

# DC Conductivity studies of Sr-V-B glasses

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# OUTLINE

- Amorphous materials
- Desirability for Magnetization & XPS Studies
- XPS & Magnetization Results of Sr-V-borate glasses
- Desirability for DC conductivity studies
- Description of the proposed research
- Theory
- Conclusion/Expectations

## Amorphous materials

- **Without form/no periodicity**
- **Not-crystalline**
- **Have short range order rather than long range order**

Glass form a particular class of amorphous materials

## Types of glasses

- Metallic glasses/spin glasses (CuMn, FeMn)
- Semiconducting glasses ( $\text{As}_2\text{Te}_3$ )
- Insulating glasses (oxide glasses) but TM oxide glasses are Semicond.

Oxide glasses have technological applications such as:

- Optical fibers (Si, Ge)
- Ionic conductors (Alkali-Si or Alkali-Ge)
- Semiconductors (Fe-B, Cu-Si, V-Ge)
- Glass Ceramics (Mg-Al-Si, Mg-P-Si)

## Methods of preparation

- Cooling from the melt
- Condensation from vapor
- Pressure quenching
- Solution hydrolysis
- Anodization
- Bombardment of crystals by high-energy particles or by shock waves

## Role of different oxides in glasses

- $\text{SiO}_2$ ,  $\text{P}_2\text{O}_5$ ,  $\text{GeO}_2$ ,  $\text{B}_2\text{O}_3$  are called **network formers** (these oxides readily form a glass)
- $\text{Al}_2\text{O}_3$ ,  $\text{TiO}_2$ ,  $\text{MgO}$  are called **intermediate** (can substitute for network formers but do not form glasses on their own)
- $\text{Na}_2\text{O}$ ,  $\text{LiO}_2$ ,  $\text{K}_2\text{O}$  are called **network modifiers** (disrupt the glass network)

# Techniques used

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- XPS (Previous project)
- Magnetization (previous project)
- DC conductivity (New project as a continuation of the previous work)



# Objectives (Previous Project)

- (i) Investigate the magnetic properties of V ions in Sr-V-borate glasses.**
- (ii) Find the redox state(s) of V ions using both XPS and magnetic measurements.**
- (iii) Study the structural role of V & Sr in these materials**
- (iv) Study electrical conductivity to further understand the mechanism of electrical properties. (New Project)**

# Glass systems investigated



# Experimental details

## Sample preparation

Stoichiometric amounts of  $V_2O_5$ , SrO and  $B_2O_3$  were melted in Alumina crucibles at  $\sim 1100$  °C for two hours.

**Chemical composition was determined by ICP.**

## Magnetic data

M vs. T data were recorded using a SQUID magnetometer in a magnetic field of 5000 Oe over a temperature range of 5 K to 300 K. Accuracy  $\sim \pm 3\%$ .

