6. 
$$\log_b(x\sqrt[3]{y}) = \log_b x + \log_b y^{1/3}$$
  
=  $\log_b x + \frac{1}{3}\log_b y$ 

12. 
$$\frac{1}{2}\log_8(x+5) - 3\log_8 y = \log_8(x+5)^{1/2} - \log_8 y^3 = \log_8 \sqrt{x+5} - \log_8 y^3 = \log_8 \frac{\sqrt{x+5}}{y^3}$$

- 26.  $t(x) = \log_9(5-x) = \frac{\log(5-x)}{\log 9}$
- 34. False.  $\log 10 \cdot \log 10 = 1 \cdot 1 = 1$ but  $\log 10 + \log 10 = 1 + 1 = 2$
- 36. False.  $\log \frac{100}{10} = \log 10 = 1$ but  $\frac{\log 100}{\log 10} = \frac{2}{1} = 2$

**39.** False. 
$$(\log 10)^2 = 1^2 = 1$$
 but  $2\log 10 = 2(1) = 2$ 

42.  

$$\log_{5} 20 \cdot \log_{20} 60 \cdot \log_{60} 100 \cdot \log_{100} 125 = \frac{\log 20}{\log 5} \cdot \frac{\log 60}{\log 20} \cdot \frac{\log 100}{\log 60} \cdot \frac{\log 125}{\log 100}$$

$$= \frac{\overline{\log 20}}{\log 5} \cdot \frac{\underline{\log 60}}{\overline{\log 20}} \cdot \frac{\overline{\log 400}}{\underline{\log 60}} \cdot \frac{\underline{\log 125}}{\overline{\log 400}} = \frac{\log 125}{\log 5} = \frac{\log 5^{3}}{\log 5}$$

$$= \frac{3 \log 5}{\log 5} = \frac{3 \log 5}{\overline{\log 5}} = 3$$

44. 
$$\ln\left(\frac{1}{50^{300}}\right) = \ln 50^{-300} = -300 \ln 50 \approx -1174$$
$$\ln\left(\frac{1}{151^{233}}\right) = \ln 151^{-233} = -233 \ln 151 \approx -1169$$
$$\frac{1}{50^{300}} \text{ is smaller.}$$