Chapter 3: Polynomial and Rational Functions

Section 3.1 The Remainder Theorem and the Factor Theorem

Division of Polynomials

Use long division to divide.

1. $\left(-6x^2+4x^3-14-6x\right)\div(2x-5)$

(a) $2x^2+2x+3+\dfrac{1}{2x-5}$

(b) $2x^2+2x+2-\dfrac{4}{2x-5}$

(c) $2x^2-2x-3+\dfrac{1}{2x-5}$

(d) $2x^2-2x-2-\dfrac{4}{2x-5}$

2. $\left(-3x^3+2x+3\right)\div(x+3)$

(a) $-3x^2+11x-30+\dfrac{90}{x+3}$

(b) $-3x^2+9x+29-\dfrac{82}{x+3}$

(c) $-3x^2+9x-25+\dfrac{78}{x+3}$

(d) $-3x^2+11x+33-\dfrac{96}{x+3}$

3. $-3x^4-3x^3-8x^2-9x$ by x^2+3

(a) $-3x^2+3x-2+\dfrac{1}{x^2+3}$

(b) $-3x^2-3x-1+\dfrac{3}{x^2+3}$

(c) $-3x^2+3x-\dfrac{1}{x^2+3}$

(d) $-3x^2-3x+1-\dfrac{3}{x^2+3}$

4. $\dfrac{3x^3+5x^2-4x-7}{-x^2-3x-1}$

(a) $-3x^2+4x+\dfrac{5x-3}{-x^2-3x-1}$

(b) $4x-3+\dfrac{5x-3}{-x^2-3x-1}$

(c) $-3x+4+\dfrac{5x-3}{-x^2-3x-1}$

(d) $4x^2-3x+\dfrac{5x-3}{-x^2-3x-1}$

The Remainder Theorem

5. Use synthetic division to find $P\left(-\dfrac{1}{6}\right)$ if $P(x)=2x^4-2x^2-7$.

(a) $-\dfrac{67}{36}$ (b) $\dfrac{-571}{1296}$ (c) $\dfrac{-131}{36}$ (d) $\dfrac{-4571}{648}$

Use synthetic division to find the function value.

6. $g(x)=x^6+4x^5+9x^3-6x^2+24,\ g(-5)$ (a) 1818 (b) 1850 (c) 1930 (d) 1874

7. $f(x)=-8x^4+6x^2-6,\ f(2)$ (a) –106 (b) –109 (c) –105 (d) –110

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8. For $\left(x^3+4x^2+kx-1\right)\div(x-5)$, find the value of k if the remainder is 214.

(a) –2 (b) 4 (c) –1 (d) 1

The Factor Theorem

9. Use synthetic division to determine which of the following polynomials is *not* a factor of x^3+2x^2-5x-6.

(a) $x+2$ (b) $x+1$ (c) $x+3$ (d) $x-2$

10. Use synthetic division to determine which of the following is *not* a zero of the polynomial equation.
$3x^4-23x^3+25x^2+71x+20=0$

(a) 4 (b) –1 (c) –4 (d) 5

11. Use the Factor Theorem to determine which of the following is *not* a factor of $f(x)=3x^4-5x^3-59x^2+41x+20$.

(a) $x-5$ (b) $3x+1$ (c) $x+5$ (d) $x+4$

12. Use the Factor Theorem to determine how many of the following polynomials are factors of
$3x^4-11x^3-55x^2+163x+60$.
$x-5,\ x+3,\ x-3,\ 3x-2,\ x-4,\ x+4,\ x+5$

(a) 4 (b) 1 (c) 2 (d) 3

Reduced Polynomials

Use synthetic division to complete the indicated factorization.

13. $x^3-21x^2+400=(x-20)(\quad)$ (a) x^2+x+20 (b) x^2-x-20 (c) x^2-19 (d) x^2-x-19

14. $x^4-x^3-22x^2+16x+96=(x-4)(\quad)$

(a) $x^3+3x^2-10x-24$ (b) $x^3+3x^2-11x-24$ (c) $x^3+4x^2-11x-24$ (d) $x^3-3x^2+10x-24$

15. $x^4+3x^3-91x^2-123x+1890=(x-5)(\quad)$

(a) $x^3+8x^2+51x-378$ (b) $x^3-2x^2-51x-378$ (c) $x^3-2x^2+51x-378$ (d) $x^3+8x^2-51x-378$

16. $x^4+4x^3-7x^2-22x+24=(x+4)(x+3)(\quad)$

(a) x^2-3x+2 (b) x^2-3x+1 (c) x^2+3x-2 (d) x^2-2x+1

Section 3.2 Polynomial Functions of Higher Degree

Far-Left and Far-Right Behavior

17. Determine the right-hand and left-hand behavior of the graph of the function.

$$f(x)=\frac{2x^2-3+9x^4}{7}$$

(a) Rises to the left
Rises to the right

(b) Rises to the left
Falls to the right

(c) Falls to the left
Falls to the right

(d) Falls to the left
Rises to the right

(e) None of these

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Examine the leading term and determine the far-left and far-right behavior of the graph of the polynomial function.