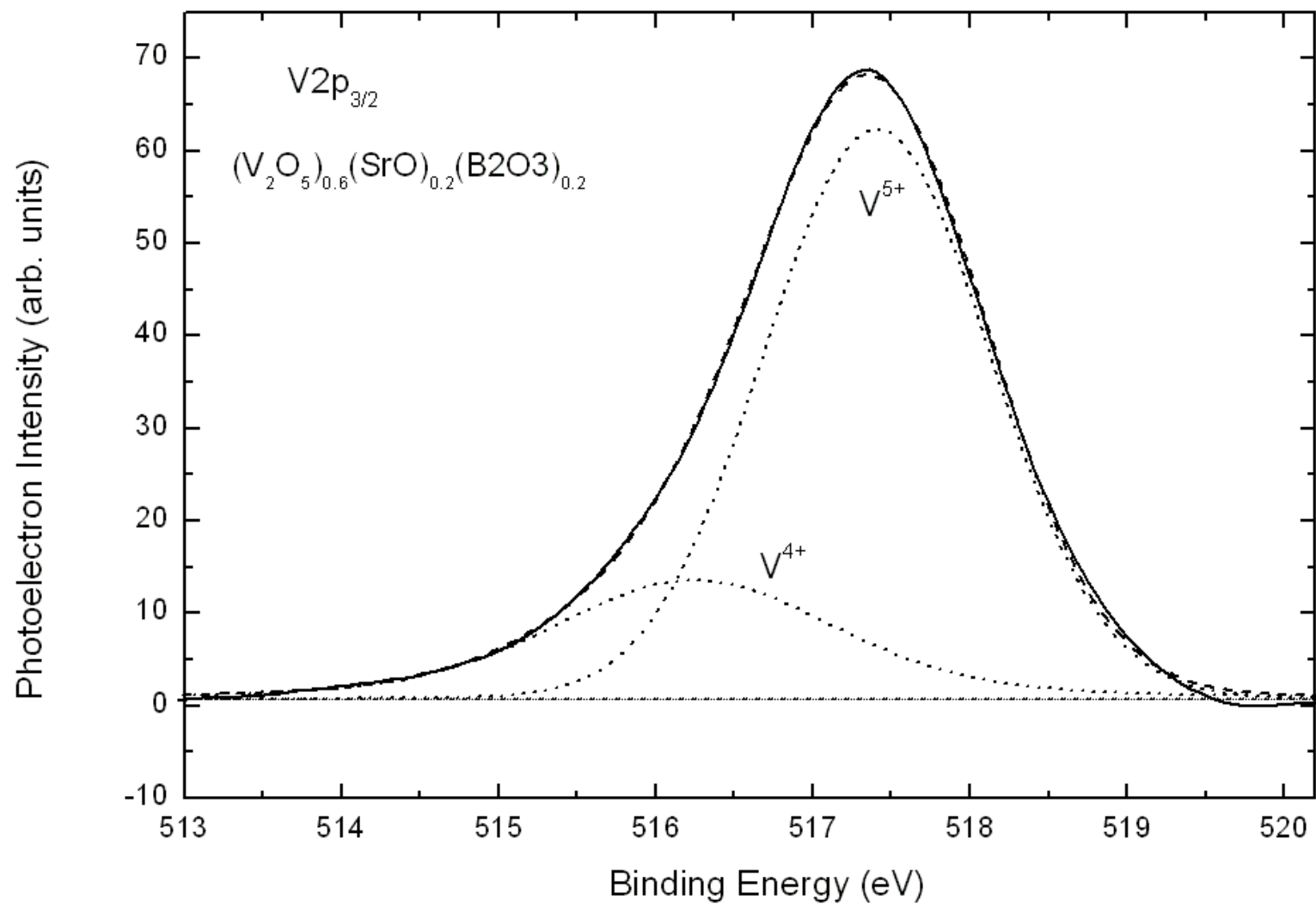
## XPS measurements

High resolution V 2p, O 1s, Sr 3p, and B 1s core level spectra were obtained Using an Al  $K\alpha$  X-ray source on a VG ESCALAB Mk II. Glass rods were Fractured in UHV ( $\sim 10^{-10}$  mbar). The C 1s was a reference level. Accuracy in the quantitative analysis  $\sim \pm 5\%$ .

- Sr 3p spectra have the same B.E. for all samples.
- Shifted by 0.6 eV towards higher B.E. in comparison to their values in SrO powder.
- This shift arises from a change in the molecular environment.

# V 2p spectra

- V  $2p_{3/2}$  spectra for the glass samples are sufficiently broaden such that two peaks are fitted to the data.
- These peaks are associated with the presence of  $V^{5+}$  and  $V^{4+}$  and the relative area under each peak reflects the relative amount of each ion.
- More than 90% of the V is found to be in the  $V^{5+}$  state in these glass samples.



## O 1s spectra

- V-O-V, V-O-B, B-O-B: bridging oxygen (BO)
- V-O-Sr, Sr-O-Sr, V = O non-bridging oxygen



