

QUIZ # 3 (C) / A

Please show your work, no grade is given for choice without the details.

1) The sum of the solutions of the equation $\left| \frac{3x-2}{2} - \frac{2}{3} \right| = 1$ is

- A) $\frac{10}{9}$ B) $\frac{12}{9}$ C) 0 D) $\frac{7}{6}$ **E) $\frac{8}{9}$**

$$\frac{3x}{2} - \frac{2}{3} = \pm 1$$

LCD = 6. multiply by LCD

$$9x - 4 = \pm 6$$

$$9x = 10 \quad \text{or} \quad 9x = -2$$

$$x = \frac{10}{9} \quad \quad \quad x = -\frac{2}{9}$$

$$\text{Sum} = \frac{8}{9}$$

2) The solution for r of the equation $S = \frac{a-rl}{1-r}$ is

- A) $\frac{a}{l}$
B) $\frac{a-S}{l-S}$
 C) $\frac{a-S+Sr}{l}$
 D) $\frac{a-1}{l-1}$
 E) $\frac{rl-a+S}{S}$

$$S = \frac{a-rl}{1-r}$$

$$S(1-r) = a-rl$$

$$S - Sr = a - rl$$

$$-Sr + rl = a - S$$

$$r(l-S) = a-S$$

$$r = \frac{a-S}{l-S}$$

3) The perimeter of a rectangular garden is 112 meters. The length is 4 meters less than twice the width, then the length is

- A) 20 B) 28 meters C) 32 meters. D) 44 meters. **E) 36 meters.**

$$P = 2l + 2w = 112 \Rightarrow l + w = 56$$

$$l = 2w - 4 \Rightarrow 2w - 4 + w = 56$$

$$\Rightarrow 3w - 4 = 56$$

$$3w = 60 \Rightarrow w = 20 \Rightarrow l = 2w - 4 = 40 - 4 = \boxed{36}$$

4) If we complete the square in $2x^2 + 4x = -6$ we get $(x+m)^2 = l$, then $m+l$ is equal to

- A) 6 B) -1 C) -3 D) 1 E) 2

$$\begin{aligned} & 2x^2 + 4x = -6 \\ +2 & \quad \quad \quad x^2 + 2x = -3 \\ +4 & \quad \quad \quad x^2 + 2x + 4 = -3 + 4 = -2 \\ & \quad \quad \quad (x+2)^2 = -2 \\ & \quad \quad \quad m+l = \boxed{3} \\ & \quad \quad \quad +1 + (-2) = \boxed{-1} \end{aligned}$$

Code A

$$\begin{aligned} 2x^2 + 8x &= -10 \\ x^2 + 4x &= -5 \\ x^2 + 4x + 4 &= -5 + 4 \\ (x+2)^2 &= -1 \\ m+l &= 2 + (-1) = \boxed{1} \end{aligned}$$

5) The equation $\sqrt{3x+1} = \sqrt{x+4} + 1$, has

- A) Two solutions in $(-7, 7)$
- B) One solution in $(-7, 1)$
- C) Two solutions in $(-1, 7)$
- D) One solution in $(1, 7)$**
- E) Two solutions in $(-1, 7)$

$$\sqrt{3x+1} = \sqrt{x+4} + 1$$

Squaring

$$3x+1 = (x+4) + 2\sqrt{x+4} + 1$$

$$3x+1 - x - 4 - 1 = 2\sqrt{x+4}$$

$$2x - 4 = 2\sqrt{x+4} \quad \div 2$$

$$x - 2 = \sqrt{x+4}$$

$$x^2 - 4x + 4 = x + 4$$

$$x^2 - 5x = 0$$

$$x(x-5) = 0$$

Check

$$x = 0$$

$$\sqrt{0+1} = \sqrt{0+4} + 1$$

$$1 = 3 \text{ false}$$

$$x = 5$$

$$\sqrt{16} = \sqrt{9} + 1$$

$$4 = 4 \text{ True}$$

$$SS = \{5\}$$

6) The solution set for $\frac{1}{x-1} \leq \frac{2}{x+2}$ is

- A) $[2, \infty)$
- B) $(-\infty, -2) \cup [1, 4)$
- C) $(-\infty, -2] \cup [1, 4]$
- D) $(-2, 1) \cup [4, \infty)$**
- E) $[-2, 1] \cup [4, \infty)$

$$\frac{1}{x-1} - \frac{2}{x+2} \leq 0$$

$$\frac{x+2 - 2x+2}{(x-1)(x+2)} \leq 0$$

$$\frac{-x+4}{(x-1)(x+2)} \leq 0$$

$$\frac{x-4}{(x-1)(x+2)} \geq 0 \rightarrow \oplus \text{ or } 0$$

x	-2	1	4	
x-4	-	-	-	+
x-1	-	-	0	+
x+2	-	0	+	+
	-	+	-	+

$$SS = (-2, 1) \cup [4, \infty)$$

7) The set of values of k for which the equation $x^2 + kx = -k$ has one or two real solutions in x is

- A) $[0, 4]$
- B) $(-\infty, -4] \cup [0, \infty)$
- C) $(-\infty, 0] \cup [4, \infty)$**
- D) $(-\infty, 0) \cup (0, \infty)$
- E) $(0, 4)$

$$x^2 + kx + k = 0$$

1 or 2 real sol^{ns}

$$\Rightarrow \Delta \geq 0$$

$$k^2 - 4k \geq 0$$

$$k(k-4) \geq 0 \rightarrow \oplus \text{ or } 0$$

k	0	4	
k	-	0	+
k-4	-	-	0
	+	0	+

~~SS~~

$$k \in (-\infty, 0] \cup [4, \infty)$$