

23. A force in the negative direction of an x-axis is applied for 27ms to a 0.40kg ball initially moving at 14m/s in the positive direction of the axis. The force varies in magnitude, and the impulse has magnitude 32.4 N.s. What are the ball's

a) Speed and

b) Direction of travel just after the force is applied ?

c) What are the average magnitude of the force and

d) The direction of the impulse on the ball?

23. The initial direction of motion is in the $+x$ direction. The magnitude of the average force F_{avg} is given by

$$F_{avg} = \frac{J}{\Delta t} = \frac{32.4 \text{ N}\cdot\text{s}}{2.70 \times 10^{-2} \text{ s}} = 1.20 \times 10^3 \text{ N}$$

The force is in the negative direction. Using the linear momentum-impulse theorem stated in Eq. 9-31, we have

$$-F_{avg}\Delta t = mv_f - mv_i.$$

where m is the mass, v_i the initial velocity, and v_f the final velocity of the ball. Thus,

$$v_f = \frac{mv_i - F_{avg}\Delta t}{m} = \frac{(0.40 \text{ kg})(14 \text{ m/s}) - (1200 \text{ N})(27 \times 10^{-3} \text{ s})}{0.40 \text{ kg}} = -67 \text{ m/s}.$$

- (a) The final speed of the ball is $|v_f| = 67 \text{ m/s}$.
- (b) The negative sign indicates that the velocity is in the $-x$ direction, which is opposite to the initial direction of travel.
- (c) From the above, the average magnitude of the force is $F_{avg} = 1.20 \times 10^3 \text{ N}$.
- (d) The direction of the impulse on the ball is $-x$, same as the applied force.

27. A 1.2 kg ball drops vertically onto floor, hitting with a speed of 25m/s. It rebounds with an initial speed of 10m/s

a) What impulse acts on the ball during the contact?

b) If the ball is in contact with the floor for 0.020s, what is the magnitude of the average force on the floor from the ball?

27. We choose $+y$ upward, which means $\vec{v}_i = -25 \text{ m/s}$ and $\vec{v}_f = +10 \text{ m/s}$. During the collision, we make the reasonable approximation that the net force on the ball is equal to F_{avg} – the average force exerted by the floor up on the ball.

(a) Using the impulse momentum theorem (Eq. 9-31) we find

$$\vec{J} = m\vec{v}_f - m\vec{v}_i = (1.2)(10) - (1.2)(-25) = 42 \text{ kg} \cdot \text{m/s}.$$

(b) From Eq. 9-35, we obtain

$$\vec{F}_{\text{avg}} = \frac{\vec{J}}{\Delta t} = \frac{42}{0.020} = 2.1 \times 10^3 \text{ N}.$$

42. A 4.0 kg mess kit sliding on a frictionless surface explodes into two 2.0kg parts: 3.0m/s, due north, and 5.0m/s 30degree north of east. What is the original speed of the mess kit?

42. Our $+x$ direction is east and $+y$ direction is north. The linear momenta for the two $m = 2.0$ kg parts are then

$$\vec{p}_1 = m\vec{v}_1 = mv_1 \hat{j}$$

where $v_1 = 3.0$ m/s, and

$$\vec{p}_2 = m\vec{v}_2 = m(v_{2x} \hat{i} + v_{2y} \hat{j}) = mv_2(\cos\theta \hat{i} + \sin\theta \hat{j})$$

where $v_2 = 5.0$ m/s and $\theta = 30^\circ$. The combined linear momentum of both parts is then

$$\begin{aligned}\vec{P} &= \vec{p}_1 + \vec{p}_2 = mv_1 \hat{j} + mv_2(\cos\theta \hat{i} + \sin\theta \hat{j}) = (mv_2 \cos\theta) \hat{i} + (mv_1 + mv_2 \sin\theta) \hat{j} \\ &= (2.0 \text{ kg})(5.0 \text{ m/s})(\cos 30^\circ) \hat{i} + (2.0 \text{ kg})(3.0 \text{ m/s} + (5.0 \text{ m/s})(\sin 30^\circ)) \hat{j} \\ &= (8.66 \hat{i} + 11 \hat{j}) \text{ kg} \cdot \text{m/s}.\end{aligned}$$