18. $N(x) = 2 + 9x^2 - 7x^3$

(a) $a_n = 2$ and $n = 3$
The graph of N goes up to the far left and up to the far right.

(b) $a_n = -7$ and $n = 3$
The graph of N goes down to the far left and up to the far right.

(c) $a_n = -7$ and $n = 3$
The graph of N goes up to the far left and down to the far right.

(d) $a_n = 9$ and $n = 3$
The graph of N goes down to the far left and down to the far right.

19. $P(x) = -\frac{1}{7}(x-6)^4$

(a) $a_n = \frac{3}{2}$ and $n = 5$
The graph of P goes up to the far left and up to the far right.

(b) $a_n = -\frac{1}{7}$ and $n = 4$
The graph of P goes down to the far left and down to the far right.

(c) $a_n = -\frac{1}{7}$ and $n = 5$
The graph of P goes down to the far left and up to the far right.

(d) $a_n = \frac{3}{2}$ and $n = 4$
The graph of P goes up to the far left and down to the far right.

20. $S(x) = -4x^6 + 7x^5 + 11$

(a) The graph of S goes up to the far left and down to the far right.

(b) The graph of S goes down to the far left and down to the far right.

(c) The graph of S goes down to the far left and up to the far right.

(d) The graph of S goes up to the far left and up to the far right.

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Maximum and Minimum Values

Find all relative extrema of the function.

21. $f(x) = x^4 - 2x^3$

(a) relative maximum: $\left(\frac{3}{2}, -\frac{27}{16}\right)$
relative minimum: none

(b) relative maximum: $\left(-\frac{3}{2}, \frac{27}{16}\right)$
relative minimum: $(0, 0)$

(c) relative maximum: none
relative minimum: $\left(\frac{3}{2}, -\frac{27}{16}\right)$

(d) The function has no relative extrema.

22. $f(x) = 64x + \frac{16}{x}$

(a) Relative minimum: $\left(-\frac{1}{2}, -64\right)$
Relative maximum: $\left(\frac{1}{2}, 64\right)$

(b) Relative maximum: $\left(-\frac{1}{2}, -64\right)$
Relative minimum: $\left(\frac{1}{2}, 64\right)$

(c) Relative minimum: $(-1, -80)$
Relative maximum: $(1, 80)$

(d) Relative maximum: $(-1, -80)$
Relative minimum: $(1, 80)$

23. $f(x) = \frac{1}{x^2 + 6x + 13}$

(a) relative minimum: $\left(-3, \frac{1}{4}\right)$

(b) relative maximum: $\left(3, \frac{1}{4}\right)$

(c) relative minimum: $\left(-3, -\frac{1}{4}\right)$

(d) relative maximum: $\left(-3, \frac{1}{4}\right)$

24. A drug that stimulates reproduction is introduced into a colony of bacteria. After *t* minutes, the number of bacteria is given approximately by
$N(t) = 1500 + 27t^2 - t^3,\ 0 \le t \le 50$
At which value of *t* is the rate of growth maximum?

(a) 36 min (b) 18 min (c) 27 min (d) 9 min

Real Zeros of a Polynomial Function

Find all real zeros of the function.

25. $f(x) = -7x^4 + 112x^2$

(a) $x = 0,\ x = \pm 16$ (b) $x = 0,\ x = 4$ (c) $x = 0,\ x = \pm 4$ (d) $x = 0,\ x = 16$ (e) None of these

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Find all real zeros of the function.

26. $f(x) = x^3 - 9x^2 + 23x - 15$

(a) $x = 1,\ x = -3,\ x = -5$ (b) $x = 1,\ x = 3,\ x = 5$ (c) $x = -1,\ x = -3,\ x = -5$

(d) $x = -1,\ x = 3,\ x = -5$ (e) None of these

27. $f(x) = x^4 - 11x^2 + 10$

(a) $x = \pm 1,\ x = \pm 10$ (b) $x = \pm 1,\ x = \pm\sqrt{10}$ (c) $x = 1,\ x = 10$

(d) $x = 1,\ x = \sqrt{10}$ (e) None of these

28. Use the Zero Location Theorem to determine whether the given polynomial has a zero between 0 and 2.
$P(y) = y^2 - 6y + 3$

(a) $P(y)$ does not have a zero between 0 and 2. (b) $P(y)$ has a zero at 0.

