

$$\Rightarrow \langle U \rangle = -4 \frac{k e^2}{a_0^3} \left(\frac{a_0}{2}\right)^2 \int_0^{\infty} z e^{-z} dz$$

but $\int_0^{\infty} z^n e^{-z} dz = n!$

$$\Rightarrow \langle U \rangle = -4 \frac{k e^2}{a_0^3} \left(\frac{a_0}{2}\right)^2 = -\frac{k e^2}{a_0} = \boxed{-27.2 \text{ eV}}$$

$$\langle K \rangle + \langle U \rangle = \langle E \rangle$$

For the ground state $\langle E \rangle = -13.6 \text{ eV}$

and $\langle U \rangle = -27.2 \text{ eV}$

$$\Rightarrow \langle K \rangle = -13.6 + 27.2 = \boxed{13.6 \text{ eV}}$$