

Name : _____ ID. # : _____ SER. # : _____

Complete the following, show your work and simplify your answer:

- If $A = \{x|x \text{ is an odd positive integer, } 4 \leq x \leq 16\}$ and $B = \{x|x \text{ is a prime number } < 12\}$, then $A \cap B = \dots\dots\dots$

Ans : $A = \{5, 7, 9, 11, 13, 15\}$; $B = \{2, 3, 5, 7, 11\}$; $A \cap B = \{5, 7, 11\}$

- The coefficient of x^2 in the product $(2x^2 + 3x - 1)(3x^2 - 5x + 2)$ is $\dots\dots\dots$

Ans : The coefficient of $x^2 = 2(2) - 1(3) + 3(-5) = -14$

- The multiplicative inverse of -0.04 is $\dots\dots\dots$

Ans : The multiplicative inverse of -0.04 is $\frac{1}{-0.04} = -\frac{1}{\frac{4}{100}} = -\frac{100}{4} = -25$

- If $1 < x < 2$, then $\left| \frac{x-2}{|x| - |x-1|} \right| = \dots\dots\dots$

Ans : $= \left| \frac{x-2}{x - (x-1)} \right| = \left| \frac{x-2}{x-x+1} \right| = |x-2| = -(x-2) = 2-x$

- When rationalized, the expression $\frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} + \sqrt{2}} = \dots\dots\dots$

Ans : $= \frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} + \sqrt{2}} \cdot \frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} - \sqrt{2}} = \frac{(\sqrt{3} - \sqrt{2})^2}{3 - 2} = 3 - 2\sqrt{3}\sqrt{2} + 2 = 5 - 2\sqrt{6}$

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Complete the following, show your work and simplify your answer:

- $A = \{x|x \text{ is an even positive integer, } 6 \leq x < 20\}$ and
 $B = \{x|x \text{ is a composite number } \leq 17\}$, then find $A \cap B = \dots\dots\dots$

Ans : $A = \{6, 8, 10, 12, 14, 16, 18\}$; $B = \{4, 6, 8, 9, 10, 12, 14, 15, 16\}$;

$$A \cap B = \{6, 8, 10, 12, 14, 16\}$$

- $-2 < x < 1$, then $\left| \frac{x+2}{|x-1|+|x+4|} \right| = \dots\dots\dots$

Ans : $= \left| \frac{x+2}{1-x+x+4} \right| = \left| \frac{x+2}{5} \right| = \frac{x+2}{5}$

- In the product $(3-2x)(2x^2-5x+1)(3+2x)$ the leading coefficient is $\dots\dots\dots$ and the degree is $\dots\dots\dots$

Ans : $= (9-4x^2)(2x^2-5x+1)$, so the leading coefficient $= (-4)(2) = -8$ and the degree $= 4$

- In the set $= \left\{ -\frac{8\sqrt{27}}{\sqrt{12}}, \frac{4}{0}, \frac{\pi}{\pi+2}, -41.123456789, 0.232332333\dots\dots \right\}$

the rational number(s) is (are) $\dots\dots\dots$

Ans : $-\frac{8\sqrt{27}}{\sqrt{12}} = -\frac{8(3)\sqrt{3}}{2\sqrt{3}} = -12$ and -41.123456789 (terminating decimal)

are the rational numbers.

- When rationalized, the expression $\frac{\sqrt[5]{2}}{\sqrt[5]{9xy^3}} = \dots\dots\dots$

Ans : $= \frac{\sqrt[5]{2}}{\sqrt[5]{3^2xy^3}} \cdot \frac{\sqrt[5]{3^3x^4y^2}}{\sqrt[5]{3^3x^4y^2}} = \frac{\sqrt[5]{54x^4y^2}}{3xy}$

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Complete the following, show your work and simplify your answer:

- In the set $\{8.112233\dots, \frac{\sqrt{9}}{\sqrt{21}}, \frac{\pi^2}{\pi^2+1}, -\sqrt{-16}, 14.235235235\dots, \frac{7}{22}\}$,

the **irrational** number(s) is (are)

Ans : $\frac{\sqrt{9}}{\sqrt{21}} = \frac{3}{\sqrt{21}}, \frac{\pi^2}{\pi^2+1}, 8.112233\dots$ (non-terminating, non-repeating decimal)

are the irrational numbers.

- If $-2 < x < 0$, then $|-x-2| + |x-1| - \frac{|x|}{x} = \dots\dots\dots$

Ans : $= -(-x-2) - (x-1) - \left(\frac{-x}{x}\right) = x+2-x+1+1 = 4$

- If $P(x)$ and $Q(x)$ are two polynomials both of degree 6, then the degree of $P(x) - Q(x)$ is
- and the degree of $P(x) \cdot Q(x)$ is

Ans : The degree of $P(x) - Q(x) \leq 6$ and the degree of $P(x) \cdot Q(x) = (6)(6) = 12$

- $(3-2x)^3 - 2(2-3x)(2+3x) = \dots\dots\dots$

Ans : $= 27 - 3(9)(2x) + 3(3)(4x^2) - 8x^3 - 2(4 - 9x^2) = 27 - 54x + 36x^2 - 8x^3 - 8 + 18x^2$
 $= -8x^3 + 54x^2 - 54x + 19$

- When rationalized, the expression $\frac{\sqrt{x}}{\sqrt[3]{x^2}} = \dots\dots\dots$

Ans : $= \frac{\sqrt{x}}{\sqrt[3]{x^2}} \cdot \frac{\sqrt[3]{x}}{\sqrt[3]{x}} = \frac{x^{\frac{1}{2}} x^{\frac{1}{3}}}{x} = \frac{x^{\frac{5}{6}}}{x} = \frac{\sqrt[6]{x^5}}{x}$