

Q12

$$\vec{J} = \int \vec{F} \cdot dt = F_{avg} \Delta t \quad \text{definition of } \vec{J}, \text{ impulse}$$

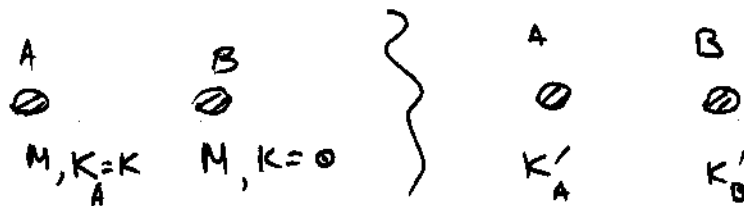
but this doesn't help as we don't know $\int \vec{F} \cdot dt$ or $F_{avg} \Delta t$, so use

$$\vec{J} = \Delta \vec{p} \quad \text{impulse momentum theory}$$

$$\begin{aligned} \Rightarrow \vec{J} &= m (\vec{v}_f - \vec{v}_i) \\ &= (3 \cdot 0) \{ (-3\hat{i} + 2\hat{j}) - (3\hat{i} + 2\hat{j}) \} \\ &= (3 \cdot 0) \{ -6\hat{i} + 0\hat{j} \} \end{aligned}$$

$$\vec{J} = \underline{\underline{-18 \hat{i}}} \text{ (N.s)}$$

Q13



Conservation of momentum

$$Mv_A + 0 = Mv'_A + Mv'_B$$

$$v_A = v'_A + v'_B \quad \text{--- (1)}$$

Conservation of K

$$\Rightarrow \frac{1}{2} M v_A^2 + 0 = \frac{1}{2} M v_A'^2 + \frac{1}{2} M v_B'^2$$

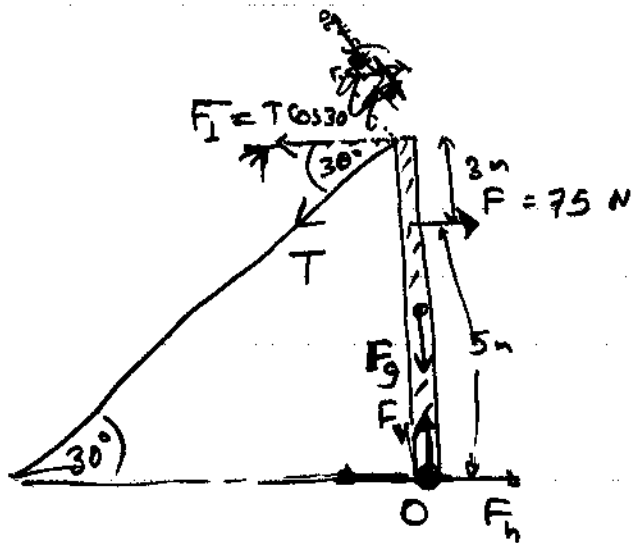
$$v_A^2 = v_A'^2 + v_B'^2 \quad \text{--- (2)}$$

Solving for (1) & (2)

$$\Rightarrow v'_A = 0 \quad \& \quad v'_B = v_A$$

$$\therefore K'_A = 0$$

Q14)



The beam is acted upon by 5 forces
 $\mathbf{F}_T, \mathbf{F}, \mathbf{F}_g, \mathbf{F}_v$ & \mathbf{F}_h .

However we can ~~efficiently~~ ^{quickly} solve the problem by taking net torque about point O (the pin) and equating it to zero (rotational equilibrium).

