

Q1.

The polynomial  $P(x) = x^4 + 2x^3 - 8x^2 - 20x - 20$  has a zero between

- A) 0 and 1
- B) 4 and 5
- C) 2 and 3
- D) 1 and 2
- E) 3 and 4

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Q2.

The graph of  $y = \frac{3x^4 + 4}{x^3 + 3x}$  intersects its slant asymptote at

- A)  $(\frac{2}{3}, -2)$
  - B)  $(\frac{2}{3}, 2)$
  - C)  $(-2, -\frac{2}{3})$
  - D)  $(-\frac{2}{3}, 2)$
  - E)  $(2, \frac{2}{3})$
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Q3.

If  $x = 2 - i$  is a zero of the polynomial  $p(x) = x^4 - 6x^3 + 10x^2 + 2x - 15$  then the sum of the **remaining** real zeros of  $p(x)$  is

- A) 4
- B) 0
- C) -4
- D) 2
- E) 3

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Q4.

The standard form of the complex number  $\frac{(5+2i)(2-3i)}{5-i}$  is

- A)  $\frac{91}{26} + \frac{39}{26}i$
- B)  $\frac{69}{26} - \frac{39}{26}i$
- C)  $\frac{69}{26} + \frac{39}{26}i$
- D)  $\frac{91}{24} - \frac{39}{24}i$
- E)  $\frac{91}{26} - \frac{39}{26}i$

Q5.

If we solve the equation  $\frac{b+c}{x+a} = \frac{b-c}{x-a}$  for  $x$ , we find

A)  $x = \frac{ab}{c}$

B)  $x = \frac{(x-a)(b+c)}{b-c}$

C)  $x = \frac{b-c}{b+c}$

D)  $x = \frac{(x+a)(b-c)}{b+c} + a$

E)  $x = \frac{2a-2c}{b}$

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Q6.

If the polynomial  $P(x) = 6x^3 - 16x^2 + 23x - 5$  is divided by  $3x - 2$ , then the sum of the remainder and the quotient is

A)  $2x^2 + 4x$

B)  $2x^2 - 4x$

C)  $2(x^2 - 2x + 5)$

D)  $2x^2 - 4x - 10$

E)  $2x^2 + 4x + 10$

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Q7.

If  $\left(\frac{x}{3}, \frac{3}{2}\right)$  is the midpoint of the line segment joining the points  $(6, 2y)$  and  $\left(-\frac{4}{3}, \frac{7}{2}\right)$ , then  $x + y =$

A)  $\frac{27}{4}$

B)  $\frac{19}{4}$

C)  $\frac{15}{2}$

D)  $\frac{14}{3}$

E)  $\frac{17}{6}$

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Q8.

If 2 is a zero of multiplicity 2 of  $P(x) = 6x^4 + ax^3 - 2x^2 + 44x + b$ , then  $a =$

A) 25

B) -33

C) -25

D) -15

E) -19

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Q9.

The absolute value notation which describes the statement "the distance between  $-a$  and  $-b$  is not less than 3" is

A)  $|a + b| > 3$

B)  $|-a - b| < 3$

C)  $|a - b| \geq 3$

D)  $|a + b| \leq 3$

E)  $|a - b| \leq 3$

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Q10.

The expression  $\frac{(2a^{1/3}b^{3/2})(-6a^{-1/5}b^{-3/4})}{(3a^{3/5}b^{1/5})(4a^{2/3}b^{1/2})}$  simplifies to

A)  $a^{7/15}b$

B)  $-a^{-17/15}b$

C)  $-a^{-17/15}b^{1/20}$

D)  $-a^{-12/15}b^2$

E)  $a^{7/15}b^2$

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Q11.

If  $f(x) = \frac{3x}{x-2}$ , then the inverse function  $f^{-1}(x) =$

A)  $x$

B)  $\frac{2x}{x-3}$

C)  $\frac{2x}{x-2}$

D)  $\frac{x-3}{3x}$

E)  $\frac{3x}{x-3}$

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Q12.

One factor of  $8x^2 - 26xy + 15y^2$  is

A)  $2x - 3y$

B)  $4x + 3y$

C)  $4x - 3y$

D)  $4x - 5y$

E)  $2x + 5y$

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Q13.

The coefficient of  $x^4$  in the product  $(3x^2 - 2)^3(2x^2 - 3)$  is

A) 162

B) 269

C) 108

D) 234

E) 72

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Q14.

