

Review Problems

From

Chapter 10&11

1) At $t=0$, a disk has an angular velocity of 360 rev/min, and constant angular acceleration of -0.50 rad/s^2 . How many rotations does the disk make before coming to rest?

A1 226

A2 180

A3 360

A4 90

A5 113

$$\omega_0 = \frac{360 \times 2\pi}{60} = 120\pi \text{ rad/s}, \quad \alpha = -0.50 \text{ rad/s}^2, \quad \omega = 0$$

$$\omega = \omega_0 + \alpha t \Rightarrow t = \frac{-\omega_0}{\alpha} \Rightarrow \text{find } t$$

$$\theta = \omega t - \frac{1}{2}\alpha t^2 = -\frac{1}{2}\alpha t^2 \Rightarrow \text{find } \theta \text{ in rad/s}$$

divide by 2π to get θ in revolutions.

2) Two wheels A and B are identical. Wheel B is rotating with twice the angular velocity of wheel A. The ratio of the radial acceleration of a point on the rim of B (a_2) to the radial acceleration of a point on the rim of A (a_1) is (a_2/a_1) :

A1 4
A2 2
A3 1/2
A4 1/4
A5 1

$$\omega_B = 2\omega_A \Rightarrow \frac{\omega_B}{\omega_A} = 2$$

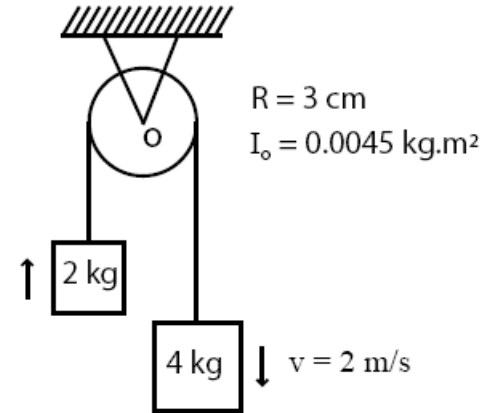
$$a_1 = \omega_A^2 R$$

$$a_2 = \omega_B^2 R$$

$$\frac{a_2}{a_1} = \frac{\omega_B^2 R}{\omega_A^2 R} = \left(\frac{\omega_B}{\omega_A} \right)^2 = 4$$

3) Fig shows a pulley ($R=3.0$ cm and $I_o= 0.0045$ kg*m**2) suspended from the ceiling. A rope passes over it with a 2.0 kg block attached to one end and a 4.0 kg block attached to the other. When the speed of the heavier block is 2.0 m/s the total kinetic energy of the pulley and blocks is :

- A1 22 J
- A2 10 J
- A3 2 J
- A4 16 J
- A5 38 J



Let's call the 2kg body 1, the 4 kg body 2 and the pulley p;

$v_p = v_1 = v_2 = 2$ m / s, v_p is the velocity of any point at the rim of the pulley.

$$\omega_p = \frac{v_p}{R} = \frac{2}{0.03} = 66.7 \text{ rad / s}$$

$$K_1 = \frac{1}{2} m_1 v_1^2 = \frac{1}{2} \times 2 \times 2^2 = 4 \text{ J}$$

$$K_2 = \frac{1}{2} m_2 v_2^2 = \frac{1}{2} \times 4 \times 2^2 = 8 \text{ J}$$

$$K_p = \frac{1}{2} I_o \omega_p^2 = \frac{1}{2} \times 0.0045 \times 66.7^2 = 10 \text{ J}$$

$$K = K_1 + K_2 + K_p = 4 + 8 + 10 = 22 \text{ J}$$

4) A uniform rod ($M = 2.0 \text{ kg}$, $L = 2.0 \text{ m}$) is held vertical about a pivot at point P, a distance $L/4$ from one end (as in the Figure). The rotational inertia of the rod about P is $1.17 \text{ kg}\cdot\text{m}^2$. If it starts rotating from rest, what is the linear speed of the lowest point of the rod as it passes again through the vertical position (v)?

