

1. Which of the following statements is FALSE?

- ~~(a)~~ The graph of  $f(x) = \log(-x)$  is increasing.
- (b) The domain of  $f(x) = -\log|x-2|$  is  $(-\infty, 2) \cup (2, \infty)$ .
- (c) The x-intercept of the graph of  $f(x) = \log_2(2x+1)$  is  $(0, 0)$ .
- (d) The range of  $f(x) = \log x$  is the set of all real numbers.
- (e) The equation of the vertical asymptote of  $f(x) = \ln \sqrt{x-1}$  is  $x = 1$ .

2. The expression  $3\log_2 a + 2\log_2 b - \frac{1}{2}\log_2 c$  can be written as

(a)  $\log_2 \left( \frac{a^3 b^2}{\sqrt{c}} \right)$

(b)  $\log_2 a^3 b^2$

(c)  $\log_2 \left( \frac{ab^2}{c} \right)$

(d)  $\log(a^3 bc)$

(e)  $\log \left( \frac{a^3 b}{\sqrt{c}} \right)$

$$= \log_2 a^3 + \log_2 b^2 - \log_2 c^{\frac{1}{2}}$$

$$= \log_2 (a^3 b^2) - \log_2 \sqrt{c}$$

$$= \log_2 \frac{a^3 b^2}{\sqrt{c}}$$

3. The  $x$ -intercept and the  $y$ -intercept of  $f(x) = -2 + \log_4(x+4)$  are

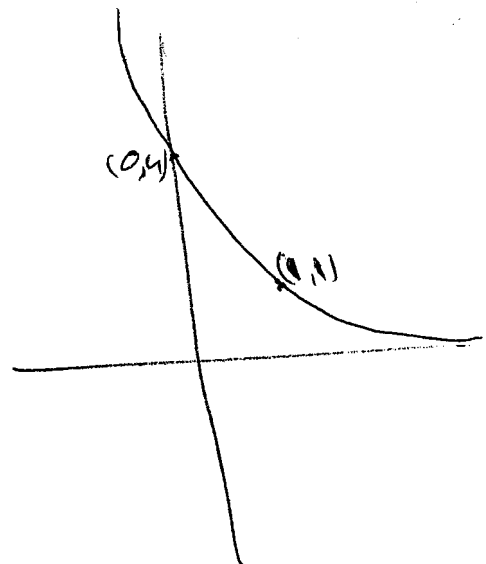
- (a)  $x$ -intercept  $(12, 0)$  and  $y$ -intercept  $(0, -1)$ .  
 (b)  $x$ -intercept  $(-12, 0)$  and  $y$ -intercept  $(0, -1)$ .  
 (c)  $x$ -intercept  $(-12, 0)$  and  $y$ -intercept  $(0, 1)$ .  
 (d)  $x$ -intercept  $(-1, 0)$  and  $y$ -intercept  $(0, 12)$ .  
 (e)  $x$ -intercept  $(1, 0)$  and  $y$ -intercept  $(0, -12)$ .

$x$ -int.  
 $0 = -2 + \log_4(x+4)$   
 $2 = \log_4(x+4)$   
 $4^2 = x+4, x=12$   
 $(12, 0)$

$y$ -int.  
 $y = -2 + \log_4 4$   
 $y = -2 + 1 = -1$   
 $(0, -1)$

4. The equation of the adjacent graph is

- (a)  $y = 2^{2-2x}$   
 (b)  $y = \left(\frac{1}{4}\right)^{-x} + 1$   
 (c)  $y = -(4^{x+1})$   
 (d)  $y = 4^{x-1}$   
 (e)  $y = \left(\frac{1}{4}\right)^x$