(c) $P(y)$ has a zero at 2. (d) $P(y)$ has a zero between 0 and 2.

Even and Odd Powers of (x - c) Theorem

Use the Even and Odd Powers of $(x - c)$ Theorem to determine where the graph of the given polynomial will cross the x-axis and where the graph will intersect but not cross the x-axis.

29. $y = (x+7)(x+5)(x+1)^2(x-4)$

(a) The graph of y will cross the x-axis at the x-intercepts $(-1,\ 0)$ and $(-7,\ 0)$.
The graph of y will intersect but not cross the x-axis at $(-5,\ 0)$ and $(4,\ 0)$.

(b) The graph of y will cross the x-axis at the x-intercepts $(-7,\ 0)$, $(-5,\ 0)$, and $(4,\ 0)$.
The graph of y will intersect but not cross the x-axis at $(-1,\ 0)$.

(c) The graph of y will cross the x-axis at the x-intercept $(-1,\ 0)$.
The graph of y will intersect but not cross the x-axis at $(-7,\ 0)$, $(-5,\ 0)$, and $(4,\ 0)$.

(d) The graph of y will cross the x-axis at the x-intercepts $(-7,\ 0)$ and $(-5,\ 0)$.
The graph of y will intersect but not cross the x-axis at $(-1,\ 0)$ and $(4,\ 0)$.

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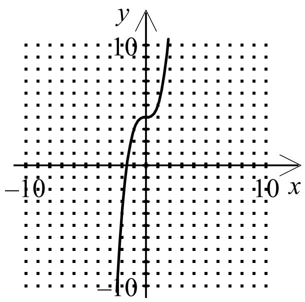
A Procedure for Graphing Polynomial Functions

Identify the graph of the function.

33. $f(x) = -x^3 + 4$

(a)



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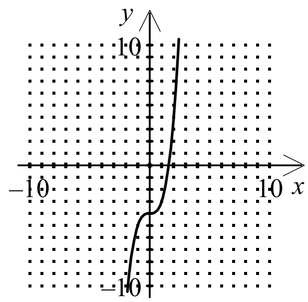

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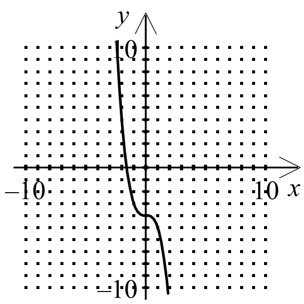

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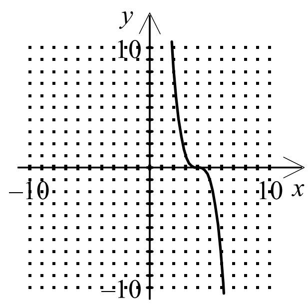
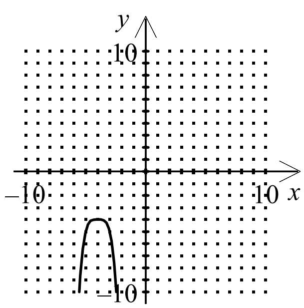


(e) None of these

34. $f(x) = (x+4)^4 + 4$

(a)



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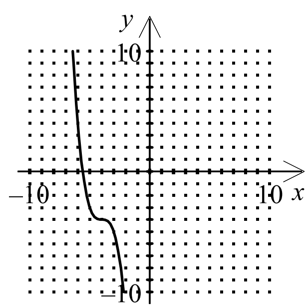
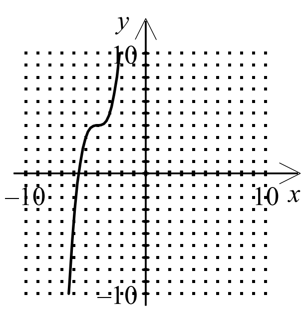
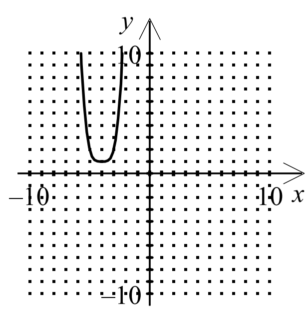


(c)



(d)



(e) None of these

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List the zeros of the cubic function and tell which, if any, are double or triple zeros.