From conservation of linear momentum we know that this is also the linear momentum of the whole kit before it splits. Thus the speed of the 4.0-kg kit is

$$v = \frac{P}{M} = \frac{\sqrt{P_x^2 + P_y^2}}{M} = \frac{\sqrt{(8.66 \text{ kg} \cdot \text{m/s})^2 + (11 \text{ kg} \cdot \text{m/s})^2}}{4.0 \text{ kg}} = 3.5 \text{ m/s}.$$

50. A 5.20g bullet moving at 672 m/s strikes a 700g wooden block at rest on a frictionless surface. The bullet emerges, traveling in the same direction with its speed reduced to 428 m/s.

a) What is the resulting speed of the block?

b) What is the speed of the bullet-block center of mass?

50. (a) We choose $+x$ along the initial direction of motion and apply momentum conservation:

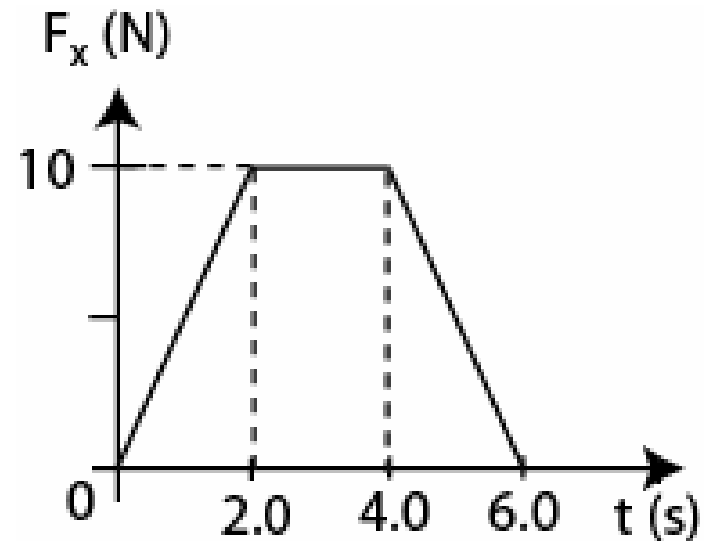
$$m_{\text{bullet}} \vec{v}_i = m_{\text{bullet}} \vec{v}_1 + m_{\text{block}} \vec{v}_2$$
$$(5.2 \text{ g})(672 \text{ m/s}) = (5.2 \text{ g})(428 \text{ m/s}) + (700 \text{ g})\vec{v}_2$$

which yields $v_2 = 1.81 \text{ m/s}$.

(b) It is a consequence of momentum conservation that the velocity of the center of mass is unchanged by the collision. We choose to evaluate it before the collision:

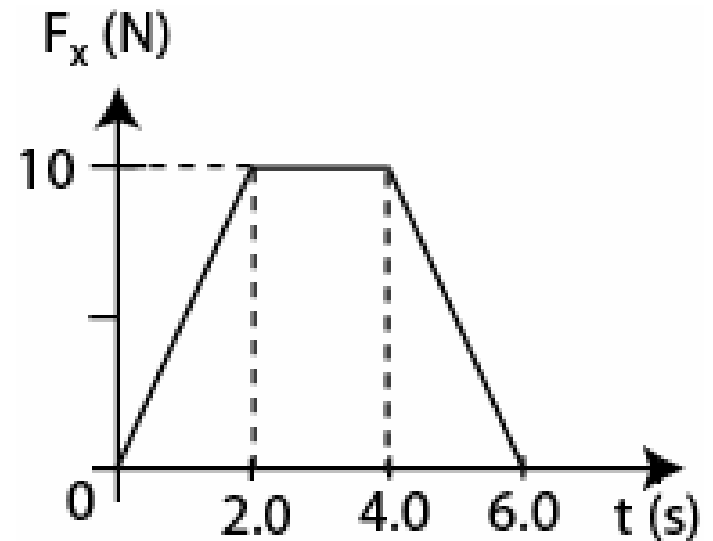
$$\vec{v}_{\text{com}} = \frac{m_{\text{bullet}} \vec{v}_i}{m_{\text{bullet}} + m_{\text{block}}} = \frac{(5.2 \text{ g})(672 \text{ m/s})}{5.2 \text{ g} + 700 \text{ g}} = 4.96 \text{ m/s}.$$