- A1 8.7 m/s
- A2 4.8 m/s
- A3 17 m/s
- A4 2.4 m/s
- A5 zero

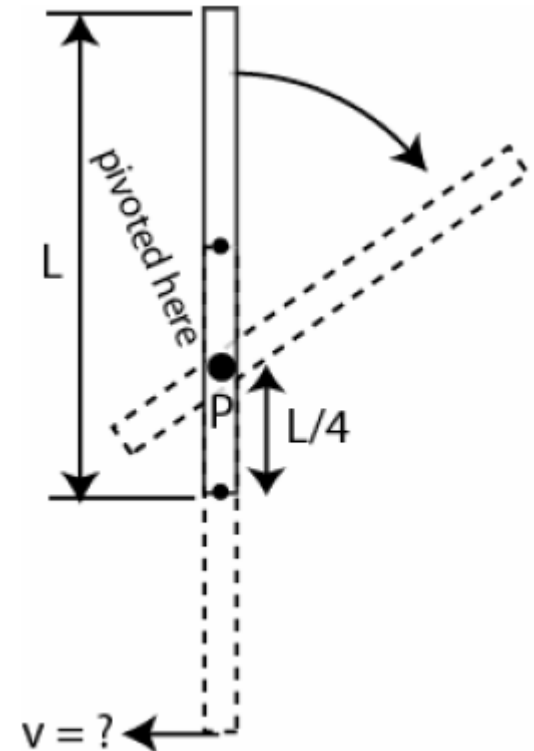
$$K_i = 0.0, \quad U_i = Mg\left(\frac{L}{4}\right) \quad (\text{taking our } U = 0.0 \text{ at the point P})$$

$$\Rightarrow E_i = K_i + U_i = Mg\left(\frac{L}{4}\right)$$

$$K_f = \frac{1}{2}I\omega^2, \quad U_f = -Mg\left(\frac{L}{4}\right) \quad \Rightarrow \quad E_f = K_f + U_f = \frac{1}{2}I\omega^2 - Mg\left(\frac{L}{4}\right)$$

$$\text{but } E_i = E_f \quad \Rightarrow \quad Mg\left(\frac{L}{4}\right) = \frac{1}{2}I\omega^2 - Mg\left(\frac{L}{4}\right)$$

$$\frac{1}{2}Mg(L) = \frac{1}{2}I\omega^2 \quad \Rightarrow \quad \omega = \sqrt{\frac{MgL}{I}} = \frac{v}{(3L/4)} \Rightarrow \text{find } v$$



5) A uniform solid sphere of radius 0.10 m rolls smoothly across a horizontal table at a speed 0.50 m/s with total kinetic energy 0.70 J. Find the mass of the sphere.

A1 4.0 kg $R = 0.10 \text{ m}, K = 0.70 \text{ J}$

A2 8.0 kg

A3 2.0 kg $K = \frac{1}{2} M v_{com}^2 + \frac{1}{2} I \omega^2$ (1)

A4 1.0 kg

A5 5.0 kg

sub. in (1) for $I = \frac{2}{5} MR^2$ (sphere) and for $\omega = \frac{v_{com}}{R}$ (rolling)

to get M .

6) A 3.0 kg wheel, rolling smoothly on a horizontal surface, has a rotational inertia about its axis = $\frac{1}{2}MR^2$, where M is its mass and R is its radius. A horizontal force is applied to the axle so that the center of mass has an acceleration of 2.0 m/s^2 . The magnitude of the frictional force of the surface is :

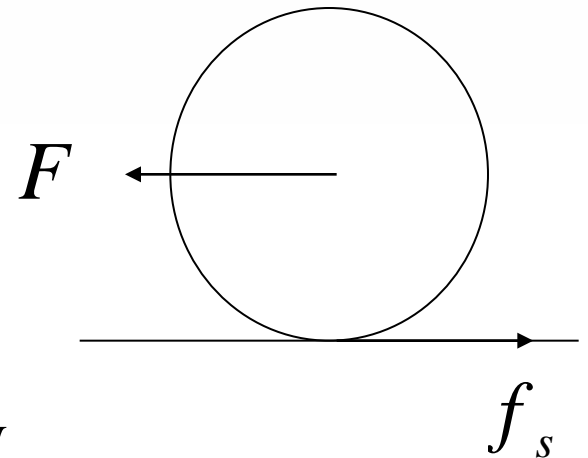
- A1 3.0 N
- A2 6.0 N
- A3 9.0 N
- A4 12 N
- A5 0 N

$$\alpha = \frac{a_{com}}{R}$$

$$\tau = I \alpha$$

$$f_s R = \left(\frac{1}{2} MR^2 \right) \times \left(\frac{a_{com}}{R} \right)$$

$$f_s = \frac{1}{2} M a_{com} = \frac{1}{2} \times 3.0 \times 2.0 = 3.0 \text{ N}$$



7) A 2.0 kg particle is moving such that its position vector (r) relative to the origin is $r = (-2.0t^2 \mathbf{i} + 3.0 \mathbf{j})$ m. What is the torque (about the origin) acting on the particle at $t=2.0$ s?