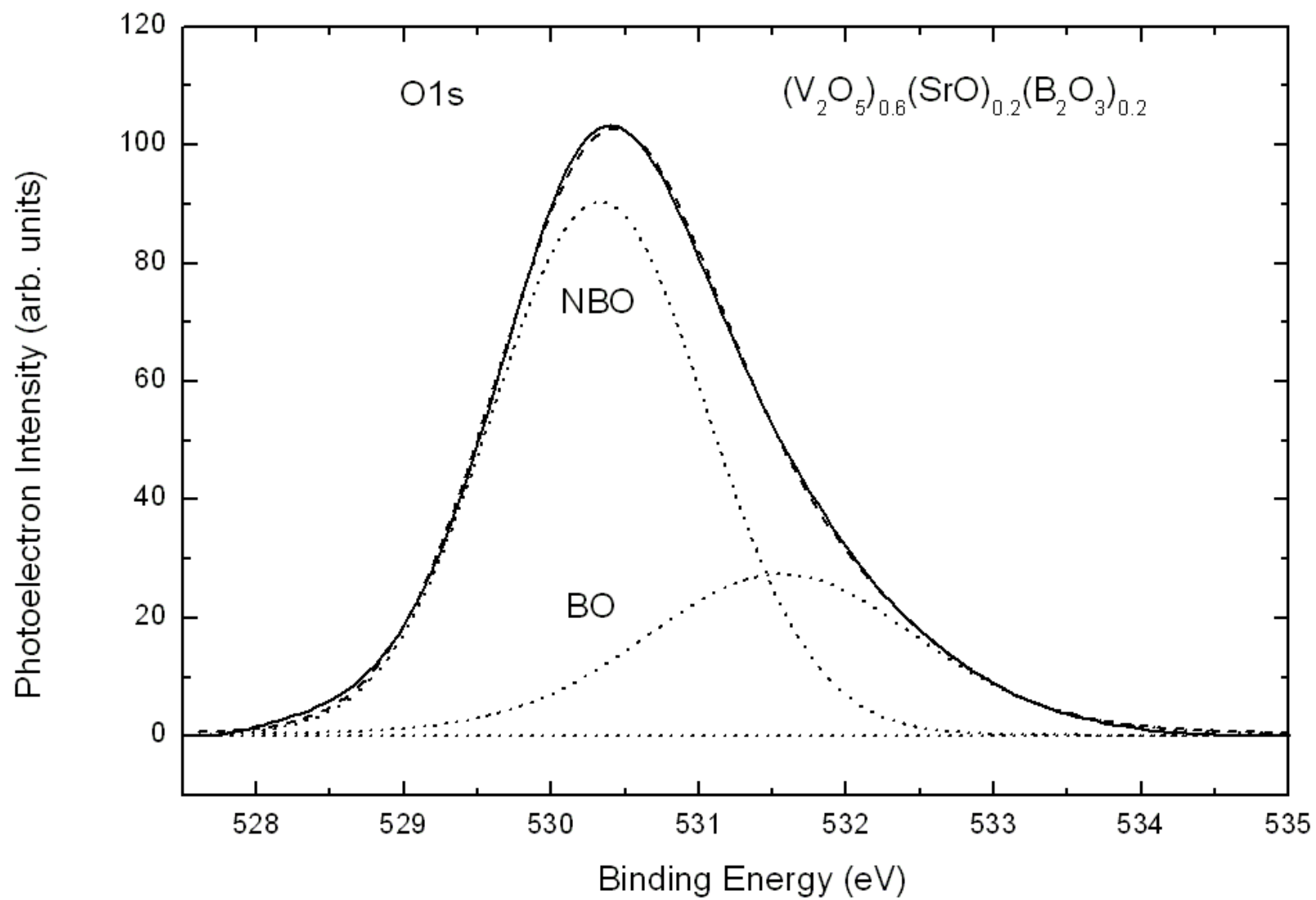
- $NBO/TO = (4x+2y)/(5x+y+3z)$
- NBO/TO 57-85%

■ Good agreement between calculated and measured.

# NBO/Total

Series	z ,y ,x	$(0.030\pm)_{\text{total}} \text{O/NBO}$ *[1Equation ]
I	= x0.2	*0.857 0.851
	0.3 =x	*0.895 0.844
	0.4 =x	*0.941 1.000
	0.5 =x	*1.000 1.000
II	0.1 =y	0.875 0.810
	0.2 =y	0.765 0.792
	0.3 =y	0.667 0.612
	0.4 =y	0.579 0.536
III	0.4 =z	0.588 0.572
	0.5 =z	0.667 0.612
	0.6 =z	0.737 0.731
	0.7 =z	0.780 0.771
	0.8 =z	0.857 851..0





# Magnetization Data

**The Temperature independent term from two contributions:**

- i) Diamagnetic from core ions in the glass matrix
- ii) Temperature-independent paramagnetic contribution from  $V_2O_5$  ( $\sim 5 \times 10^{-7} \text{ emu/Oe g } V_2O_5$ )

**The temperature-independent term can be either positive or negative depending on the relative size of these two contributions**