39. $y=(3x+1)^3$ (a) 3 (triple) (b) $\frac{1}{3}$ (triple) (c) -3 (triple) (d) $-\frac{1}{3}$ (triple)

40. Find the roots of the polynomial equation, and state the multiplicity of each root.
$P(x)=-\frac{1}{4}(x+4)(x-4)(4x+1)$

(a) $4,\ -4,$ and $\frac{1}{4}$ are roots each of multiplicity 1.
(b) $-4,\ 4,$ and $-\frac{1}{4}$ are roots each of multiplicity 1.
(c) –4 and 4 are roots each of multiplicity 1.
$-\frac{1}{4}$ is a root of multiplicity 2.
(d) none of these

The Rational Zero Theorem

Use the Rational Zero Theorem to find all possible rational zeros of the polynomial.

41. $f(x)=-6x^4+6x^3-2x^2+3x-77$

(a) $\pm1,\ \pm7,\ \pm11,\ \pm77,\ \pm\frac{7}{3},\ \pm\frac{11}{3},\ \pm\frac{77}{3},\ \pm\frac{1}{6},\ \pm\frac{7}{6},\ \pm\frac{11}{6},\ \pm\frac{77}{6}$

(b) $\pm1,\ \pm7,\ \frac{7}{2},\ \pm\frac{11}{2},\ \pm\frac{7}{3},\ \pm\frac{11}{3}$

(c) $\pm1,\ \pm7,\ \pm11,\ \pm77,\ \pm\frac{1}{2},\ \pm\frac{7}{2},\ \pm\frac{11}{2},\ \pm\frac{77}{2},\ \pm\frac{1}{3},\ \pm\frac{7}{3},\ \pm\frac{11}{3},\ \pm\frac{77}{3},\ \pm\frac{1}{6},\ \pm\frac{7}{6},\ \pm\frac{11}{6},\ \pm\frac{77}{6}$

(d) $\pm\frac{7}{2},\ \pm\frac{11}{2},\ \pm\frac{77}{2},\ \pm\frac{1}{3},\ \pm\frac{7}{3},\ \pm\frac{11}{3},\ \pm\frac{77}{6}$

42. $g(x)=-15x^3-5x^2-x-1$

(a) $\pm1,\ \pm\frac{1}{4},\ \pm\frac{1}{6},\ \pm\frac{1}{15}$
(b) $\pm1,\ \pm\frac{1}{3},\ \pm\frac{1}{5},\ \pm\frac{1}{15}$
(c) $\pm1,\ -\frac{1}{3},\ -\frac{1}{5},\ \pm\frac{1}{17}$
(d) $-2,\ -\frac{1}{3},\ \pm\frac{1}{7},\ -\frac{1}{15}$

Use the Rational Zero Theorem to determine all possible rational zeros of f.

43. $f(x)=2x^3+6x^2+5x+8$

(a) $\pm\frac{1}{2},\ \pm2,\ \pm4,\ \pm8,\ \pm16$
(b) $\pm\frac{1}{2},\ \pm1,\ \pm2,\ \pm4,\ \pm8$
(c) $\pm\frac{1}{2},\ \pm2,\ \pm4,\ \pm8$
(d) $0,\ \pm\frac{1}{2},\ \pm1,\ \pm2,\ \pm4$

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52. Use Descartes's Rule of Signs to determine the possible number of positive and negative zeros of the function.
$f(x) = x^6 - 4x^5 - x^4 + 2x^3 + 5x^2 + x + 3$

(a) Four, two, or no positive zeros
Two or no negative zeros

(b) Two or no positive zeros
Five, three, or one negative zeros

(c) Two or no positive zeros
Four, two, or no negative zeros

(d) Three or one positive zeros
Four, two, or no negative zeros

Zeros of a Polynomial Function

Find all the zeros of the function.

53. $x^3 + 5x^2 + x - 10$

(a) $-2, \dfrac{-3+\sqrt{29}}{2}, \dfrac{-3-\sqrt{29}}{2}$

(b) $-3+\sqrt{29}, -3-\sqrt{29}$

(c) $-2, \dfrac{2+\sqrt{27}}{2}, \dfrac{2-\sqrt{27}}{2}$

(d) none of these

54. $f(x) = 6x^4 - 13x^3 + 13x - 6$

(a) $-1, 1, -\frac{3}{2}, \frac{3}{2}$ (b) $-1, 1, -\frac{3}{2}, -\frac{2}{3}$ (c) $-1, 1, -3, -\frac{3}{2}$ (d) $-1, 1, \frac{2}{3}, \frac{3}{2}$

55. $p(x) = x^3 - 4x^2 - 15x + 18$ (a) –3, 1, and 6 (b) 3, 1, and 6 (c) –3, 1, and –6 (d) 3, 1, and –6

56. $y = 4x^4 - 4x^3 - 224x^2$ (a) 0, 4, 8 (b) –7, 8 (c) 0, 8 (d) –7, 0, 8

Applications of Polynomial Functions

57. A cubic model for the yearly worldwide carbon emissions is
$W = -0.051x^3 + 2.93x^2 + 74.6x + 1589$
where W is the weight of the emissions in millions of tons and x is the number of years since 1950. Use synthetic division to evaluate the model for the year 1960.