A1 24 k N.m

A2 -36 k N.m

A3 -24 k N.m

A4 -48 k N.m

A5 0

$$v = \frac{dr}{dt} = -4t \mathbf{i}$$

$$a = \frac{dv}{dt} = -4.0 \mathbf{i}$$

$$F = ma = 2.0(-4.0)\mathbf{i} = -8.0 \mathbf{i}$$

$$r(2.0) = -8.0 \mathbf{i} + 3.0 \mathbf{j}$$

$$\tau(2.0) = r \times F$$

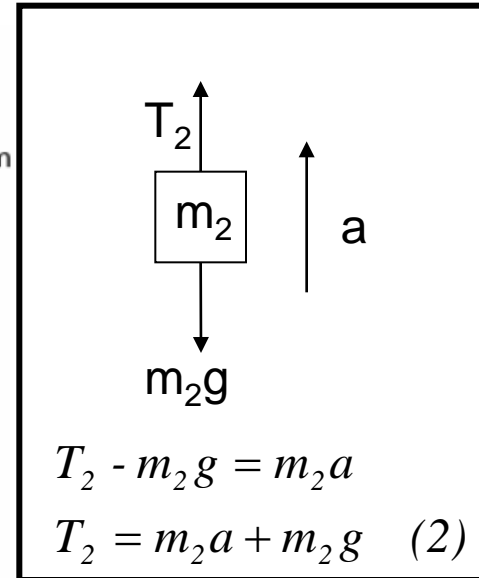
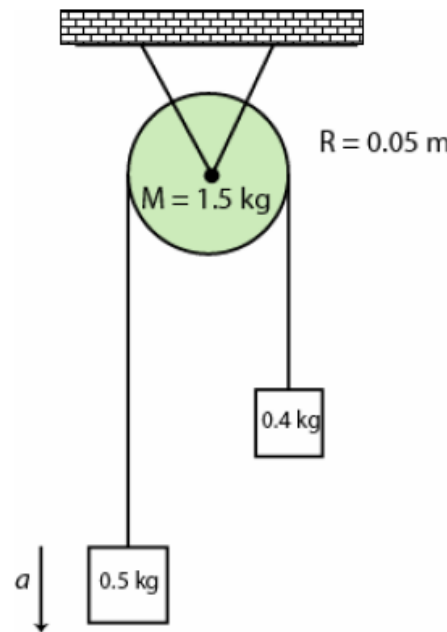
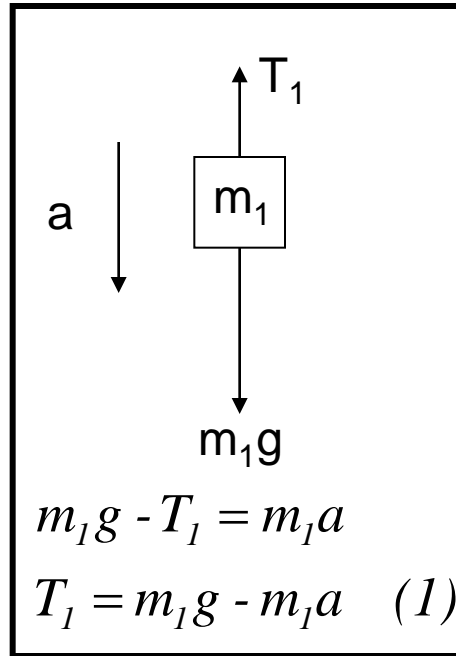
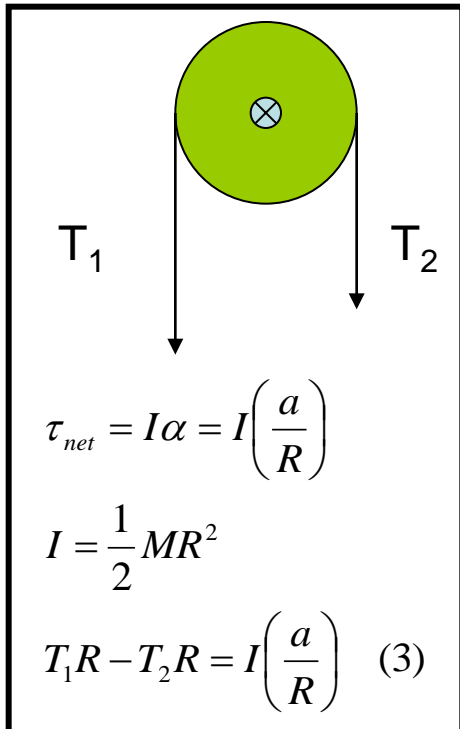
$$= (-8.0 \mathbf{i} + 3.0 \mathbf{j}) \times (-8.0 \mathbf{i})$$

