

Exam 1-932

Problem 1 (10 points)

Assuming the density of nitrogen gas,  $\rho$ , in a container that measures  $1.0\text{ m} \times 2.0\text{ m} \times 4.0\text{ m}$  is  $1/800$  that of water, and  $\rho$  (water) =  $1.0\text{ g/cm}^3$ .

- a) What is the mass of nitrogen gas in the above container?
- b) Find the number of nitrogen molecules in this container given that the molecular weight of nitrogen  $M = 28\text{ g}$   $N_A = 6.02 \times 10^{23}$  molecules/mole.

Problem 2 (10 points)

Energy is a physical quantity with dimensions equal to the dimension of mass multiplied by the dimensions of the square of velocity. Suppose the energy,  $E$ , of an object is given by:  
 $E = c m^j v^k + m g k y^n$   
where  $m$ ,  $v$ , and  $y$  are mass, velocity, and relative position of the object,  $g$  is the acceleration due to gravity,  $c$  is a dimensionless constant, and  $j$ ,  $k$ , and  $n$  are constant numbers.

- a) Use dimensional analysis to find numerical values for the constants  $j$ ,  $k$ , and  $n$ .
- b) What are the units of energy in SI system?

Problem 3 (10 points)

Two displacement vectors,  $\mathbf{a}$  has a length of  $20\text{ m}$  and makes an angle of  $\theta_a = 60^\circ$  with respect to the **negative y-axis (counterclockwise)** and  $\mathbf{b} = (40\mathbf{i} - 32\mathbf{j})\text{ m}$ .

- a) What are the magnitude and direction of the vector  $(2\mathbf{a} - \mathbf{b})$ ?
- b) What is the angle between the two vectors  $\mathbf{a}$  and  $\mathbf{b}$ ?

Problem 4 (10 points)

An object is released from rest from an unknown height  $h$  above the ground. It requires  $2.0\text{ s}$  to travel the last  $50\text{ m}$  just before hitting the ground.

- a) Find the speed when the object is  $50\text{ m}$  above the ground.
- b) Calculate the height  $h$  above the ground.
- c) What are the magnitudes of the average velocity and the average acceleration of the object during the last  $50\text{ m}$  of the trip just before hitting the ground?

Problem 5 (10 points)

A projectile is fired at an angle of  $30^\circ$  to a horizontal ground. The total flight time is  $10\text{ s}$  as it returns to the ground.

- a) Find the initial speed,  $v_0$ , of the projectile.
- b) Find the maximum height,  $H$ , reached by the projectile.
- c) Find the range (the maximum horizontal distance),  $R$ , traveled by the projectile.

Problem 6 (10 points)

A ball is thrown from the ground at an angle of  $45^\circ$  to the horizontal with an initial speed,  $v_0$ , of  $15.5\text{ m/s}$ . At the same moment a man runs from the opposite side to catch the ball in the air. He catches the ball at a height of  $1.0\text{ m}$  above the ground as it descends.

- a) Find the speed of the man if he runs at a constant speed for a distance of  $6.0\text{ m}$  before catching the ball.
- b) Find the speed of the ball at the highest point.
- c) What is the relative speed of the ball relative to the running man when the ball is at the highest point?

Problem 7 (10 points)

A boat can move at  $8.0\text{ m/s}$  in still water. The boat takes  $4\text{ minutes}$  to complete a round trip of distance  $2d$  along a river where the speed of the current is  $2\text{ m/s}$ .

- a) Find the distance  $d$ .
- b) How long does it take to complete the same round trip if the river is calm (still)?

**Problem 8** (10 points)

A block of mass  $m$  is kicked up a  $30^\circ$  rough inclined plane with an initial speed of  $6.0 \text{ m/s}$ . The block slides a distance of  $2.0 \text{ m}$  up the incline before coming to rest.

- a) Draw a free body diagram showing all the forces applied on the object as it is moving up the inclined plane.
- b) Find the acceleration of the block.
- c) Find the coefficient of kinetic friction between the block and the plane.

**Problem 9** (10 points)

string and hung vertically over a light, frictionless pulley. Assume the two masses,  $m_1 = 1.00 \text{ kg}$  and  $m_2 = 1.11 \text{ kg}$ .

- a) Draw free body diagrams of the two masses,  $m_1$  and  $m_2$ .
- b) Find the acceleration of the masses.
- c) Find the tension in the string.