Point  $(1, 1)$  on the graph

$$x = 1, \quad y = 1$$

$$x = 0, \quad y = 4 \quad (0, 4)$$

only (a) satisfy the conditions

5. The function  $f(x) = -\frac{1}{2} \sin\left(x - \frac{\pi}{2}\right) - 2$  has

- (a) Amplitude =  $\frac{1}{2}$ , period =  $2\pi$  and phase shift =  $\frac{\pi}{2}$   
 (b) Amplitude =  $-\frac{1}{2}$ , period =  $2\pi$  and phase shift =  $\frac{\pi}{2}$   
 (c) Amplitude =  $\frac{1}{2}$ , period =  $\pi$  and phase shift =  $\pi$   
 (d) Amplitude =  $-\frac{1}{2}$ , period =  $\frac{\pi}{4}$  and phase shift =  $\pi$   
 (e) Amplitude =  $\frac{1}{2}$ , period =  $\pi$  and phase shift =  $\frac{\pi}{2}$

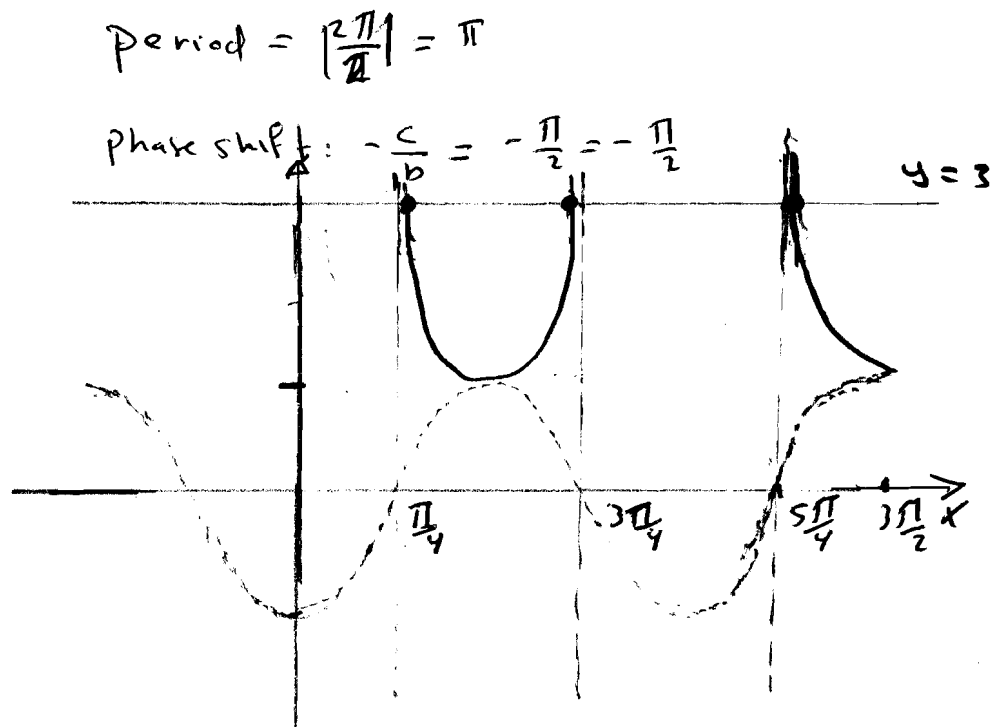
$$\text{amp.} = \left| -\frac{1}{2} \right| = \frac{1}{2}$$

$$\text{period} = \left| \frac{2\pi}{b} \right| = \left| \frac{2\pi}{1} \right| = 2\pi$$

$$\text{p. shift} = -\frac{c}{b} = -\frac{(-\pi/2)}{1} = \frac{\pi}{2}$$

6. If  $x \in \left[0, \frac{3\pi}{2}\right]$ , then the number of the points of intersection between the graph of  $y = \sec(2x + \pi)$  and the line  $y = 3$  is equal to

