1}{2}, \infty\right)$     (e):  $\emptyset$

**Answer:** (d):  $\left(\frac{1}{2}, \infty\right)$

**Question 5:** If 2 is a zero of multiplicity 2 of  $P(x) = x^4 + ax^3 + 8x^2 - 16x + b$  then find  $a$  and  $b$ .

**Answer:**  $\boxed{a = -4}$      $\boxed{b = 16}$

**Question 6:** If  $\frac{2x^5 + x^3 - 2x^2 + 3x - 5}{x^2 - 3x + 1} = Q(x) + \frac{R(x)}{x^2 - 3x + 1}$ , then what are  $Q(x)$  and  $R(x)$ ?

**Answer:**  $Q(x) = 2x^3 + 6x^2 + 17x + 43$      $R(x) = 115x - 48$