

$$\begin{aligned} 6. \quad \sqrt{25} + \sqrt{-9} &= 5 + i\sqrt{9} \\ &= 5 + 3i \end{aligned}$$

$$\begin{aligned} 14. \quad (3-5i) - (8-2i) &= 3-5i-8+2i \\ &= (3-8) + (-5i+2i) \\ &= -5-3i \end{aligned}$$

$$\begin{aligned} 30. \quad (-5-i)(2+3i) &= -5(2+3i) - i(2+3i) \\ &= -10-15i-2i-3i^2 \\ &= -10-15i-2i-3(-1) \\ &= -10-15i-2i+3 \\ &= (-10+3) + (-15i-2i) \\ &= -7-17i \end{aligned}$$

$$\begin{aligned} 36. \quad (5-3\sqrt{-48})(2-4\sqrt{-27}) &= (5-3i\sqrt{48})(2-4i\sqrt{27}) = [5-3i(4\sqrt{3})][2-4i(3\sqrt{3})] = (5-12i\sqrt{3})(2-12i\sqrt{3}) \\ &= 5(2-12i\sqrt{3}) - 12i\sqrt{3}(2-12i\sqrt{3}) = 10-60i\sqrt{3}-24i\sqrt{3}+144i^2(\sqrt{3})^2 \\ &= 10-60i\sqrt{3}-24i\sqrt{3}+144(-1)(3) = 10-60i\sqrt{3}-24i\sqrt{3}-432 \\ &= (10-432) + (-60i\sqrt{3}-24i\sqrt{3}) = -422-84i\sqrt{3} \end{aligned}$$

$$40. \quad \frac{4-8i}{4i} = \frac{4(1-2i)}{4i} = \frac{\cancel{4}(1-2i)}{\cancel{4}i} = \frac{1-2i}{i} = \frac{1-2i}{i} \cdot \frac{i}{i} = \frac{i-2i^2}{i^2} = \frac{i-2(-1)}{-1} = \frac{i+2}{-1} = -2-i$$

$$\begin{aligned} 45. \quad \frac{5-i}{4+5i} &= \frac{5-i}{4+5i} \cdot \frac{4-5i}{4-5i} = \frac{(5-i)(4-5i)}{(4+5i)(4-5i)} = \frac{5(4-5i)-i(4-5i)}{4(4-5i)+5i(4-5i)} = \frac{20-25i-4i+5i^2}{16-20i+20i-25i^2} \\ &= \frac{20-25i-4i+5(-1)}{16-25(-1)} = \frac{20-25i-4i-5}{16+25} = \frac{(20-5)+(-25i-4i)}{16+25} = \frac{15-29i}{41} = \frac{15}{41} - \frac{29}{41}i \end{aligned}$$

$$\begin{aligned} 54. \quad (2-i)^3 &= (2-i)(2-i)^2 \\ &= (2-i)[2^2+2(2)(-i)+(-i)^2] \\ &= (2-i)[4-4i+i^2] \\ &= (2-i)[4-4i-1] \\ &= (2-i)(3-4i) \\ &= 2(3-4i)-i(3-4i) \\ &= 6-8i-3i+4i^2 \\ &= 6-8i-3i+4(-1) \\ &= 6-8i-3i-4 \\ &= 2-11i \end{aligned}$$

62. Use the Powers of i Theorem.
The remainder of $52 \div 4$ is 0.

$$i^{-52} = \frac{1}{i^{52}} = \frac{1}{i^0} = \frac{1}{1} = 1$$

66. Use $a=2$, $b=1$, $c=3$.

$$\begin{aligned}\frac{-b + \sqrt{b^2 - 4ac}}{2a} &= \frac{-(1) + \sqrt{(1)^2 - 4(2)(3)}}{2(2)} \\ &= \frac{-1 + \sqrt{1 - 24}}{4} \\ &= \frac{-1 + \sqrt{-23}}{4} = \frac{-1 + i\sqrt{23}}{4} \\ &= -\frac{1}{4} + \frac{\sqrt{23}}{4}i\end{aligned}$$

80. $i + i^2 + i^3 + i^4 + \dots + i^{100} = 25(i + i^2 + i^3 + i^4) = 25(i + (-1) + (-i) + 1) = 25(0) = 0$