

King Fahd University of Petroleum and Minerals

Prep-Year Math Program

Math 002 - Term 132

Recitation (7.1)

Question 1:

a) Find the exact value of $\sin 44^\circ + \cos 134^\circ + \sin(-510^\circ)$.

b) If $\sec x = -\frac{13}{12}$, find all possible values of $\frac{\sin x + \cos x}{\sec x}$

Answer (a): $-\frac{1}{2}$

Answer (b): $\frac{84}{169}$ or $\frac{204}{169}$

Question 2:

(i): If $\tan \theta = 2.6$, then $\tan(-\theta) =$

(ii): If $\cos \theta = -.65$, then $\cos(-\theta) =$

(iii): If $\cos \theta = .8$ and $\sin \theta = .6$, then $\tan(-\theta) =$

(iv): If $\sin \theta = \frac{2}{3}$, then $-\sin(-\theta) =$

(v): If $\cos \theta = -\frac{1}{5}$, then $-\cos(-\theta) =$

Answer: (i): -2.6 (ii): $-.65$ (iii): $-\frac{4}{3}$ (iv): $\frac{2}{3}$ (v): $\frac{1}{5}$

Question 3 Write $\csc t$ in terms of $\tan t$, where $\pi < t < \frac{3\pi}{2}$.

Solution:

$$\csc^2 t = 1 + \cot^2 t$$

$$\csc t = -\sqrt{1 + \cot^2 t}$$

$$= -\sqrt{1 + \frac{1}{\tan^2 t}}$$

$$= -\sqrt{\frac{\tan^2 t + 1}{\tan^2 t}}$$

$$= -\frac{\sqrt{\tan^2 t + 1}}{\sqrt{\tan^2 t}}$$

$$= -\frac{\sqrt{\tan^2 t + 1}}{|\tan t|}$$

$$= -\frac{\sqrt{\tan^2 t + 1}}{\tan t} \quad (\text{because } \tan t \text{ is positive for } t \text{ in Quadrant III})$$

Answer: $-\frac{\sqrt{\tan^2 t + 1}}{\tan t}$

Question 4:

Determine whether the function is even, odd, or neither.

A) $f(x) = \frac{\tan x - \sin x}{x \sec x}$ B) $f(x) = 2x \cos x - x^2 \csc x$ C) $h(x) = \frac{x \tan x - \cos x}{x - \sec x}$

Answer:

(A): f is even.

(B): f is odd.

(C): h is neither odd nor even.

Question 5:

If $\tan(-\theta) = \frac{1}{4}$ and $\sec \theta > 0$, then $\sin \theta =$

A) $-\frac{\sqrt{17}}{17}$

B) $\frac{\sqrt{17}}{17}$

C) $\frac{4\sqrt{17}}{17}$

D) $-\frac{4\sqrt{17}}{17}$

E) $\frac{\sqrt{15}}{15}$