If  $P(x) = x^3 - 18x^2 + 19x - 37$ , then  $P(17) =$

A) 1

B) -3

C) 2

D) -2

E) -1

Q15.

The graph of the function  $f(x) = \frac{(x+1)(x+3)}{(x+6)(x-2)}$  is

- A) decreasing on  $(-6, -3)$
- B) increasing on  $(-\infty, -6)$
- C) below the  $x$ -axis on  $(-\infty, -6)$
- D) over the  $x$ -axis on  $(-6, -3)$
- E) increasing on  $(2, \infty)$

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Q16.

If  $(a, b)$  and  $(c, d)$  are two points at which the graph of  $f(x) = \frac{x^3 + x^2 + 4x + 1}{x^3 + 1}$  intersects its horizontal asymptote, then  $a + b + c + d =$

- A) 3
  - B) -2
  - C) -3
  - D) 1
  - E) -1
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Q17.

If the solution set of the inequality  $|2 - 4x| \leq 2$  is equal to  $[m, n]$  and the solution set of the inequality  $\frac{4x + 1}{3} > 7 - \frac{x}{3}$  is equal to  $(k, \infty)$ , then  $m + n + k =$

A) 0

B)  $\frac{5}{3}$

C) 5

D)  $\frac{3}{2}$

E) 3

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Q18.

The graph of  $f(x) = -x^3 - 2x^2 + 3x$  is above or on the  $x$ -axis on

A)  $(-3, 1) \cup (1, \infty)$

B)  $(-3, -1) \cup (0, 1)$

C)  $(-\infty, -3] \cup [0, 1]$

D)  $(-3, -1) \cup (1, \infty)$

E)  $(-\infty, -3) \cup (1, \infty)$

Q19.

The minimum value of the function  $f(x) = (2x - 1)(x + 3) - 4$  is at  $x =$

A)  $\frac{7}{4}$

B)  $-\frac{5}{4}$

C)  $-\frac{7}{4}$

D)  $-\frac{5}{2}$

E)  $\frac{5}{2}$

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Q20.

Which one of the following is a factor of  $P(x) = x^3 + x^2 + x - 14$ ?

A)  $x - 1$

B)  $x - 7$

C)  $x + 2$

D)  $x - 2$

E)  $x + 1$

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Q21.

If  $x = \frac{5 - \sqrt{21}}{2}$ , then  $x + \frac{1}{x}$  is equal to

A)  $5 + \sqrt{21}$

B) 23

C) 10

D) 5

E)  $5 - \sqrt{21}$

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Q22.

The expression  $\frac{x-y}{xy} + \frac{x-z}{xz} - \frac{z-y}{yz}$  simplifies to

A)  $\frac{2(x-z)}{xz}$

B)  $\frac{2(x-y)}{xy}$

C)  $\frac{2(x+z)}{xz}$

D)  $\frac{2(y-z)}{yz}$

E)  $\frac{2(x+y)}{xy}$

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Q23.

The polynomial function  $f$  of lowest degree with real coefficients that satisfies the condition  $f(2) = 5$  and has the zeros  $5$  and  $i$  is

A)  $f(x) = x^3 + x^2 + x - 5$

B)  $f(x) = -\frac{1}{3}x^3 + \frac{5}{3}x^2 - \frac{1}{3}x + \frac{5}{3}$

C)  $f(x) = -\frac{1}{3}x^3 + 2x - 1$

D)  $f(x) = \frac{1}{3}x^3 + \frac{5}{3}x^2 - \frac{1}{3}x + 5$

E)  $f(x) = x^2 + 1$

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Q24.

If  $f(x) = 2x^2 - 9$ ,  $g(x) = ax + b$  and  $(f \circ g)(x) = x^2 + 4x - 5$ , then  $b^2 - a^2 =$

A)  $-8$

B)  $\frac{5}{2}$

C)  $\frac{3}{2}$

D)  $3$

E)  $5$

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Q25.

If  $L$  is a line perpendicular to  $2y + x = 5$ , and both lines pass through the point  $(-1, 3)$ , then the sum of the slopes of the two lines is

A)  $-\frac{1}{2}$

B)  $\frac{1}{2}$

C)  $\frac{5}{2}$

D) 0

E)  $\frac{3}{2}$

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Q26.

The sum of all solutions of the equation  $\frac{\frac{1}{1-x} + 3}{5 + \frac{1}{1-x}} = \frac{\frac{1}{1-x} - 3}{\frac{1}{1-x} - 4}$  is

A) 1

B)  $-\frac{1}{2}$

C) -1

D) 0

E)  $\frac{1}{2}$

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Q27.

