KFUPM, Math 001 Recitation 3.3, Term 131, Answered by Sayed Omar, Page 1/1 21-Dec-13 King Fahd University of Petroleum and Minerals Prep-Year Math Program Math 001 - Term 131 Recitation (3.3)

Question 1: If x + 2 is a factor of the polynomial $p(x) = x^5 - 2x^3 + 5x^2 - kx + 2$ find value of k. Answer: k = -3

Question 2: If x = -1 is a zero with multiplicity 2 of the polynomial $P(x) = x^4 + x^3 + x^2 + kx + k - 1$ Then find k Answer: k = 3

<u>Question 3:</u> According to Descartes' Rules of Signs, find the number of possible positive and the number of possible negative real zeros of the polynomial

 $p(x) = 5x^4 + x^3 + 3x^2 - 3x - 1 \implies$ One positive real zero

$$P(x) = 5x^4 + x^3 + 3x^2 - 3x - 1$$

Answer:

 $p(-x) = 5x^4 - x^3 + 3x^2 + 3x - 1 \implies$ Either 3 negative or one negative real zero

: One positive and either three or one negative zeros

Question 4: If x = i is a zero of $P(x) = 8x^5 - 12x^4 + 14x^3 - 13x^2 + 6x - 1$, then find the other zeros

Answer: The other zeros are -i, $\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$. The other zeros are -i and $\frac{1}{2}$ with multiplicity 3

Question 5: The Polynomial $p(x) = 8x^3 + 8x^2 - 4x - 1$ has

- A) one rational and two irrational zeros.
- B) no real zeros.
- C) three irrational zeros.
- D) two rational and one irrational zeros.
- E) three irrational zeros.

<u>Question 6:</u> A polynomial of lowest degree with real coefficients having -2i, *i* and 0 of multiplicity 2 as roots is.

A)
$$x^{5} + 3x^{3} + 4x$$

B) $x^{6} + 5x^{4} + 4x^{2}$
C) $x^{4} + ix^{3} + 2x^{2}$
D) $x^{2}(x+2i)^{2}(x-i)^{2}$
E) $x^{2}(x^{2}-4)(x^{2}-1)$

Answer: $x^{6} + 5x^{4} + 4x^{2}$