

Pb #24.

Use the uncertainty principle $\Delta x \cdot \Delta p \geq \frac{\hbar}{2}$

$$\lambda = 6000 \text{ \AA} \quad \text{and} \quad \frac{\Delta \lambda}{\lambda} = 10^{-6}$$

$$\lambda = \frac{h}{p} \Rightarrow d\lambda = -\frac{h}{p^2} dp = -\frac{h \lambda^2}{h^2} dp$$

$$\Delta \lambda = \frac{\lambda^2}{h} \Delta p \Rightarrow \Delta p = \frac{h}{\lambda^2} \Delta \lambda$$

$$\Rightarrow \Delta x \cdot \frac{h}{\lambda^2} \Delta \lambda = \frac{\hbar}{2} = \frac{h}{4\pi}$$

$$\Rightarrow \Delta x = \frac{\lambda^2}{4\pi \Delta \lambda} = \frac{\lambda}{4\pi \frac{\Delta \lambda}{\lambda}} = \frac{6000 \text{ \AA}}{4\pi \times 10^{-6}} =$$

$$\Delta x = 4.78 \times 10^8 \text{ \AA} = \boxed{0.0478 \text{ m}}$$

Pb #29.

 $\tau = 0.1 \text{ ns}$ for γ -rays of energy 2.00 MeVUse the uncertainty principle $\Delta E \cdot \tau \geq \frac{\hbar}{2}$

$$\Delta E = \frac{\hbar}{2\tau} = \frac{h}{4\pi\tau} = \frac{6.63 \times 10^{-34}}{4\pi \times 0.1 \times 10^{-9}} = 5.27 \times 10^{-25} \text{ J}$$

$$= 3.3 \times 10^{-6} \text{ eV}$$

This is the natural width of the γ -emission line at 2.0 MeV energy.

This energy is much less than the experimental resolution of the detector ($\pm 5 \text{ eV}$). The width cannot be measured.