- In these glasses it is positive as  $V_2O_5$  contribution dominates
- In V-Na-Silicate glasses the diamagnetic contribution dominates so the term  $(M/H)$  background is negative
- $V_2O_5$  contribution increases with an increase in the  $V_2O_5$  content

# Magnetization Data

## Curie-Weiss formula is adequate:

Magnetic ions appear to be interacting

Still in the low field limit ( $\mu H \ll kT$ )

$$M/H = C/(T-\theta)$$

## Analysis based on three fitting parameters

$M/H = (M/H)_{\text{background}} + C/(T-\theta)$ ;  $M/H$  vs  $T$  will give  $(M/H)_{\text{background}}$

$$M^*/H = M/H - (M/H)_{\text{background}} = C/(T-\theta)$$

$H/M^*$  vs  $T$ , least square fitting gives  $C$  &  $\theta$

## Finally we use the three fitting parameters in the

$M/H = (M/H)_{\text{background}} + C/(T-\theta)$  equation and compare the fit to the measured  $M/H$ .

$(M/H)_{\text{background}}$  is positive,  $\theta$  values negative, antiferromagnetic interactions between the  $V^{4+}$  ions.

# Magnetization Results

TABLE Compositions and magnetic characterization parameters for the vanadate glasses.

	Batch	Actual			$(M/H)_{const}$ $\left(\frac{10^{-7} \text{ emu}}{\text{g Oe}}\right)$	$C$ $\left(\frac{10^{-4} \text{ emu K}}{\text{g Oe}}\right)$	$\theta$ (K)	$V^{4+}/V$
		$V_2O_5$	SrO	$B_2O_3$				
$(SrO)_x(V_2O_5)_{1-x}$	x = 0.5	0.488	0.511	-	0.700	0.533	-0.91	0.0206
	x = 0.4	0.591	0.409	-	1.17	0.700	0.03	0.0236
	x = 0.3	0.692	0.308	-	1.55	0.955	-0.05	0.0289
	x = 0.2	0.792	0.208	-	2.00	1.54	-2.85	0.0427
$(V_2O_5)_{0.5}(SrO)_{0.5-y}(B_2O_3)_y$	y = 0.1	0.498	0.415	0.087	0.670	0.603	-0.07	0.0225
	y = 0.2	0.483	0.299	0.218	0.630	0.731	0.42	0.0270
	y = 0.3 <sup>a</sup>	0.516	0.214	0.270	0.850	1.41	-1.38	0.0489
	y = 0.3 <sup>b</sup>	0.486	0.192	0.322	2.00	0.771	-5.65	0.0276
	y = 0.4	0.539	0.112	0.347	1.76	0.617	-7.41	0.0204
$(V_2O_5)_z(SrO)_{0.2}(B_2O_3)_{0.8-z}$	z = 0.4	0.434	0.220	0.346	0.950	0.734	-1.88	0.0283
	z = 0.5 <sup>b</sup>	0.486	0.192	0.322	2.00	0.771	-5.65	0.0276
	z = 0.5 <sup>a</sup>	0.516	0.214	0.270	0.850	1.41	-1.38	0.0489
	z = 0.6	0.613	0.209	0.178	2.00	3.24	-2.64	0.1007
	z = 0.7	0.701	0.209	0.091	1.67	2.47	-1.94	0.0721
	z = 0.8	0.792	0.208	0.000	2.00	1.54	-2.85	0.0427

<sup>a,b</sup> – Refers to two samples with the same nominal composition.

# Magnetization Results

1. The Ratio  $V^{4+}/V_{\text{total}}$  consistent with XPS findings
2. The negative values for  $\theta$  in the range of -0.2 - -4.2 K indicate a weak 2 antiferromagnetic interaction between the  $V^{4+}$  ions
3. These small values are not surprising since  $\theta$  is proportional to:
  - a) the # of neighboring magnetic ions (negligible for these low  $V^{4+}$  concentration)
  - b) as well as the strength of the magnetic interaction.

# DC electrical conductivity

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- Continuation of our previous work (XPS & Magnetization)
- To understand the nature of the mechanism of DC conductivity
- To develop a correlation between the composition, microstructure & DC conductivity in these glasses.