$$\sum \tau_O = 0$$

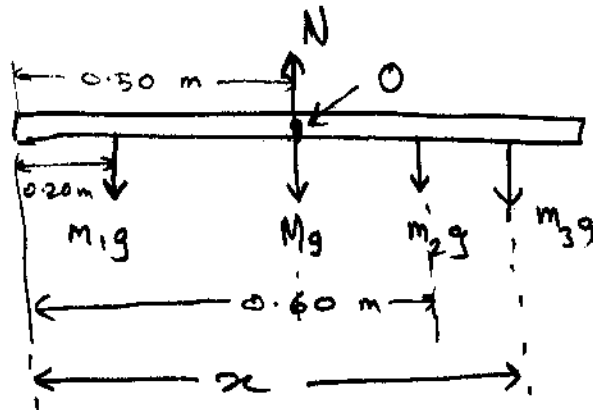
$$\vec{\tau}_T + \vec{\tau}_F + \vec{\tau}_{F_g} + \vec{\tau}_{F_v} + \vec{\tau}_{F_h} = 0$$

$$\vec{\tau}_T + \vec{\tau}_F = 0$$

$$+ (T \cancel{30})(8) - (75)5 = 0$$

$$T = \frac{(75)(5)}{8 \cancel{30}} = \underline{\underline{54 \text{ N}}}$$

Q15



$m_1 = 0.5 \text{ kg}$
 $m_2 = 0.3 \text{ kg}$
 $M = \text{mass of meter stick?}$
 (not given)

m_3 is the third mass hung at position ' x ' to keep the meter stick balanced. Take the torque about the center of the meter stick. (point O).

$$Mg + m_1g(0.3) - m_2g(0.1) - m_3g(x - 0.5) = 0$$

$$(0.5)(0.3) - (0.3)(0.1) = m_3(0.6)(x - 0.5)$$

$$\cancel{5} 0.15 - 0.03 = 0.6x - 0.3$$

$$0.6x = 0.42$$

$$x = 0.70 \text{ m}$$

$$x = \underline{\underline{70 \text{ cm}}}$$

Q16

$$\frac{F}{A} = E \frac{\Delta l}{l} \quad \text{tensile stress (stretching)}$$

$$\Delta l = \frac{F l}{EA} = \frac{(25000)(20)}{(2.0 \times 10^{11})(1.0 \times 10^{-4})}$$

Note $A = 1.0 \text{ cm}^2 = \underline{\underline{1.0 \times 10^{-4} \text{ m}^2}}$

$$\Delta l = 0.025 \text{ m} \\ = \underline{\underline{2.5 \text{ cm}}}$$

Q17

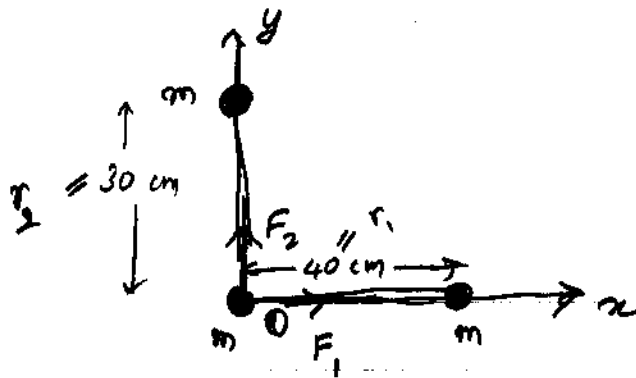
$$T^2 = \frac{4\pi^2}{GM} r^3$$

$$r^3 = \frac{GM T^2}{4\pi^2} = \frac{(6.67 \times 10^{-11})(5.0 \times 10^{24})(98 \times 60)^2}{4\pi^2}$$

Note $T = 98 \text{ min} = \underline{\underline{(98 \times 60) \text{ s}}}$

$$\Rightarrow r^3 = 2.92 \times 10^{20} \text{ m}^3 \\ \Rightarrow r = \underline{\underline{6.6 \times 10^6 \text{ m}}}$$

