

Physics 101- Chapter 4

Quiz No. 2

Name: Key

ID:

Sec: 28

A stone was thrown with initial speed 17.5 m/s from original point O. The stone has passed through constant point A, which has horizontal distance 10 m, and vertical 5 m from O.

1- Find out the two possible values of throw angles.

2- Calculate the horizontal ranges for the two throw angles.

$$1- v_0 = 17.5 \text{ m/s}, x = 10 \text{ m}, y = 5 \text{ m}, \theta_0 = ?$$

$$y = x \tan \theta_0 - \frac{g x^2}{2 v_0^2 \cos^2 \theta_0}$$

$$5 = 10 \tan \theta_0 - \frac{9.8 \times (10)^2}{2 \times (17.5)^2 \cos^2 \theta_0}$$

$$5 = 10 \tan \theta_0 - \frac{100 \times 9.8 \sec^2 \theta_0}{2 \times (17.5)^2}$$

$$50 = 100 \tan \theta_0 - 16 \tan^2 \theta_0 - 16$$

$$16 \tan^2 \theta_0 - 100 \tan \theta_0 + 66 = 0$$

$$8 \tan^2 \theta_0 - 50 \tan \theta_0 + 33 = 0$$

$$(4 \tan \theta_0 - 3)(2 \tan \theta_0 - 11) = 0$$

$$\therefore \tan \theta_{01} = \frac{3}{4}, \quad \tan \theta_{02} = \frac{11}{2}$$

2- Horizontal ranges:

$$R = \frac{v_0^2 \sin 2\theta_0}{g} \Rightarrow R = \frac{v_0^2 2 \sin \theta_0 \cos \theta_0}{g}$$

$$\therefore R_1 = \left[2 \times (17.5)^2 \times \frac{11}{\sqrt{125}} \times \frac{2}{\sqrt{125}} \right] / g = 11 \text{ m}$$

$$\therefore R_2 = \left[2 \times (17.5)^2 \times \frac{3}{5} \times \frac{4}{5} \right] / g = 30 \text{ m}$$