$$= (3.0 \mathbf{j}) \times (-8.0 \mathbf{i})$$

$$= 24 \mathbf{k}$$

8) In the figure, $m_1 = 0.50 \text{ kg}$, $m_2 = 0.40 \text{ kg}$ and the pulley has a disk shape of radius 0.05 m and mass $M = 1.5 \text{ kg}$. What is the linear acceleration of the block of mass m_2 ?

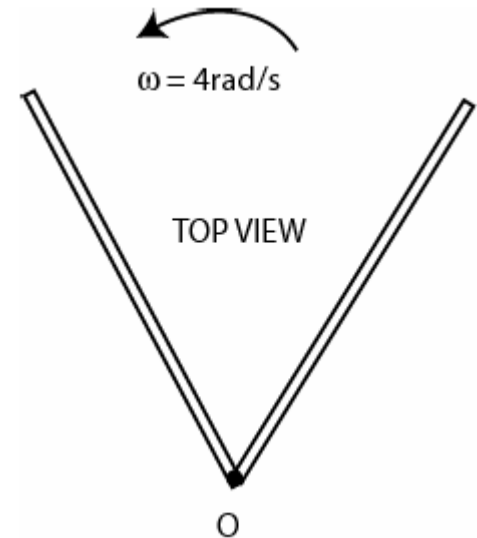
- A1 0.59 m/s^2
- A2 0.42 m/s^2
- A3 1.46 m/s^2
- A4 0.21 m/s^2
- A5 0.0



from (1) and (2) we get :
 $T_1 - T_2 = (m_1 - m_2)g - (m_1 + m_2)a$
 put this in (3) to get the value of a

9) Consider two thin rods each of length ($L = 1.5 \text{ m}$) and mass 30 g , arranged on a frictionless table as shown in the figure. The system rotates about a vertical axis through point O with constant angular speed of 4.0 rad/s . What is the angular momentum of the system about O ?

- A1 $0.18 \text{ kg}\cdot\text{m}^2/\text{s}$
- A2 $0.54 \text{ kg}\cdot\text{m}^2/\text{s}$
- A3 $1.5 \text{ kg}\cdot\text{m}^2/\text{s}$
- A4 $0.27 \text{ kg}\cdot\text{m}^2/\text{s}$
- A5 0.0



$$I = 2I_{rod} \text{ around } O$$

$$= 2\left(\frac{1}{12}ML^2 + M\left(\frac{L}{2}\right)^2\right) = 2\left(\frac{1}{3}ML^2\right)$$

$$L(\text{ around } O) = I\omega$$

10) Fig shows two disks mounted on bearings on a common axis . The first disk has rotational inertia I and is spinning with angular velocity w . The second disk has rotational inertia $2I$ and is spinning in the same direction as the first disk with angular velocity $2w$. The two disks are slowly forced toward each other along the axis until they stick and have a final common angular velocity of:

A1 $5*w/3$

A2 $w*\text{sqrt}(3)$

A3 w

A4 $3*w$

A5 $2*w$

$$\ell_1 = I_1 \omega_1 = I \omega$$

$$\ell_2 = I_2 \omega_2 = 4I \omega$$

$$L_i = \ell_1 + \ell_2 = 5I \omega$$

$$I_{tot} = I_1 + I_2 = 3I$$

$$L_f = I_{tot} \omega_f = 3I \omega_f$$

$$L_i = L_f$$

$$5I \omega = 3I \omega_f$$

$$\omega_f = \frac{5}{3} \omega$$