The sum of all solutions of the equation  $2x^{\frac{1}{2}} - x^{\frac{1}{4}} = 6$  is

A) 16

B) 8

C)  $\frac{175}{16}$

D)  $\frac{1}{2}$

E)  $\frac{337}{16}$

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Q28.

If  $f(x) = (x-2)^2 - 4$  and  $g(x) = -f(x-2) - \frac{3}{2}$ , then  $g(x) =$

A)  $-(x-4)^2 - \frac{11}{2}$

B)  $-x^2 + \frac{5}{2}$

C)  $-(x-4)^2 + \frac{5}{2}$

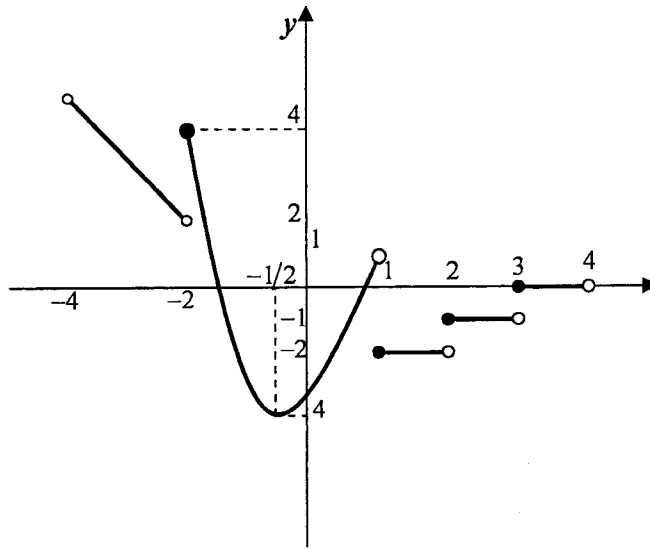
D)  $-(x-2)^2 - \frac{5}{2}$

E)  $-(x-2)^2 + \frac{11}{2}$

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Q29.

Which one of the following statements is TRUE for the function whose graph is given below?



- A) The function is increasing on  $(-1/2, 1)$
- B) The range of the function  $[-4, 4]$
- C) The domain of the function is  $[-2, 4)$
- D) The function is decreasing on  $(-1/2, 1)$
- E) The function is increasing on  $(-\infty, -2)$

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Q30.

The sum of all values of  $k$  for which the equation

$$kx^2 + 2(k+4)x + 25 = 0$$

has exactly one solution is

- A) 15
  - B) -4
  - C) 7
  - D) 17
  - E) -8
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Item 005  
Q31.

The expression  $x - \frac{x}{x + \frac{1}{2}}$  can be simplified to

A)  $-2x$

B)  $2x - 1$

C)  $\frac{-x}{2x + 1}$

D)  $\frac{x(2x - 1)}{2x + 1}$

E)  $x$

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Q32.

One factor of  $16x^{4n} - 8x^{2n} + 1$  is

A)  $4x^n + 1$

B)  $2x^{2n} - 1$

C)  $2x^n - 1$

D)  $2x^{2n} + 1$

E)  $4x^n - 1$



Q33.

If  $f(x) = (x + 2)^2(x - 3)^3(x^2 + 1)^2$ , then the graph of  $f$

- A) crosses the  $x$ -axis at  $(-1, 0)$  and  $(1, 0)$
- B) intersects but does not cross the  $x$ -axis at  $(-2, 0)$
- C) intersects but does not cross the  $x$ -axis at  $(3, 0)$
- D) intersects but does not cross the  $x$ -axis at  $(1, 0)$  and  $(-2, 0)$
- E) crosses the  $x$ -axis at  $(3, 0)$  and  $(-2, 0)$

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Q34.

The sum of all zeros of  $f(x) = 9x^3 + 36x^2 + 41x + 10$  is

- A)  $-5$
- B)  $-6$
- C)  $-3$
- D)  $-4$
- E)  $-10$

Q35.

The polynomial  $P(x) = x^4 - 8x^3 + 24x^2 - 32x + 16$  has

- A) Four non-real complex zeros.
- B) One rational zero of multiplicity 4.
- C) Two rational and two irrational zeros.
- D) Two rational zeros and two non-real zeros.
- E) Two rational zeros of multiplicity 2 each.

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Q36.

The sum of all solutions of the equation  $3|x-3| = 7-x$  is

- A) 8
- B) 3
- C) -2
- D) 5
- E) -7