King Fahd University of Petroleum and Minerals Prep-Year Math Program Math (001)-Term (131)

Recitation R.4

Answered by Sayed Omar

Question 1: Find $\sqrt{25^2 - 24^2}$

Answer: 7

Question 2: Factor the following completely:

(a)
$$2x^3y - 8(xy)^2 + 6y^3$$

$$(d) 9x^2 + 3x - y - y^2$$

$$(b) x (2x + 3) - 2$$

$$(e) x^6 + 7x^3 - 8$$

(c)
$$(2a-b)^2 - (a+2b)^2$$

$$(f) 4x^3 - 8x^2y - xy^2 + 2y^3$$

Answer:

(a):
$$2y(x^3-4x^2y+3y^2)$$

(b):
$$(2x-1)(x+2)$$

(c):
$$(3a+b)(a-3b)$$

(d):
$$(3x - y)(3x + y + 1)$$

(e):
$$(x+2)(x^2-2x+4)(x-1)(x^2+x+1)$$

(f):
$$(x-2y)(2x+y)(2x-y)$$

Question 3: Find all values of k such that $16x^2 + kx + 4$ is a perfect square.

Answer: $k = \pm 16$

Question 4: One factor of the polynomial $x^2y^2 - 1 - 2xyz + z^2$ is

(a)
$$(xyz -1)$$

$$(b) (xy + z + 1)$$

$$(c) (xy - z - 1)$$

$$(d)(xy + z - 1)$$

(e)
$$(x + y + z + 1)$$

Answer: (c):(xy-z-1)

Question 5: Facorization of: $10x^3y - 15xy^3 + 25x^2y^2$ is equal to:

(a)
$$5xy(2x + y)(x - 3y)$$

(b)
$$10xy(x-y)(x+3y)$$

$$(c) 5xy (2x - y)(x + 3y)$$

$$(d) 5xy (x - y)(2x + 3y)$$

(e)
$$5(2x^2-y^3)(x+3y)$$

Answer: (c):
$$5xy(2x - y)(x + 3y)$$

Question 6: Factor $x^4 - x^2 + 16$. (Hint: add and subtract a term)

Answer:
$$(x^2 + 4 + 3x)(x^2 + 4 - 3x)$$