A 10.0 kg toy car is moving along the x axis. The only force F_x acting on the car is shown in Fig. 5 as a function of time (t). At time $t = 0$ s the car has a speed of 4.0 m/s. What is its speed at time $t = 6.0$ s? (Ans: 8.0 m/s)



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$$\begin{aligned}\vec{F} &= \frac{d\vec{p}}{dt} \Rightarrow |\vec{p}| = \int \vec{F} dt = \text{Area under the curve} \\ &= \frac{10 \times (6 + 2)}{2} = 40 \\ \therefore |\vec{p}| &= m (v_f - v_i) \\ \therefore v_f &= \frac{|\vec{p}|}{m} + v_i = \frac{40}{10} + 4 = \underline{8 \text{ m/s}}\end{aligned}$$

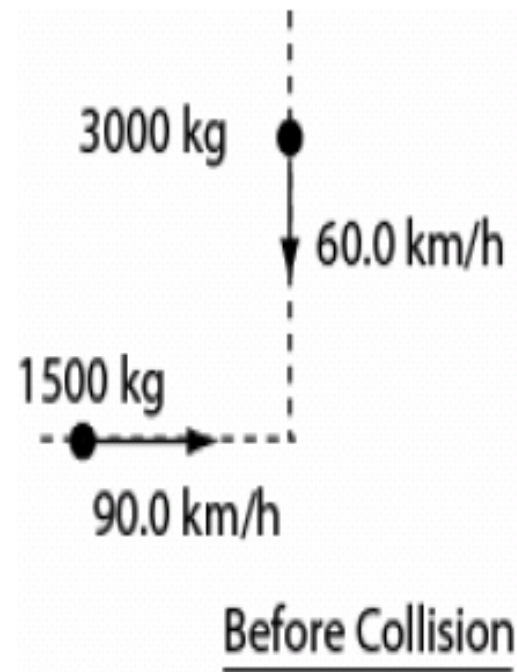


A 0.20 kg steel ball, travels along the x-axis at 10 m/s, undergoes an elastic collision with a 0.50 kg steel ball traveling along the y-axis at 4.0 m/s. The total kinetic energy of the two balls after collision is:

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$$\begin{aligned}\frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2 &= \frac{1}{2} \times 0.2 \times 10^2 + \frac{1}{2} \times 0.5 \times 4^2 = 10 + 4 \\ &= 14 \text{ J.}\end{aligned}$$

A 1500 kg car traveling at 90.0 km/h east collides with a 3000 kg car traveling at 60.0 km/h south. The two cars stick together after the collision (see Fig 2). What is the speed of the cars after collision?