- (a) 3  
 (b) 1  
 (c) 2  
 (d) 4  
 (e) 5



7. The range of  $y = 1 + 4 \csc x$  is

(a)  $(-\infty, -3] \cup [5, \infty)$

(b)  $(-\infty, -3) \cup (5, \infty)$

(c)  $(-\infty, -1) \cup (1, \infty)$

(d)  $(-\infty, -1] \cup [1, \infty)$

(e)  $(-1, 4) \cup (5, \infty)$

$$-\infty < \csc x \leq -1 \text{ or } 1 \leq \csc x < \infty$$

$$-\infty < 4 \csc x \leq -4 \text{ or } 4 \leq \csc x < \infty$$

$$-\infty < 4 \csc x + 1 \leq -3 \text{ or } 5 \leq \csc x + 1 < \infty$$

$$R: (-\infty, -3] \cup [5, \infty)$$

8. The number of vertical asymptote(s) of  $y = 3 \cot \frac{x}{2}$  in the interval  $(-\frac{\pi}{2}, \pi)$  is

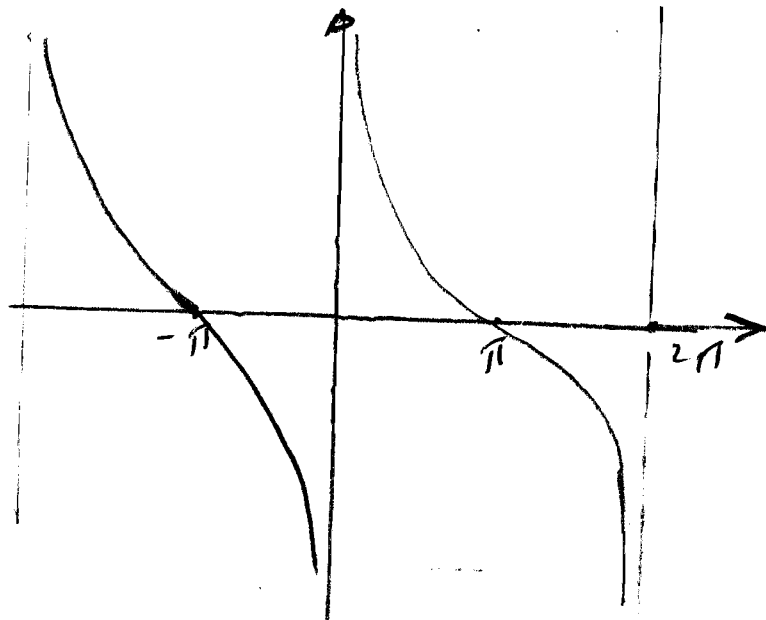
(a) 1

(b) 2

(c) 0

(d) 3

(e) 4



only one asymptote  $x = 0$

9. The adjacent figure represents the graph of

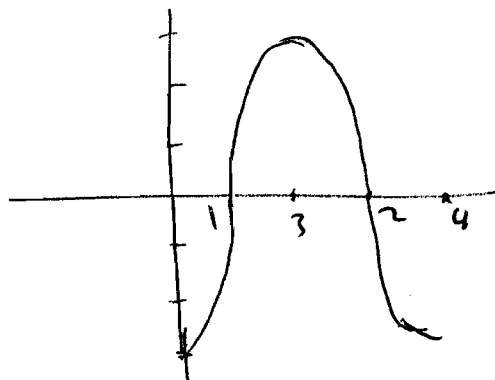
(a)  $y = -3 \cos\left(\frac{\pi}{2}x\right)$

(b)  $y = 3 \sin \pi x$

(c)  $y = 3 \cos\left(\frac{5\pi}{2}x\right)$

(d)  $y = 3 \sin(-\pi x)$

(e)  $y = -3 \cos\left(\frac{3\pi}{2}x\right)$



$$y = a \cos bx \quad a = -3$$

$$\text{period} = 4 = \frac{2\pi}{b}, \quad b = \frac{\pi}{2}$$

$$y = -3 \cos\left(\frac{\pi}{2}x\right)$$

10. The expression  $\frac{\sin x}{1 + \cos x} + \frac{1 + \cos x}{\sin x}$  can be simplified to

(a)  $2 \csc x$

(b)  $2 \cos x$

(c)  $\tan x$

(d)  $\sin x - \cos x$

(e)  $\sin x + \cos x$

$$\frac{\sin x}{1 + \cos x} + \frac{1 + \cos x}{\sin x} = \frac{\sin^2 x + (1 + \cos x)^2}{\sin x (1 + \cos x)}$$

$$= \frac{\sin^2 x + 1 + 2 \cos x + \cos^2 x}{\sin x (1 + \cos x)}$$

$$= \frac{1 + 1 + 2 \cos x}{\sin x (1 + \cos x)} = \frac{2(1 + \cos x)}{\sin x (1 + \cos x)}$$