Q18



$$m = 5 \text{ kg}$$

$$r_1 = 40 \text{ cm}$$

$$r_2 = 30 \text{ cm}$$

$$\vec{F}_{\text{net}} = \vec{F}_1 + \vec{F}_2$$

$$= \frac{G m^2}{r_1^2} \hat{i} + \frac{G m^2}{r_2^2} \hat{j}$$

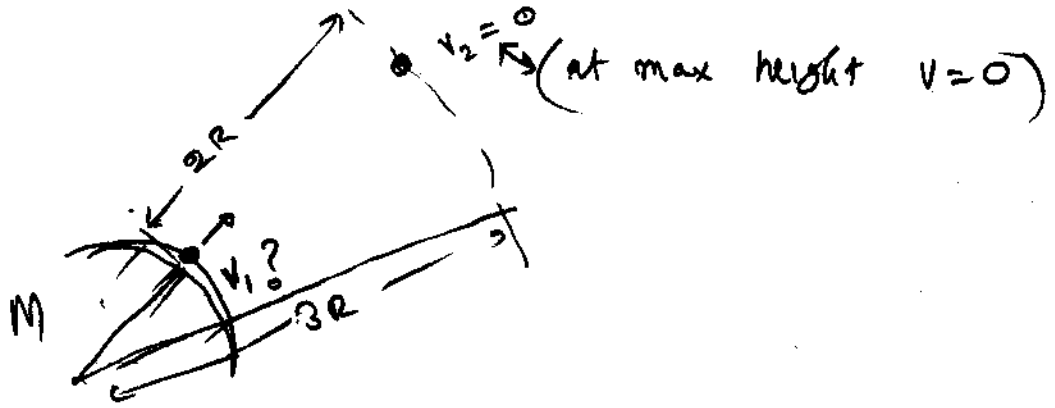
$$= G m^2 \left\{ \frac{1}{(0.4)^2} \hat{i} + \frac{1}{(0.3)^2} \hat{j} \right\}$$

$$\vec{F}_{\text{net}} = (6.67 \times 10^{-11}) (5)^2 \left\{ 6.25 \hat{i} + 11.1 \hat{j} \right\}$$

$$|\vec{F}_{\text{net}}| = (6.67 \times 10^{-11}) (25) \sqrt{(6.25)^2 + (11.1)^2}$$

$$= \underline{\underline{2.1 \times 10^{-8} \text{ N}}}$$

Q19



$$K_1 + U_1 = K_2 + U_2$$

(Note you can't say $K + U = C = \frac{GMm}{R}$)

$$\frac{1}{2} M v_1^2 + \left(-\frac{GMm}{R} \right) = 0 + \left(-\frac{GMm}{3R} \right)$$

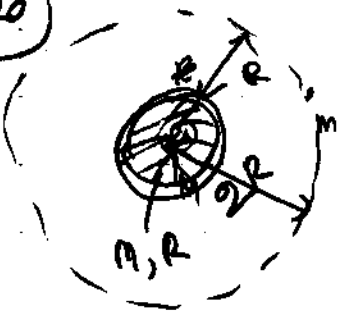
(m) is the mass of the rocket (say)

$$\frac{1}{2} v_1^2 = \frac{GM}{R} - \frac{GM}{3R} = \frac{GM}{R} \left\{ 1 - \frac{1}{3} \right\}$$

$$v_1^2 = \frac{2GM}{R} \left(\frac{2}{3} \right)$$

$$v_1 = \sqrt{\frac{4GM}{3R}}$$

Q20



$$\frac{1}{2} M v_{esc}^2$$

$$K_1 + U_1 = K_2 + U_2$$

$$\frac{1}{2} M v_{esc}^2 + \left(-\frac{GMm}{R} \right) = 0 + \left(-\frac{GMm}{2R} \right)$$

$$K_{esc} + \left(-\frac{GMm}{R} \right) = \left(-\frac{GMm}{2R} \right)$$

$$v_{esc}^2 = \frac{2GM}{R}$$

~~K_{esc}~~
 This question is not clear whether the spaceship is at a distance R from the center of the planet OR a distance $(2R)$ from the center of the planet with R as the radius of the planet.