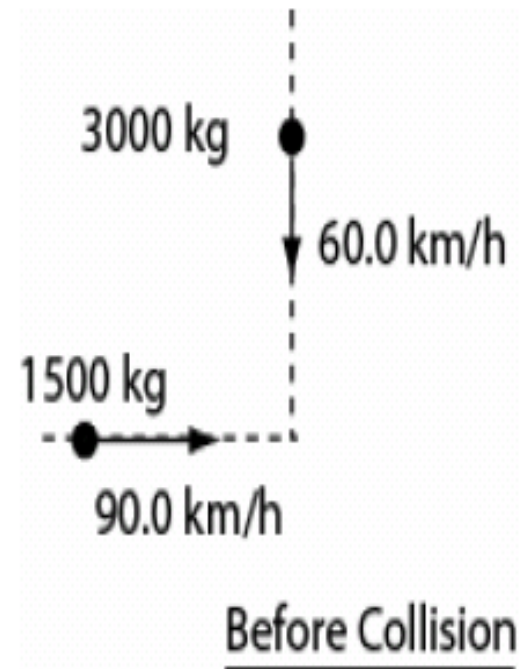


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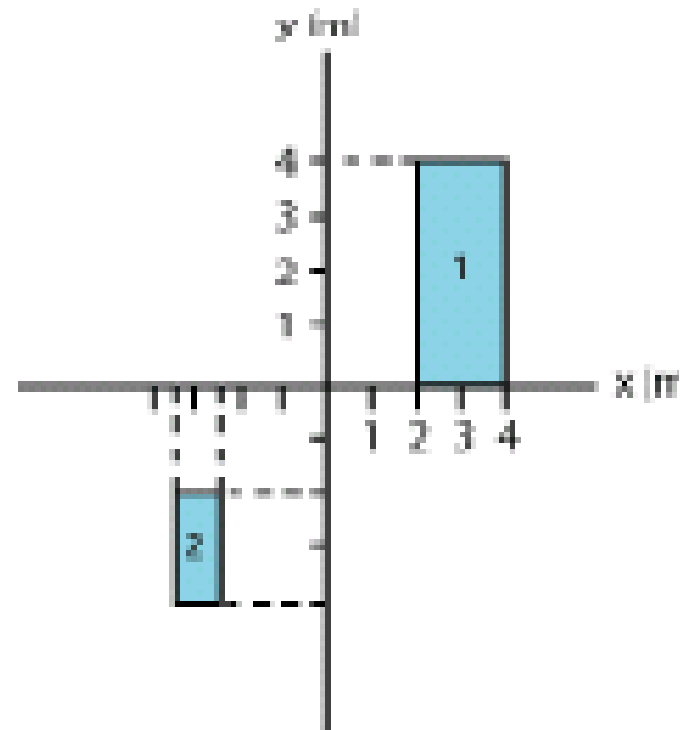
$$M \vec{v} = m_1 \vec{v}_1 + m_2 \vec{v}_2$$

$$(1500 + 3000) \vec{v} = 1500 \times 90 \hat{i} - 3000 \times 60 \hat{j}$$

$$\Rightarrow |\vec{v}| = \sqrt{(30^2 + 40^2)} = 50 \frac{\text{km}}{\text{hour}} = 13.9 \underline{\text{m/s}}$$



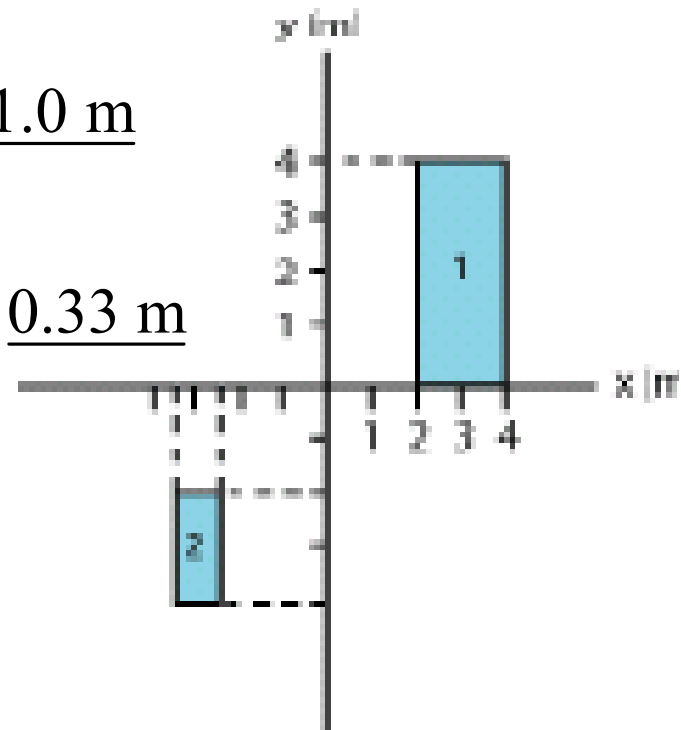
The location of two thin flat objects of masses $m_1 = 4.0$ kg and $m_2 = 2.0$ kg are shown in the figure, where the units are in m. The x and y coordinates of the center of mass of this system are:



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$$x_{cm} = \frac{m_1 x_1 + m_2 x_2}{m_1 + m_2} = \frac{4.0 \times 3.0 + 2.0 \times (-3.0)}{6.0} = \underline{1.0 \text{ m}}$$

$$y_{cm} = \frac{m_1 y_1 + m_2 y_2}{m_1 + m_2} = \frac{4.0 \times 2.0 + 2.0 \times (-3.0)}{6.0} = \underline{0.33 \text{ m}}$$



A 2.00 kg pistol is loaded with a bullet of mass 3.00 g. The pistol fires the bullet at a speed of 400 m/s. The recoil speed of the pistol when the bullet was fired is: (Ans: 0.600 m/s)

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$$0 = m_1 \vec{v}_1 + m_2 \vec{v}_2$$

$$0 = 2 \times \vec{v} + 0.003 \times 400 \Rightarrow |\vec{v}| = 0.6 \frac{\text{m}}{\text{s}}.$$

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$$v_{Bf} = \frac{2m_A}{m_A + m_B} v_{1i} + \frac{m_A - m_B}{m_A + m_B} v_{2i}$$
$$\Rightarrow v_{Bf} = \frac{2M}{3M + M} (10) + \frac{3M - 2M}{3M + 1M} (0) = \underline{5}$$

An object of 12.0 kg at rest explodes into two pieces of masses 4.00 kg and 8.00 kg. The velocity of the 8.00 kg mass is 6.00 m/s in the +ve x-direction. The change in the kinetic is:

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$$M\vec{v} = m_4\vec{v}_4 + m_8\vec{v}_8 \Rightarrow 0 = 4 \times \vec{v}_4 + 8 \times 6\hat{i} \Rightarrow \vec{v}_4 = -12\hat{i},$$

$$\begin{aligned} \Delta K &= K_f - \cancel{K_i} = \frac{1}{2}m_4(\vec{v}_4)^2 + \frac{1}{2}m_8(\vec{v}_8)^2 = \frac{4}{2}(12)^2 + \frac{8}{2}(6)^2 \\ &= \underline{432 \text{ J}} \end{aligned}$$

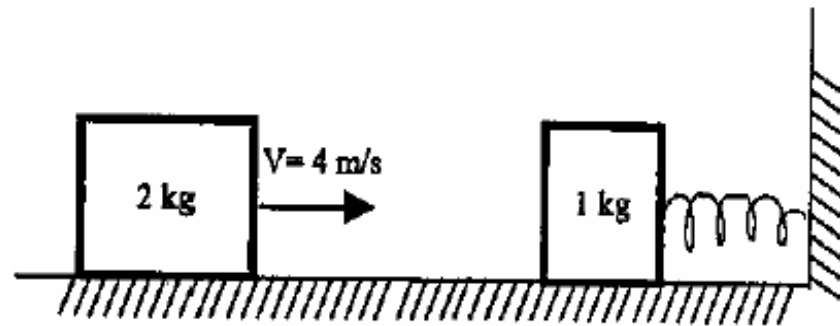
A 6.0 kg body moving with velocity v breaks up (explodes) into two equal masses. One mass travels east at 3.0 m/s and the other mass travels north at 2.0 m/s. The speed v of the 6.0 kg mass is:

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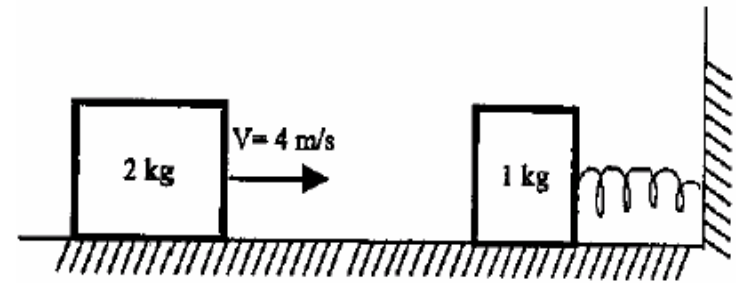
$$M \vec{v} = m_1 \vec{v}_1 + m_2 \vec{v}_2$$

$$6\vec{v} = 3 \times 3 \hat{i} + 3 \times 2 \hat{j} \quad \Rightarrow \quad |\vec{v}| = \sqrt{\frac{1}{6} (3^2 + 4^2)} = 1.8 \frac{\text{m}}{\text{s}}$$

A 1.0-kg block at rest on a horizontal frictionless surface is connected to a spring ($k = 200 \text{ N/m}$) whose other end is fixed (see figure). A 2.0-kg block moving at 4.0 m/s collides with the 1.0-kg block. If the two blocks stick together after the one-dimensional collision, what maximum compression of the spring does occur when the blocks momentarily stop?



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Conservation of momentum $\Rightarrow m v = (m + M)V$

$$\Rightarrow V = \frac{2 \times 4}{(2 + 1)} \approx 2.67 \frac{\text{m}}{\text{s}}$$

Conservation of K.E. after collision $\Rightarrow \frac{1}{2}(m + M)V^2 = \frac{1}{2}k x^2$

$$\Rightarrow x = V \sqrt{\frac{(m + M)}{k}} = 2.67 \sqrt{\frac{3}{200}} = \underline{0.33 \text{ m}}$$

A 10 gram bullet is shot in the +x-direction with a speed of $v_0 = 500$ m/s into a stationary block of wood that has a mass of 5.0 kg (see Fig 3). The bullet embeds itself in the block. What distance (d) will the block slide on a surface having a coefficient of kinetic friction equal to 0.5?