$$= \frac{2}{\sin x} = 2 \csc x$$

11. If  $w$  is the wrapping function, then  $w\left(\frac{22\pi}{3}\right)$  is equal to

✓ (a)  $\left(-\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$

(b)  $\left(-\frac{\sqrt{3}}{2}, -\frac{1}{2}\right)$

(c)  $\left(-\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$

(d)  $\left(\frac{\sqrt{3}}{2}, -\frac{1}{2}\right)$

(e)  $\left(\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$

$$w\left(\frac{22\pi}{3}\right) = w\left(6\pi + \frac{4\pi}{3}\right)$$

$$= w\left(\frac{4\pi}{3}\right) = (x, y)$$

$$= \left(\cos \frac{4\pi}{3}, \sin \frac{4\pi}{3}\right)$$

$$\cos \frac{4\pi}{3} = -\cos \frac{\pi}{3} = -\frac{1}{2}$$

$$\sin \frac{4\pi}{3} = -\sin \frac{\pi}{3} = -\frac{\sqrt{3}}{2}$$

$$w\left(\frac{22\pi}{3}\right) = \left(-\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$$

12. The reference angle of  $\theta = 30$  radians is equal to

$$30 = 4(2\pi) + 4.88$$

$$30 \text{ in } \underline{10}$$

$$10\pi \approx 31.4$$

$$\theta' = 2\pi - (30 - 8\pi)$$

$$= 10\pi - 30$$

✓ (a)  $10\pi - 30$

(b)  $30 - 10\pi$

(c)  $30 - 8\pi$

(d)  $-30$

(e)  $30 - 6\pi$

13. If the point  $(-2, -3)$  is on the terminal side of the angle  $\theta$  in the standard position, then  $3 \sin \theta + 2 \cos \theta$  is equal to

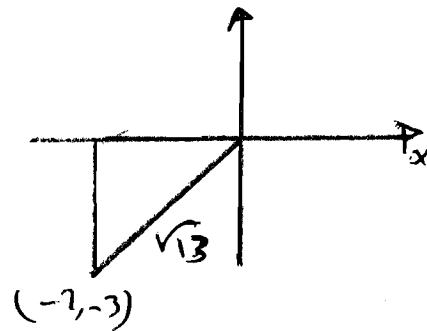
(a)  $-\sqrt{13}$

(b)  $-5 \frac{\sqrt{13}}{13}$

(c)  $-2 \frac{\sqrt{13}}{13}$

(d)  $-6 \frac{\sqrt{13}}{13}$

(e) 13



$$\sin \theta = \frac{-3}{\sqrt{13}}, \quad 3 \sin \theta = \frac{-9}{\sqrt{13}}$$

$$\cos \theta = \frac{-2}{\sqrt{13}}, \quad 2 \cos \theta = \frac{-4}{\sqrt{13}}$$

$$3 \sin \theta + 2 \cos \theta = \frac{-9}{\sqrt{13}} - \frac{4}{\sqrt{13}} = \frac{-13}{\sqrt{13}}$$

$$= -\sqrt{13}$$

14.  $\csc(-510^\circ) + 4 \cos(150^\circ) \sin(120^\circ) + \tan(405^\circ)$  is equal to

(a) -4

(b) 3

(c) 5

(d) -5

(e) -2

$$\begin{aligned} \csc(-510^\circ) &= -\csc(510^\circ) = -\csc 210^\circ \\ &= -\csc 30^\circ \\ &= -2 \end{aligned}$$

$$\begin{aligned} 4 \cos(150^\circ) \sin(120^\circ) &= 4(-\cos 30^\circ) \sin 60^\circ \\ &= -4 \cdot \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{3}}{2} = -3 \end{aligned}$$

$$\tan(405^\circ) = \tan 45^\circ = 1$$

$$\begin{aligned} &\csc(-510^\circ) + 4 \cos 150^\circ \sin 120^\circ + \tan 405^\circ \\ &= -2 - 3 + 1 = -4 \end{aligned}$$

