

**King Fahd University of Petroleum and Minerals**  
**Prep-Year Math Program**  
**Math 002 - Term 132**  
**Recitation (9.7)**

**Question 1:** If  $\begin{bmatrix} x+2 & 8 & -3 \\ 1 & 2y & 2x+1 \\ 7 & -2 & y+2 \end{bmatrix} = \begin{bmatrix} 2x+6 & 8 & -3 \\ 1 & 18 & -7 \\ 7 & -2 & 11 \end{bmatrix}$ , then  $x + y =$

A) -13      B) -5      C) 5      D) 4      E) 13

**Answer:**  $x + y = -4 + 9 = 5$

**Question 2:** If  $A = \begin{bmatrix} 1 & -2 & 2 \\ 3 & 1 & -1 \\ 1 & 1 & 4 \end{bmatrix}$ , then find the element in the third row and second column of the matrix  $A^2 + 3A - 2I_3$

**Answer:**  $c_{32} = 6$

**Question 3:** If  $A$ ,  $B$  and  $C$  are  $n \times n$  matrices and  $I_n$  is the identity matrix of order  $n$ , then which of the following statements is TRUE?

- A)  $(A + I_n)(A - I_n) = A^2 - I_n^2$       (True) because  $(A + I_n)(A - I_n) = A^2 - A + A - I_n^2 = A^2 - I_n^2$
- B)  $(A - B)^2 = A^2 - 2AB + B^2$       (False)
- C)  $A^2C = ACA$       (False)
- D)  $(A + I_n)^2 = A^2 + I_n$       (False)
- E)  $(A + B)(A^2 - AB + B^2) = A^3 + B^3$       (False)

**Question 4:** If  $A = \begin{bmatrix} -1 & 2 & -3 \\ 6 & -1 & 2 \end{bmatrix}$ ,  $B = \begin{bmatrix} 0 & -1 & 4 \\ -2 & 6 & -3 \end{bmatrix}$ , then find the matrix  $X$  for which  $4X + B = X - 2A$ .

**Answer:**  $X = \begin{bmatrix} \frac{2}{3} & -1 & \frac{2}{3} \\ -\frac{10}{3} & -\frac{4}{3} & -\frac{1}{3} \end{bmatrix}$