(a) 2029 million tons (b) 2835 million tons (c) 2679 million tons (d) 2577 million tons

58. A cubic model for the weight of an alligator is
$W = 0.001l^3 - 0.22l^2 + 17.4l - 426$
where W is the weight of the alligator in pounds and l is the length in inches. Use synthetic division to evaluate the model for an alligator 72 inches long.

(a) 46 lb (b) 66 lb (c) 60 lb (d) 54 lb

59. A cubic model for the increase in population of a certain town is
$P = -0.003x^3 + 6.8x^2 - 79x + 4972$
where x is the number of years since 1950. Use synthetic division to evaluate the population in 2050.

(a) 74,569 (b) 50,755 (c) 62,072 (d) 71,976

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Identify the polynomial written as a product of linear factors.

68. $f(x) = x^2 + 36$

(a) $f(x) = (-x + 6i)(x - 6i)$ (b) $f(x) = (x + 6i)(x - 6i)$ (c) $f(x) = (x + 6i)^2$

(d) $f(x) = (x - i)(x + 36i)$ (e) None of these

The Conjugate Pair Theorem

69. Solve $z^3 - 5z^2 + 4z + 10$ given that $3 + i$ is a root.

(a) $-1, 3 + i, 3 - i$ (b) $7, 2 + i, 2 - i$ (c) $-7, 2 + i, 2 - i$ (d) $1, 3 + i, -3 - i$

Use the given zero of *f* to find all the zeros of *f*.

70. $f(x) = x^3 + 5x^2 + 11x + 15,\ -1 + 2i$ (a) $-1 \pm 2i,\ -3$ (b) $-1 - 2i,\ 4$ (c) $1 \pm 2i,\ -3$ (d) $1 + 2i,\ 4$

71. $f(x) = x^4 - 4x^3 + 6x^2 + 4x - 7,\ 2 + \sqrt{3}i$

(a) $2,\ -2,\ -2 + \sqrt{3}i,\ -2 - \sqrt{3}i$ (b) $-3,\ 3,\ 2 + \sqrt{3}i,\ 2 - \sqrt{3}i$

(c) $1,\ -1,\ 2 + \sqrt{3}i,\ 2 - \sqrt{3}i$ (d) $1,\ -1,\ -2 + \sqrt{3}i,\ -2 - \sqrt{3}i$

72. $f(x) = x^4 + 2x^3 - 2x^2 - 8x - 8,\ -1 + i$

(a) $-3,\ 3,\ -1 + i,\ -1 - i$ (b) $2,\ -2,\ -1 + i,\ -1 - i$ (c) $-1,\ 1,\ 1 + i,\ 1 - i$ (d) $2,\ -2,\ 1 + i,\ 1 - i$

Find a Polynomial Function with Given Zeros

Find a polynomial with integer coefficients that has the given zeros.

73. $2,\ 3 + i$

(a) $P(x) = x^3 + 8x^2 + 22x + 20$ (b) $P(x) = x^3 - 8x^2 + 22x - 20$

(c) $P(x) = x^3 - 8x^2 - 2x - 20$ (d) $P(x) = x^3 - 4x^2 - 2x + 20$

74. $1,\ -4 + i,\ -4 - i$

(a) $f(x) = x^3 + 7x^2 + 9x - 17$ (b) $f(x) = x^3 - 7x^2 + 9x + 17$

(c) $f(x) = x^3 + 7x^2 + 25x - 17$ (d) $f(x) = x^3 + 9x^2 + 25x + 17$

75. $2,\ 3i,\ -3i,\ 4i,\ -4i$

(a) $f(x) = x^5 + 2x^4 + 50x^2 - 144x + 288$ (b) $f(x) = x^5 - 2x^4 + 25x^3 - 50x^2 + 144x - 288$

(c) $f(x) = x^5 - 2x^4 - 7x^3 - 12x + 288$ (d) $f(x) = x^5 - 7x^4 - 12x^3 - 50x^2 - 144x - 288$

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Which shows the true statement for the graph of the rational function *g*?

82. $g(x) = \dfrac{x}{x^2 + 3x - 4}$

(a) The graph of *g* is positive for all *x* such that $x < -4$.

(b) The graph of *g* is negative for all *x* such that $-4 < x < 0$.

(c) The graph of *g* is positive for all *x* such that $0 < x < 1$.

(d) The graph of *g* is negative for all *x* such that $x < -4$.

83. $g(x) = \dfrac{x - 1}{x^2 - 2x - 8}$

(a) The graph of *g* is positive for all *x* such that $x < -2$.