17. If  $\alpha$  is the smallest positive angle coterminal with  $-743^\circ$  and  $\beta$  is the smallest positive angle coterminal with  $610^\circ$ , then  $\alpha - \beta$  is equal to

(a)  $87^\circ$

(b)  $105^\circ$

(c)  $337^\circ$

(d)  $250^\circ$

(e)  $225^\circ$

$$-743^\circ = X^\circ - 2(360^\circ)$$

$$X^\circ = -743^\circ + 720 = -23 \text{ (Neg. cot)}$$

$$\alpha = -23^\circ + 360^\circ = 337^\circ \text{ (pos. cot)}$$

$$610^\circ = X^\circ + 1(360^\circ)$$

$$X^\circ = 610^\circ - 360^\circ = 250^\circ$$

$$\beta = 250^\circ$$

$$\alpha - \beta = 337^\circ - 250^\circ = 87^\circ$$

18. The solution of the equation  $\frac{e^x + e^{-x}}{e^x - e^{-x}} = 3$  is equal to

(a)  $\frac{\ln 2}{2}$

(b)  $\ln 3$

(c)  $\frac{\ln 3}{2}$

(d)  $\ln\left(\frac{2}{3}\right)$

(e)  $\frac{\ln 2}{3}$

$$e^x + e^{-x} = 3e^x - 3e^{-x}$$

$$e^{2x} + e^0 = 3e^{2x} - 3e^0$$

$$e^{2x} - 3e^{2x} = -4$$

$$2e^{2x} = 4$$

$$e^{2x} = 2$$

$$2x \ln e = \ln 2$$

$$2x = \ln 2$$

$$x = \frac{\ln 2}{2}$$



19. The solution of the equation  $\log(x+8) + \log(2x+13) = \log(4-x)$  consists of

- (a) One negative integer only.  
 (b) One positive real number only.  
 (c) Two non-negative integers.  
 (d) Two positive real numbers.  
 (e) One negative and one positive integers.

$$\begin{aligned} \log(x+8)(2x+13) &= \log(4-x) \\ \log(2x^2 + 29x + 104) &= \log(4-x) \\ 2x^2 + 29x + 104 &= 4-x \\ 2x^2 + 30x + 100 &= 0 \\ x^2 + 15x + 50 &= 0 \\ (x+5)(x+10) &= 0 \\ x &= -10 \\ x &= -5 \end{aligned}$$

reject  $x = -10$ , solution  $x = -5$

20. If  $\log_2 5 = x$  and  $\log_2 3 = y$ , then  $\log_{\sqrt{2}} 30$  is equal to

- (a)  $2(x+y+1)$   
 (b)  $\frac{1}{2}(x+y+1)$   
 (c)  $\frac{x+y}{2}$   
 (d)  $2x+1$   
 (e)  $\frac{x+2y}{2}$

$$\begin{aligned} \log_{\sqrt{2}} 30 &= \frac{\log_2 30}{\log_2 \sqrt{2}} = 2 \log_2 30 \\ 2 \log_2 30 &= 2 \log_2 (5 \cdot 6) \\ &= 2 [\log_2 5 + \log_2 6] \\ &= 2 [\log_2 5 + \log_2 2 \cdot 3] \\ &= 2 [\log_2 5 + \log_2 2 + \log_2 3] \\ &= 2 (x + 1 + y) \end{aligned}$$

21. If  $f(x) = a^x$  and  $f(-2) = \frac{1}{3}$ , then  $f(6)$  is equal to

(a) 27

(b) 2

(c) 9

(d) 12

(e) 18

$$f(-2) = a^{-2} = \frac{1}{a^2} = \frac{1}{3}$$

$$f(6) = a^{-6} = \frac{1}{a^6} = \left(\frac{1}{a^2}\right)^3 = \left(\frac{1}{3}\right)^3 = \frac{1}{27}$$

22. Which of the following is undefined

(a)  $\ln(\cos \pi)$

(b)  $\cos(\ln 1)$

(c)  $\sin(\ln 1)$

(d)  $\log(\ln e)$

(e)  $\log(\cos 0)$

$$\cos \pi = -1$$

$\ln(-1)$  undefined.