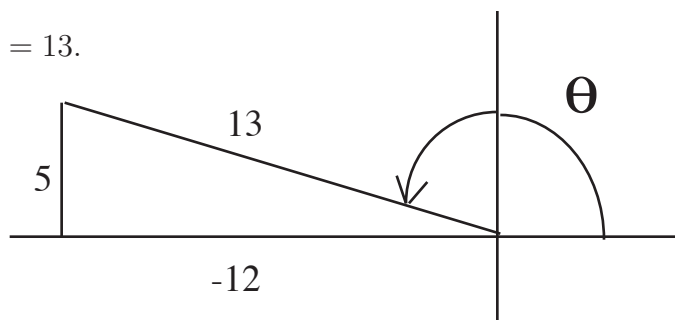


Math 002 – Term 052
Recitation hour (5.3 & 5.4)

Q1) If the terminal side of an angle θ passes through the point $(-12, 5)$, then find $\cot \theta + \csc \theta$.

Solution: $x = -12, y = 5 \implies r = \sqrt{x^2 + y^2} = \sqrt{144 + 25} = 13$.

So $\cot \theta = \frac{x}{y} = -\frac{12}{5}$, $\csc \theta = \frac{r}{y} = \frac{13}{5} \implies \cot \theta + \csc \theta = -\frac{12}{5} + \frac{13}{5} = \frac{1}{5}$.



Q2) a) Find the reference angle θ' for the angles: (i) -120° (ii) 8 radians

b) Find the exact value of $\tan 54^\circ + \tan 126^\circ + \tan 300^\circ$

Solution: a) (i) The smallest positive angle coterminal with -120° is $-120^\circ + 360^\circ = 240^\circ \in \text{Q III}$

$\implies \theta' = 240^\circ - 180^\circ = 60^\circ$

(ii) $\theta = 8$ radians $> 2\pi$, so the smallest positive angle coterminal with 8 radians is $8 - 2\pi \approx 8 - 6.28 = 1.72$

$\in \text{Q II} \implies \theta' = \pi - (8 - 2\pi) = 3\pi - 8 \approx 9.42 - 8 = 1.42$

b) Notice that $\theta = 126^\circ \in \text{Q II}$, so $\theta' = 180^\circ - 126^\circ = 54^\circ$. For $\alpha = 300^\circ \in \text{Q IV}$, $\alpha' = 360^\circ - 300^\circ = 60^\circ$.

Therefore $\tan 54^\circ + \tan 126^\circ + \tan 300^\circ = \tan 54^\circ + (-\tan 54^\circ) + (-\tan 60^\circ) = -\tan 60^\circ = -\sqrt{3}$

Q3) If W is the wrapping function, then find $W(-\frac{13\pi}{3})$.

Solution: $W(-\frac{13\pi}{3}) = (x, y) = \left(\cos(-\frac{13\pi}{3}), \sin(-\frac{13\pi}{3}) \right) = \left(\cos \frac{13\pi}{3}, -\sin \frac{13\pi}{3} \right)$

$= \left(\cos(4\pi + \frac{\pi}{3}), -\sin(4\pi + \frac{\pi}{3}) \right) = \left(\cos \frac{\pi}{3}, -\sin \frac{\pi}{3} \right) = \left(\frac{1}{2}, -\frac{\sqrt{3}}{2} \right)$

Q4) (a) Write $\cos t$ in terms of $\tan t$, $\pi < t < \frac{3\pi}{2}$.

(b) Determine whether the function $f(x) = x^3 \tan x$ is even, odd, or neither.

Solution: a) $\cos t = \frac{1}{\sec t} = \frac{1}{\pm \sqrt{1 + \tan^2 t}}$, but $t \in \text{Q III}$. So $\cos t = -\frac{1}{\sqrt{1 + \tan^2 t}}$

(b) $f(-x) = (-x)^3 \tan(-x) = (-x^3)(-\tan x) = x^3 \tan x = f(x) \implies f(x)$ is even.