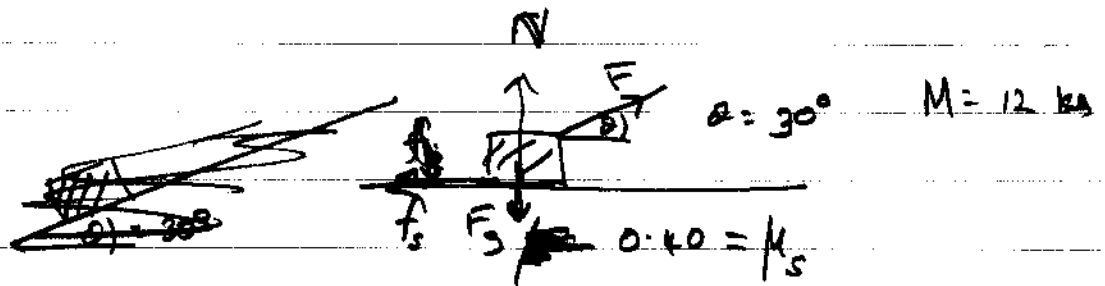
ASSUMING

$$\begin{array}{c}
 K_{esc} + U_1 = K_a + U_2 \\
 \downarrow \quad \downarrow \quad \searrow \quad \swarrow \\
 K_{esc} + \left(\frac{-GMm}{(2R)} \right) = 0 + 0
 \end{array}$$

(assuming $r = 2R$)

$$K_{esc} = \frac{GMm}{2R}$$

(P21)



$\Sigma F_x = 0$ with max static friction force $f_s = f_{s, \max}$

$$F \cos \theta - f_{s, \max} = 0$$

$$F \cos \theta - \mu_s N = 0 \quad \text{--- (1)}$$

$$\Sigma F_y = 0$$

$$N + F \sin \theta - F_g = 0$$

$$N = Mg - F \sin \theta \quad \text{--- (2)}$$

(2) via (1)

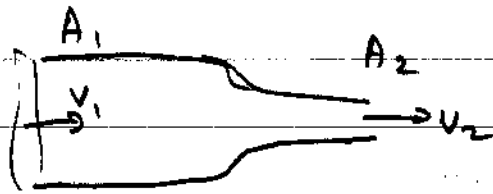
$$F \cos \theta - \mu_s (Mg - F \sin \theta) = 0$$

$$F (\cos \theta + \mu_s \sin \theta) = \mu_s Mg$$

$$F = \frac{\mu_s Mg}{\cos \theta + \mu_s \sin \theta} = \frac{(0.4)(12)(9.8)}{(\cos 30 + (0.4) \sin 20)}$$

$$F = \underline{\underline{44 \text{ (N)}}}$$

(Q23)



continuity equation

$$A_1 v_1 = A_2 v_2$$

$$\frac{v_2}{v_1} = \frac{A_1}{A_2}$$

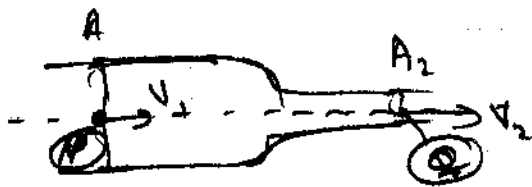
(Q24)

$$P + \frac{1}{2} \rho v^2 + \rho g y = \text{const}$$

is derived from law of conservation

of Energy

Q25



$$A_1 v_1 = A_2 v_2 \quad \text{--- (1)}$$

Bernoulli's equ. $\rightarrow P_1 + \frac{1}{2} \rho v_1^2 + \cancel{\rho g y_1} = P_2 + \frac{1}{2} \rho v_2^2 + \cancel{\rho g y_2}$

But we have ~~P_1~~ $y_1 = y_2$ horizontal

$$P_1 + \frac{1}{2} \rho v_1^2 = P_2 + \frac{1}{2} \rho v_2^2$$

$$(P_1 - P_2) = \frac{1}{2} \rho (v_2^2 - v_1^2)$$

$$= \frac{1}{2} \rho \left(\left[\frac{A_1 v_1}{A_2} \right]^2 - v_1^2 \right) \quad \text{from (1)}$$

$$\Rightarrow v_2 = \frac{A_1 v_1}{A_2}$$

but it is given that $\frac{A_1}{A_2} = 2$

$$\Rightarrow (P_1 - P_2) = \frac{1}{2} \rho (4v_1^2 - v_1^2) = \frac{1}{2} \rho 3v_1^2$$

$$v_1^2 = \frac{2(P_1 - P_2)}{\rho(3)} = \frac{2(4120)}{(791)(3)} =$$

$$v_1 = \underline{\underline{1.86 \text{ m/s}}}$$

Q26

$$x = \frac{2}{3} \text{Gs} (50 \text{ t}) \quad k = ? \quad m = \underline{\underline{3 \text{ kg}}}$$