(b) The graph of *g* is negative for all *x* such that $x > 4$.

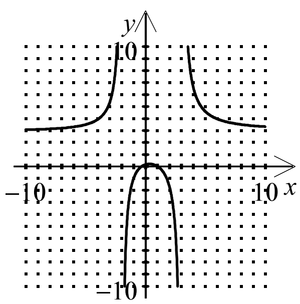
(c) The graph of *g* is positive for all *x* such that $-2 < x < 1$.

(d) The graph of *g* is positive for all *x* such that $1 < x < 4$.

84. Identify the graph of the rational function. Find any vertical and horizontal asymptotes.

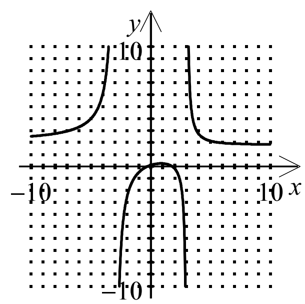
$f(x) = \dfrac{3x^2 - 4x + 1}{x^2 + x - 6}$

(a)



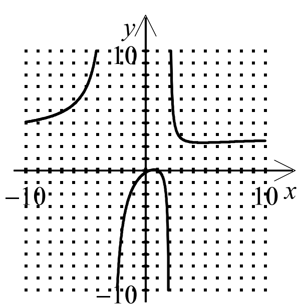
Asymptotes: $x = -2$, $x = 3$, $y = 3$

(b)



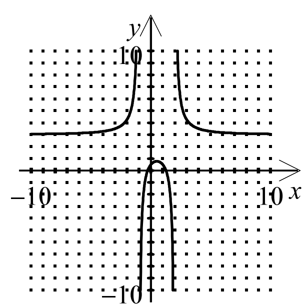
Asymptotes: $x = -3$, $x = -3$, $y = 2$

(c)



Asymptotes: $x = -3$, $x = 2$, $y = 3$

(d)



Asymptotes: $x = -1$, $x = 2$, $y = 3$

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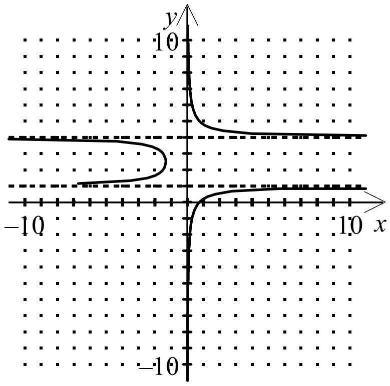
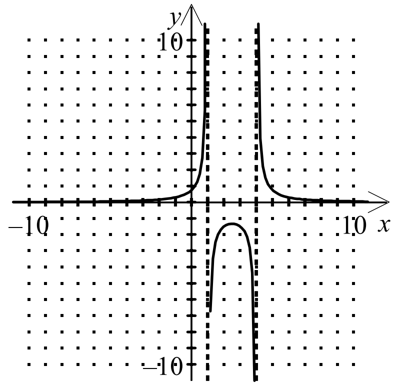
87. Graph: $y = \dfrac{3}{(x-4)(x-1)}$

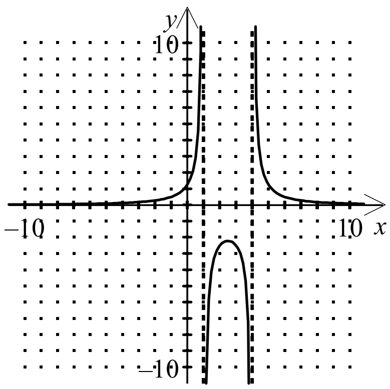
(a)



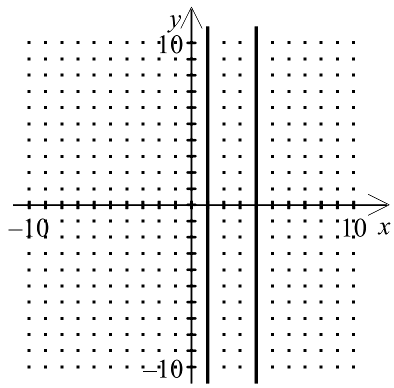
(b)



(c)



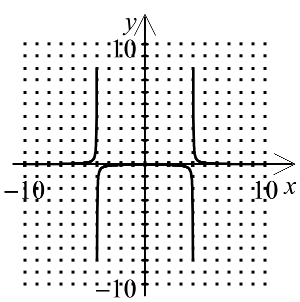
(d)



