

56. Since the force acts tangentially at $r = 0.10$ m, the angular acceleration (presumed positive) is

$$\alpha = \frac{\tau}{I} = \frac{Fr}{I} = \frac{(0.5t + 0.3t^2)(0.10)}{1.0 \times 10^{-3}} = 50t + 30t^2$$

in SI units (rad/s^2).

(a) At $t = 3$ s, the above expression becomes $\alpha = 420 \text{ rad/s}^2$.

(b) We integrate the above expression, noting that $\omega_o = 0$, to obtain the angular speed at $t = 3$ s:

$$\omega = \int_0^3 \alpha dt = (25t^2 + 10t^3) \Big|_0^3 = 5.0 \times 10^2 \text{ rad/s} .$$