
Chapter 2 Homework Solutions – phys101-081

1. q1

A car travels up a hill at a constant speed of 58.3 km/h and returns down the hill at a constant speed of 27.4 km/h. Calculate the average speed for the round trip in km/h and give to three significant digits.

$$\begin{aligned}\text{Average speed} &= \frac{s(\text{total distance})}{t(\text{total time})} = \frac{s_1(\text{uphill}) + s_2(\text{downhill})}{t_1 + t_2} \\ &= \frac{(s_1 + s_2)km}{\frac{(s_1)km}{(58.3)km/h} + \frac{(s_2)km}{(27.4)km/h}} \\ \text{But } s_1 &= s_2 = s \\ &= \frac{(2s)km}{\frac{(s)km}{(58.3)km/h} + \frac{(s)km}{(27.4)km/h}} \\ &= \frac{2}{\frac{1}{(58.3)km/h} + \frac{1}{(27.4)km/h}} \\ &= \boxed{37.3}\end{aligned}$$

Give the answer to **exactly 3** significant figures and no need to give units; an answer such as 37.30 or 37.3km or +37.3 would result in zero score. if you want to write the units give it after a space: 37.3 km

2. q2

At a certain time a particle has a speed of 44.6 m/s in the positive x direction, and 1.2 s later its speed was 24.3 m/s in the opposite direction. What is the average acceleration of the particle during this 1.2 s interval? Give the answer in m/s² and give three significant digits only.

$$\text{average acceleration} = \frac{\Delta v}{\Delta t} = \frac{-24.3 - (44.6)}{1.2} = \boxed{-57.4}$$

3. q3a

An electron has a constant acceleration of +2.3 m/s². At a certain instant its velocity is +9.6 m/s. What is its velocity 2.52 s earlier? Give the answer in m/s and give two significant figures only.

Using $v = v_o + at$

with $v=9.6$ m/s at time 2.52 s and v_o is the unknown initial velocity
at $t = 0$.

$$9.6 = v_o + 2.3 \times 2.52$$

$$\Rightarrow v_o = \boxed{3.8}$$

4. q3b

An electron has a constant acceleration of $+2.3 \text{ m/s}^2$. At a certain instant its velocity is $+9.6$ m/s. What is its velocity 2.36 s later? Give the answer in m/s and give two significant figures only.

Using $v = v_o + at$

with $v_o = 9.6$ m/s at $t=0$ and unknown final velocity v
at $t = 2.36$ s.

$$v = 9.36 + 2.3 \times 2.36$$

$$\Rightarrow v = \boxed{15}$$

5. q4a

If the maximum acceleration that is tolerable for passengers in a subway train is 1.34 m/s^2 and subway stations are located 253 m apart. What is the maximum speed a subway train can attain between stations? Give the answer in m/s and give three significant figures.

The key point here is to understand that to attain maximum speed the train has to accelerate at 1.34 m/s^2 halfway to the next station and then decelerate at 1.34 m/s^2 for the second half.

Applying $v^2 = v_o^2 + 2a\Delta x$ for the first half ($\Delta x = 253/2$, $a = 1.34$ and $v_o = 0$)

$$v = \boxed{18.4}$$

6. q4b

If the maximum acceleration that is tolerable for passengers in a subway train is 1.34 m/s^2 and subway stations are located 806 m apart. If a subway train stops for 20 s at each station, what is the maximum average speed of the train, from one start-up to the next? Give the answer in m/s and give three significant figures.

The journey consists of three parts: Station A to halfway, from halfway to Station B, and the stopping at station B for 20 s. To solve this question, one has to again calculate the maximum speed as above (with the new values now).

Applying $v^2 = v_o^2 + 2a\Delta x$ for the first half ($\Delta x = 806/2$, $a = 1.34$ and $v_o = 0$)

$$v_{\text{max}} = 32.864 \text{ m/s}$$

time (t_1) to reach halfway:

Applying $v = v_o + at$; ($v = 32.864$, $a = 1.34$, and $v_o = 0$)

$$t_1 = (32.864 - 0) / 1.34 = 24.5253 \text{ s} = \text{this is also equal to } t_2; \text{ and } t_3 = 20 \text{ s.}$$

$$\begin{aligned}
\text{average speed} &= \frac{s_1 + s_2 + s_3}{t_1 + t_2 + t_3} \\
&= \frac{s_1 + s_1 + s_3}{t_1 + t_1 + 20} \text{ from symmetry of the two journeys} \\
&= \frac{2s_1}{2t_1 + 20} \\
&= \frac{806}{2 * 24.5253 + 20} \\
&= \boxed{11.7}
\end{aligned}$$

7. q5

A rock is thrown vertically upward from ground level at time $t = 0$. At $t = 1.6$ s it passes the top of a tall tower, and 2.6 s later it reaches its maximum height. What is the height of the tower? Give the answer in m and give only 3 significant digits.

First consider the rock going from ground level to the maximum height to get the initial velocity of the rock:

Solving: $0 = v_o - 9.8 * 3.6$, gives $v_o = 35.28$ m/s

Now consider the motion from the ground to the top of the tower only:

Using $\Delta y = v_o t + (1/2) a t^2 = 35.28 * 1.6 - 0.5 * 9.8 * 1.6^2 = \boxed{43.9}$

8. q6

A jumbo jet must reach a speed of 396 km/h on the runway for takeoff. What is the lowest constant acceleration needed for takeoff a 2.7 km runway? Give the answer in m/s^2 and give three significant figures.

$\Delta x = 2700$ m, $v_o = 0$, $v = 396/3.6$ m/s, $a = ?$, $t = ?$

Solving $v^2 = v_o^2 + 2 a \Delta x$ gives $a = \boxed{2.24}$