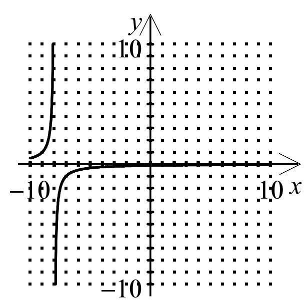
88. Graph:

$f(x) = \dfrac{x^2}{x^2 - 16}$

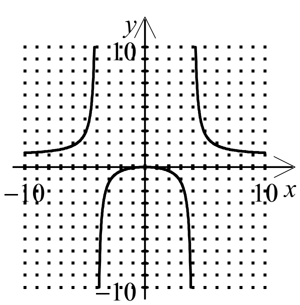
(a)



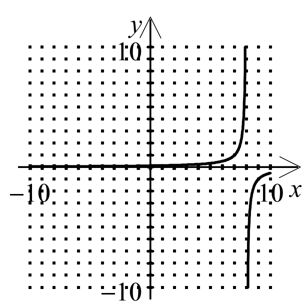
(b)



(c)



(d)



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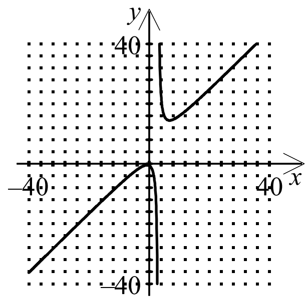
Identify the graph of the rational function and find the equation of the slant asymptote.

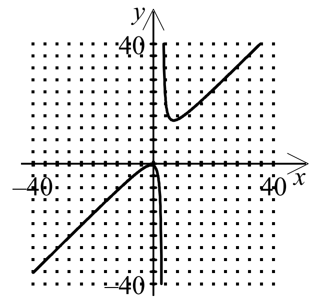
92. $f(x) = \dfrac{-x^2 - x - 2}{x - 3}$

(a)



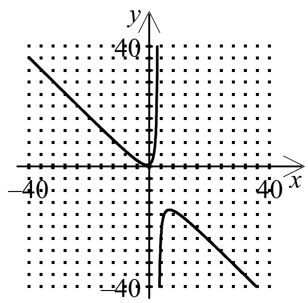
Slant asymptote: $y = x + 4$

(b)



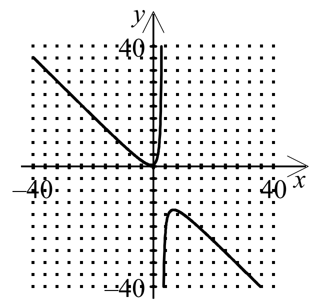
Slant asymptote: $y = -x - 4$

(c)



Slant asymptote: $y = x + 4$

(d)



Slant asymptote: $y = -x - 4$

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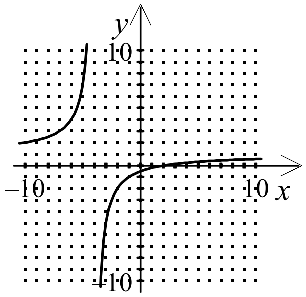
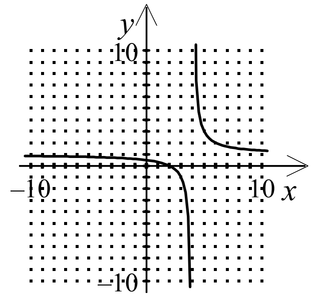
Graph:

95. $f(x) = \dfrac{x^2 + 4x - 12}{x^2 + 2x - 24}$

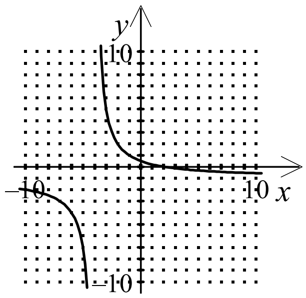
(a)



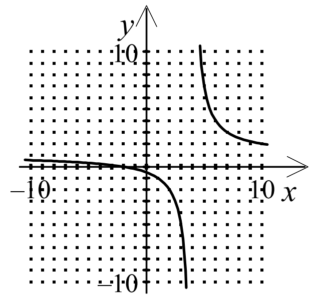
(b)



(c)

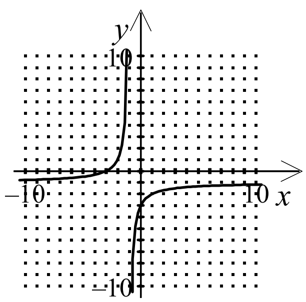


(d)