# DC conductivity

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- Two types of conductivities:
  - i) Ionic conductivity (higher temp. region)
  - ii) Electronic conductivity (lower temp. region)
- ionic conductivity is a thermally activated process: mobile ions jump from a potential well to the next due to thermal motion. The vibrating ions have a finite and equal probability of surrounding the potential barrier and moving to the adjacent pot.well.

# Ionic conductivity continued

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- Resistivity  $\rho$  is given by

$$\rho = \rho_0 \exp(W/K_B T)$$

$$\rho_0 = \text{constant} = 6K_B T / f s d^2 q^2 N$$

$f$  = frequency of the ions

$d$  = average distance between holes

$q$  = ionic charge,  $N$  = # mobile ions

$W$  = activation energy

$S$  = # of holes



# Example of ionic and electronic conduction

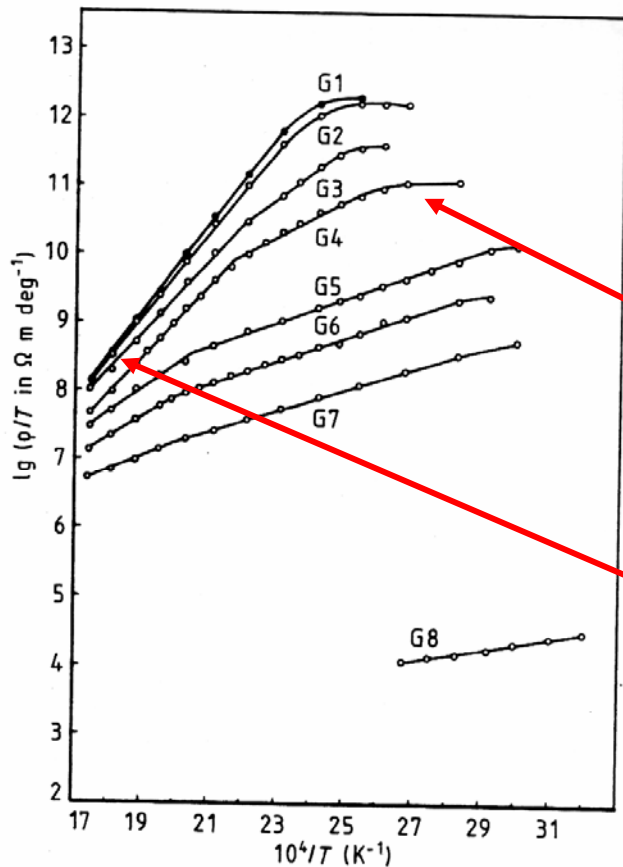


Figure 1. Resistivity-temperature dependence of glasses G1-G8.

Table 1. Compositions of the glasses studied (in mol%).

Glass No	G1	G2	G3	G4	G5	G6	G7	G8
Na <sub>2</sub> O	16	16	16	16	16	16	16	16
V <sub>2</sub> O <sub>5</sub>	—	2	4	5.5	7	8.5	10	14
B <sub>2</sub> O <sub>3</sub>	84	82	80	78.5	77	75.5	74	70

**electronic**

**ionic**

# Procedure

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- Disc- shaped samples
- Polished
- Evaporation of Gold electrodes
- Measure  $I$  vs  $V$  in the temperature range 293-473 K
- Analysis of the data will be carried out as follows

# DC conductivity

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- Electronic conduction by small polaron hopping process (through the hopping of an unpaired electrons from  $V^{4+}$  site to  $V^{5+}$  site..)
- Depends on the ratio of  $V^{4+}/V^{5+}$
- Analysis of the conductivity as follows:

# DC Electrical Conductivity Theory

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$$\sigma(T) = A(T) e^{-\beta W(T)}, \quad (1)$$

Where:

$W$  is the activation energy

$T$  is the temperature,

$\beta^{-1} = k_B T$ ,  $k_B$  is the Boltzmann constant,

and  $A(T)$  and  $W(T)$  are assumed to be slowly varying functions of the temperature. Usually analysis of the conduction curve by Arrhenius plot calculates the slope, or

$W'(T)/k_B^{-1}$  where

# DC conductivity continued

$$\cancel{W'(T) = -\partial \ln \sigma / \partial \beta} \quad (2)$$

$$= W(T) - \partial / \partial \beta \ln[A(T)] + \beta \partial / \partial \beta [W(T)] \quad (3)$$

$$= W$$

for A and W to be temperature independent, the slope should be constant, yielding directly the activation energy, W.

