Solution of Recitation - 1.1 and 1.2

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Q1) (a)
$$\frac{2x-3}{3} - \frac{x-1}{2} = 3 - \frac{x-1}{6} \xrightarrow{\text{multiply}}{\text{by } 6} 2(2x-3) - 3(x-1) = 18 - (x-1) \implies 4x - 6 - 3x + 3$$

= $18 - x + 1 \implies x - 3 = -x + 19 \implies 2x = 22 \implies x = 11.$

The equation has one solution, so it is a conditional equation.

(b) $x^2 - 2x + 1 = (x - 1)^2 \implies x^2 - 2x + 1 = x^2 - 2x + 1$ which is always true (the two sides are identical). This means that the equation is an identity. Moreover S.S. = \Re

(c) $\frac{4x+8}{4} = x+5 \implies \frac{4x}{4} + \frac{8}{4} = x+5 \implies x+2 = x+5 \implies 2=5$ which is never true, so

the equation is a contradiction and S.S. $= \phi$.

Q2) (a)
$$S = 2\pi (r_1 + r_2)h \implies S = 2\pi hr_1 + 2\pi hr_2 \implies S - 2\pi hr_2 = 2\pi hr_1 \implies r_1 = \frac{S - 2\pi hr_2}{2\pi h}$$

(b) $y = \frac{a+x}{3-ax} \implies a+x = 3y - ayx \implies x + ayx = 3y - a \implies (1+ay)x = 3y - a \implies x = \frac{3y-a}{1+ay}$

Q3) Let the two consecutive odd integers (عدران فردیان متتالیان) be x and x + 2. Therefore $(x + 2)^2 - x^2 = 40 \implies x^2 + 4x + 4 - x^2 = 40 \implies 4x = 36 \implies x = 9$. So the two consecutive odd integers are 9 and 11.

- Q4) Let L = length and W = width, where L = W + 6. The perimeter = 60 = 2(L + W) $\implies 30 = L + W = (W + 6) + W = 2W + 6 \implies 24 = 2W \implies W = 12 \text{ cm}$ and L = W + 6 = 12 + 6 = 18 cm.
- Q5) The equation 2[5(x-3)+m] = (m+4)x 18 is an **identity**. This means that the two sides are **identical**. Thus $10(x-3) + 2m \equiv mx + 4x 18 \implies 10x + (2m-30) \equiv (m+4)x 18$ $\implies 10 = m+4$ and $2m-30 = -18 \implies m=6$ and $2m = 12 \implies m=6$.