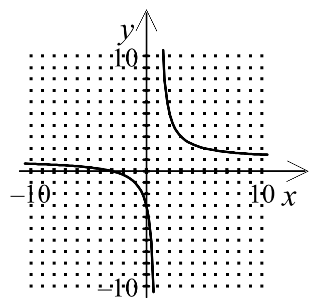


96. $f(x) = \dfrac{x^2 + 8x + 15}{x^2 + 4x - 5}$

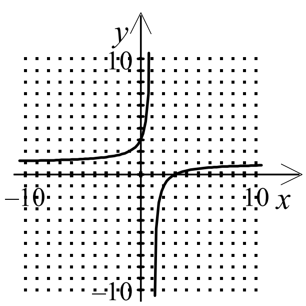
(a)



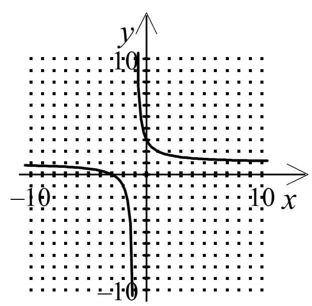
(b)



(c)



(d)



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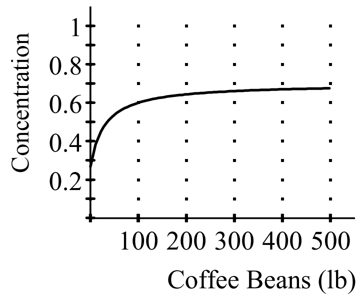
100. Calypso Coffee mixes 50 pounds of a standard coffee containing 10% Columbian coffee beans with x pounds of a premium coffee containing 60% Columbian coffee beans. The concentration of Columbian coffee beans in the final mix is given by

$$C = \frac{6x + 50}{10(x + 50)}.$$

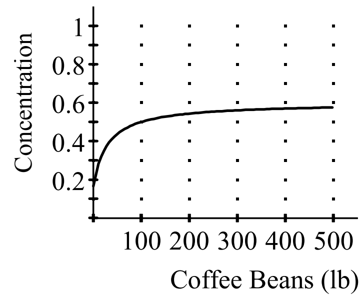
Identify the graph of the concentration function and find the concentration of Columbian coffee beans the graph approaches as x increases.

(a)



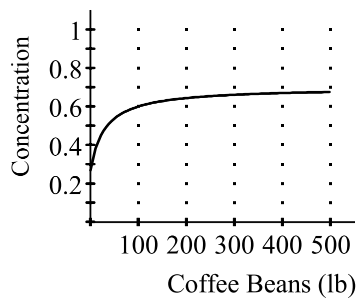
The concentration approaches 70%.

(b)



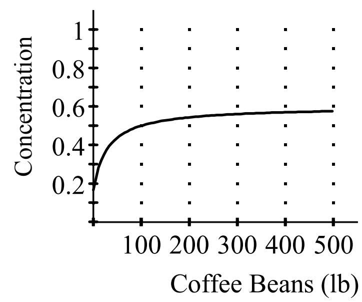
The concentration approaches 35%.

(c)



The concentration approaches 60%.

(d)



The concentration approaches 60%.

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Chapter 3: Polynomial and Rational Functions (Answer Key)

Section 3.1 The Remainder Theorem and the Factor Theorem

Division of Polynomials

[1] (b)

[2] (c)

[3] (d)

[4] (c)

The Remainder Theorem

[5] (d)

[6] (d)

[7] (d)

[8] (a)

The Factor Theorem

[9] (a)

[10] (c)

[11] (c)

[12] (d)

Reduced Polynomials

[13] (b)

[14] (a)

[15] (d)

[16] (a)

Section 3.2 Polynomial Functions of Higher Degree

Far-Left and Far-Right Behavior

[17] (a)

[18] (c)

[19] (b)

[20] (b)

Maximum and Minimum Values

[21] (c)

[22] (b)

[23] (d)

[24] (b)

Real Zeros of a Polynomial Function

[25] (c)

[26] (b)

[27] (b)

[28] (d)

Even and Odd Powers of (x - c) Theorem

[29] (b)

[30] (a)

[31] (d)

[32] (b)

A Procedure for Graphing Polynomial Functions

[33] (e)

[34] (e)

[35] (e)

[36] (b)

Section 3.3 Zeros of Polynomial Functions

Multiple Zeros of a Polynomial Function

[37] (b)

[38] (c)

[39] (d)

[40] (b)

The Rational Zero Theorem

[41] (c)

[42] (b)

[43] (b)

[44] (a)

Upper and Lower Bounds for Real Zeros

[45] (a)

[46] (b)

[47] (a)

[48] (a)

Descartes' Rule of Signs

[49] (d)

[50] (d)

[51] (b)

[52] (c)

Zeros of a Polynomial Function

[53] (a)

[54] (d)

[55] (a)

[56] (d)

Applications of Polynomial Functions

[57] (d)

[58] (c)

[59] (c)

[60] (a)

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