

Molecules can store rotational energy as well as vibrational energy.

$$E_{\text{rot}} = \frac{\hbar^2}{2 I_{\text{cm}}} l(l+1) \quad l=0,1,2,\dots$$

l : rotational quantum number.

$$I_{\text{cm}} = \mu R_0^2$$

↓ ↑
reduced mass bond length

$$\begin{array}{c} E_l \\ \uparrow \Delta E \downarrow \\ E_{l-1} \end{array}$$

$$\Delta E = \frac{\hbar^2}{I_{\text{cm}}} l$$

quantum number of
the higher energy state.

Photons should be observed at the frequencies

$$\omega_0 = \frac{\Delta E}{\hbar} = \frac{\hbar}{I_{\text{cm}}} , 2\omega_0 , 3\omega_0 , \dots$$

transition: $0 \rightarrow 1$ $1 \rightarrow 2$ $2 \rightarrow 3 \dots$

$$E_{\text{vib}} = (v + \frac{1}{2})\hbar\omega \quad v=0,1,2,\dots$$

v : vibrational quantum number.

ω : frequency of vibration and related to the force constant by:

$$k = \frac{\hbar\omega^2}{m_1 m_2 / (m_1 + m_2)}$$

↑ ↓
a measure of reduced mass = $\frac{m_1 m_2}{m_1 + m_2}$
the bond strength