$$\Rightarrow x_m = 2 \text{ (m)} \quad \& \quad \omega = 50 \text{ (rad/s)}$$

$$k = m\omega^2 = (3)(50)^2 = \underline{\underline{7500 \text{ N/m}}}$$

Q27

$$v_m = \omega x_m = ?$$

Given $x_m = 'A'$, ~~mass = 'm'~~, spring const = 'k' & *
mass = 'm'

$$k = m\omega^2 \Rightarrow \omega = \sqrt{\frac{k}{m}}$$

$$\Rightarrow v_m = \underline{\underline{\left(\sqrt{\frac{k}{m}}\right) A}}$$

Q28

$m = 0.25 \text{ kg}$, $k = 200 \frac{\text{N}}{\text{m}}$, } given
 $x(t=0) = 0.15 \text{ (m)}$
 $v(t=0) = 3.0 \text{ (m/s)}$

find $v_m = \omega x_m$

$$\omega = \sqrt{\frac{k}{m}} = \sqrt{\frac{200}{0.25}} = 28.3 \text{ rad/s}$$

$$x = x_m \cos(\omega t + \phi)$$

$$\Rightarrow 0.15 = x_m \cos \phi \quad \text{--- (1)}$$

$$v = -\omega x_m \sin(\omega t + \phi)$$

$$\underline{\underline{v_m \sin(\omega t + \phi)}}$$

$$\Rightarrow 3.0 = -28.3 x_m \sin \phi \quad \text{--- (2)}$$

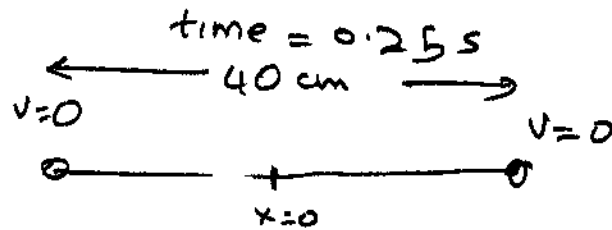
$$-0.106 = x_m \sin \phi \quad \text{--- (2)}$$

$$\text{(1)}^2 + \text{(2)}^2 \Rightarrow (0.15)^2 + (-0.106)^2 = x_m^2$$

$$x_m = 0.184 \text{ (m)}$$

$$v_m = \omega x_m = (28.3)(0.184) = \underline{\underline{5.2 \text{ m/s}}}$$

Q29



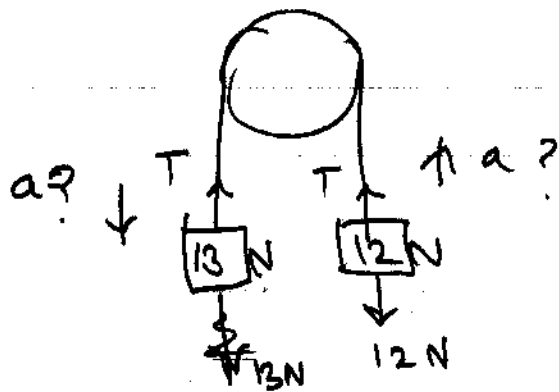
$$\Rightarrow T/2 = 0.25 \text{ (s)} \quad \& \quad \frac{2L}{m} = 40 \text{ cm}$$

$$x_m = \underline{20 \text{ cm}} = \del{0.20 \text{ m}}$$

$$T = 0.50 \text{ (s)} \Rightarrow \del{0.50 \text{ s}}$$

$$f = \frac{1}{T} = \underline{2 \text{ Hz}}$$

Q30



$$\underline{13 \text{ N}} \quad 13 - T = \left(\frac{13}{g}\right) a \quad \text{--- (1)}$$

$$\underline{12 \text{ N}} \quad T - 12 = \left(\frac{12}{g}\right) a \quad \text{--- (2)}$$

$$\textcircled{1} + \textcircled{2} \quad 1 = \left(\frac{13}{g} + \frac{12}{g}\right) a$$

$$g = 25 a$$

$$a = \underline{\underline{\frac{g}{25}}}$$