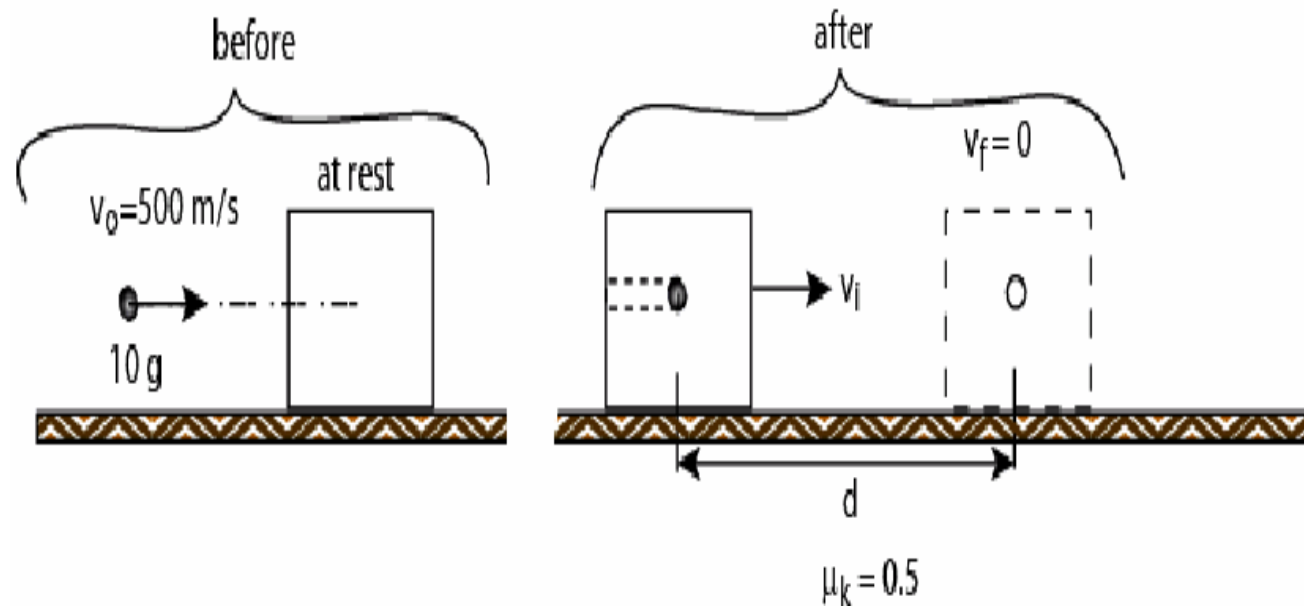


FIGURE 2

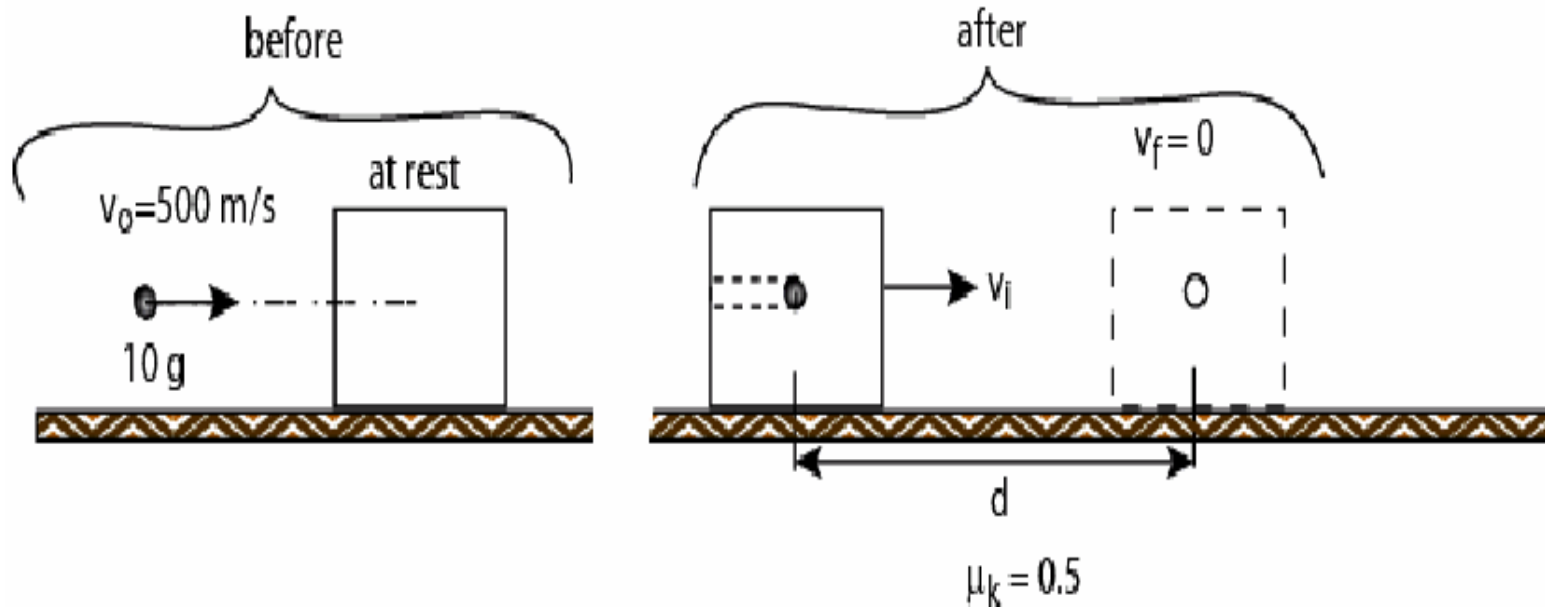


Figure 2

Conservation of momentum $\Rightarrow m v = (m + M) V$

$$\Rightarrow V = \frac{.001 \times 500}{(5.0 + 0.001)} \approx 1.0 \text{ m/s}$$

Change in K.E. after collision $\Rightarrow -\frac{1}{2}(m + M) V^2 = -\mu(m + M) g d$

$$\Rightarrow d = \frac{V^2}{2\mu g} = \frac{1.0^2}{2 \times 0.5 \times 9.8} = \underline{0.1 \text{ m}}$$