# DC conductivity continued

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- In general case,  $W'(T)$  does not permit  $A$  and  $W$  to be uniquely determined.
- Often, however, models of electrical transport place additional constraints on the functions  $A(T)$  and  $W(T)$ , and with these constraints we can determine both  $A(T)$  and  $W(T)$  from  $\sigma(T)$ . We illustrate this with two model examples.

# Model1-Variable range hopping

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- Assuming  $N(E) = N_0 (E-E_F)^p$ , Hamilton has shown that

$$\sigma(T) = \sigma(o) \exp(-BT^{-[(p+1)/(p+4)]}),$$

Where  $0 < p < \infty$  (5)

Equation (3) yields the function

$$W'(T) = Bk_B [(p+1)/(p+4)] T^{3/(p+4)}. \quad (6)$$

The constants B and p can be determined from the intercept and slope on a log W' versus log T plot.

# Brief explanation

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- Mott (1968): At low temperatures the most frequent hopping process would not be to a nearest neighbor.
- Within a range  $R$  of a given site the density of states per unit energy range is, near  $E_F$ ,  
$$(4\pi/3)R^3N(E_F)$$

The energy  $\Delta E = 1/[(4\pi/3)R^3N(E_F)]$



# continued

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- But hopping over a large distance involves tunneling and the probability will contain a factor  $\exp(-2\alpha R)$ ,  $1/\alpha$  =decay length of the localized wave function.
- There will be an optimum hopping distance  $R$ , for which  $\exp(-2\alpha R)\exp(-\Delta E /k_B T)$  is a maximum or  $2\alpha R + 1/(4\pi/3)R^3 N(E_F)$  is minimum ---->  $R = [1/8\pi N(E) \alpha k_B T]^4$

# Continued..

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- $\sigma(T) = A \exp(-B/T^n),$   
 $B = 2(3/2\pi)^{1/4}[\alpha^3/k_B N(E_F)]$

# Continued

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- As a check on the validity of this model, according to Mott the energy  $W'(T)$  must satisfy

$$W'(T) < 2^{p/(p+4)} K_B T. \quad (7)$$

# Model 2-Conduction by small polarons

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- Schnakenberg has analysed the hopping energy  $W$  of small polarons at temperatures above  $\Theta_D/4$ , where  $\Theta_D$  is the Debye temperature of the optical phonons of the solid, and he deduced the following high temperature relation:

$$W(T) = W_H [ \{ \tanh(\Theta_D/4T) / (\Theta_D/4T) \} ] + W_D/2 \quad (8)$$

# Continued

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- $W_D$  and  $W_H$  are two constants, called disorder energy and small polaron hopping energy, respectively.
- $W_D$  between the initial and final sites due to variations in the local distributions of the TM ions.
- $W_D = 0.09$  eV,  $W_H = 0.35$  eV
- Using Eqn.(3) again, we find
$$W'(T) = W_H \operatorname{sech}^2 (\Theta_D/4T) + W_D/2 \quad (9)$$

# Continued

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- $W_H$ ,  $W_D$  and  $\Theta_D$  are determined in two steps:
  - First we assume  $W_D = 0$ , and expand  $\text{sech}^2(\Theta_D/4T)$ . Eqn(9) becomes
$$W'(T) = W_H [1 - (\Theta_D/4T)^2 + \dots] \quad (10)$$
A plot of  $W'(T)$  vs  $T^{-2}$  yield a straight Line with intercept  $W_H$  and slope  $W_H(\Theta_D/4T)^2$   
 $\Theta_D$  is found here.

# Continued

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ii) The data is then replotted as  $W'$  versus  $\text{sech}^2(\Theta_D/4T)$  using  $\Theta_D$  values determined in the preceding step. A straight line should yield

Intercept =  $W_D/2$  and

Slope =  $W_H$

The hopping energy  $W(T)$  may then be determined using eq.(8).

# Expectations

✓ *We hope to achieve the following:*

*i) Dependence of  $\sigma(T)$  on  $V^{4+}/V_{\text{total}}$*

*ii) Dependence of  $\sigma(T)$  on  $BO/O_{\text{total}}$*

*iii)  $V_2O_5$  plays the role of a glass modifier or glass former and its concentration dependence.*



**Thank you**