

Chapter 30 - Faraday's and Lenz's Laws

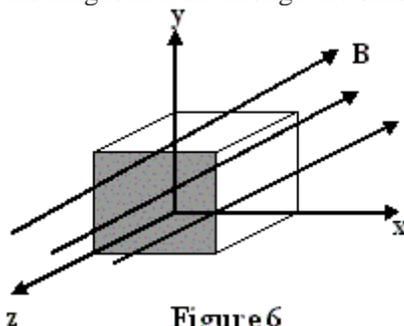
Faraday's Law of Induction

Q1. Consider a circular loop of radius $R = 20$ cm lying in the x - y plane. There is throughout the region a uniform magnetic field given by: $\vec{B} = (5.0\hat{i} + 4.0\hat{j} + 3.0\hat{k})$ T.

Calculate the magnetic flux through the loop. Ans: 0.38 Tm^2

Q2. A uniform magnetic field $\vec{B} = (2.0\hat{i} + 4.0\hat{j} + 5.0\hat{k})$ T intersects a circular surface of radius 2 cm lying in the yz plane. What is the magnetic flux through this surface? Ans: $2.5 \times 10^{-3} \text{ Tm}^2$

Q3. Consider a cube of side $L = 10$ cm positioned as shown in Figure 6. Throughout the region, There is a magnetic field $\vec{B} = (4.0\hat{i} + 5.0\hat{j} - 6.0\hat{k})$ T. Calculate the magnetic flux through the shaded face of the cube. Ans: -0.06 Tm^2



Q4. A constant magnetic flux of 4.0×10^{-5} Wb is maintained through a coil for 0.5 s. What emf is induced in the coil by this flux during that period? Ans: Zero.

Q5. A 2.0 Tesla uniform magnetic field makes an angle of 60 degrees with the xy -plane. The magnetic flux through an area of 3 m^2 portion of the xy -plane is: Ans: 5.2 Wb .

Q6. Figure 12 shows a conducting loop consisting of a half circle of radius 0.20 m and three straight sections. The loop lies in a uniform magnetic field that is directed as shown in the figure and is given by: $B = 4.5t^2 - 10t$, with B in tesla and t in seconds. What is the magnitude of the induced emf at $t = 10$ s? Ans: 8.2 V

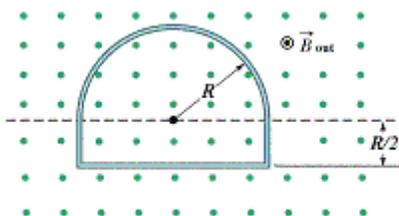


Figure 12

Q7. A 400-turn coil of total resistance 6.0 ohm has a cross sectional area of 30 cm^2 . How rapidly should a magnetic field parallel to the coil axis change in order to induce a current of 0.3 A in the coil? Ans: 1.5 T/s .

Q8. A circular wire loop of area 0.5 m^2 is perpendicular to a magnetic field of 0.8 T. If the coil is removed completely from the field in 0.1 s, the average emf induced in the loop has a magnitude: Ans: 4.0 V .

Lenz's Law

Q9. A plane loop of wire consisting of a single turn of cross-sectional area 0.20 m^2 is perpendicular to a magnetic field that increases uniformly in magnitude from 0.25 T to 3.25 T in a time of 2.0 s. What is the resistance of the coil if the induced current has a value of 2.0 A? Ans: 0.15 Ohm .

Q10. Each turn of a 100-turn coil, whose resistance is 60 Ohm, encloses an area of 80 cm^2 . What should be the rate of change of a magnetic field parallel to its axes in order to induce a current of 1 mA in the coil? Ans: 0.075 T/s .

Q11. A flat coil of wire consisting of 20 turns, each with an area of 50 cm^2 , is positioned perpendicularly to a uniform magnetic field that increases its magnitude at a constant rate from 2.0 T to 6.0 T in 2.0 s. If the coil has a total resistance of 0.4 ohms, what is the magnitude of the induced current in the coil? Ans: 0.5 A

Q12. The square circuit shown in Figure 8 is in a uniform magnetic field directed into the page and is decreasing at a rate of 1.5 T/s . Calculate the induced current in the circuit if the resistance of the wire 10 ohms. Ans: 2.16 milli-A

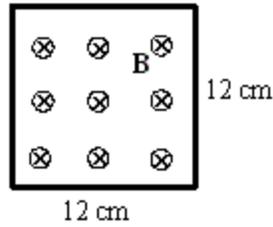


Figure 8

Induction and Energy Transfers

Q13. In the arrangement shown in Figure (7), a conducting bar moves to the right. Assume $R=10\ \Omega$, $L=0.5\ \text{m}$, and that a uniform $3.5\ \text{T}$ magnetic field is directed into the page. Neglect the mass of the bar, find the power dissipated in the resistor such that the bar moves to the right with a constant speed of $4.0\ \text{m/s}$? Ans: $4.9\ \text{W}$.

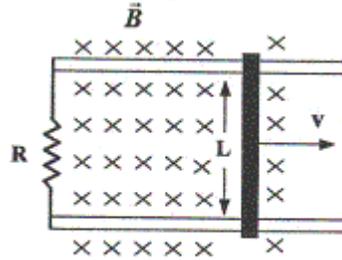


Figure # 7

Q14. A conducting rod of length $1.2\ \text{m}$ is moving with a speed of $10\ \text{m/s}$ as shown in Figure 9. If the magnetic field is $0.55\ \text{T}$ into the page, calculate the potential difference between the ends of the rod. Ans: $6.6\ \text{V}$

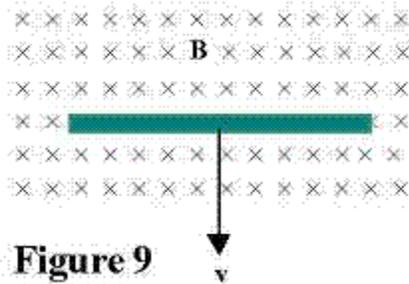


Figure 9

Q15. Figure 7 shows a conducting bar moving with a constant speed of $5.0\ \text{m/s}$ to the right. Assume that $R = 5.0\ \Omega$, $L = 0.20\ \text{m}$, and that a uniform magnetic field of $3.5\ \text{T}$ is directed into the page. Calculate the magnitude of the applied force pulling the bar. (Neglect the mass of the bar.) Ans: $0.49\ \text{N}$

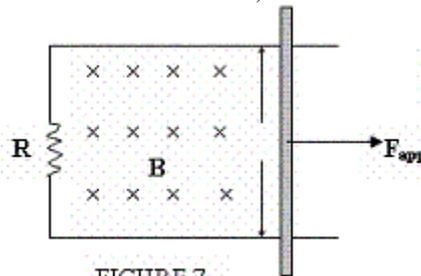


FIGURE 7

Q16. The square coil shown in figure 12 is $20\ \text{cm}$ on a side and has 15 turns of wire on it. It is moving to the right at $2\ \text{m/s}$. Find the induced emf in it at the instant shown, and the direction of the induced current in the coil. (The magnetic field is $0.2\ \text{T}$ and its direction is out of the page.) Ans: $1.2\ \text{V}$, clockwise

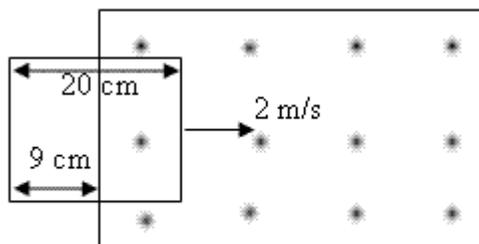


Figure 12