

Physics 101 Rec
Quiz#5c
Chapter 7

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Name: Key Id: _____ Sect: _____

- (a) What is the work done by a force $\vec{F} = 2x\hat{i} - 3y\hat{j}$ (N) that moves a particle of mass $m = 2$ kg from a coordinates (2 m, 3 m) to (-4 m, -3 m).

\vec{F} is a varying force $\Rightarrow W = \int \vec{F} \cdot d\vec{r}$

$$\begin{aligned}
 W &= \int_{x_i}^{x_f} F_x dx + \int_{y_i}^{y_f} F_y dy \\
 &= \int_2^{-4} 2x dx - \int_3^{-3} 3y dy \\
 &= 2 \left[\frac{x^2}{2} \right]_2^{-4} - 3 \left[\frac{y^2}{2} \right]_3^{-3} = \left[(4)^2 - (2)^2 \right] - \frac{3}{2} \left[(-3)^2 - (3)^2 \right] \\
 &= 12 - (13.5 - 13.5) = 12 \text{ J}
 \end{aligned}$$

- (b) If this particle starts from rest, what is its final ~~kinetic energy~~ ^{speed}?

$$W = \Delta K = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$$

$$v_f = \sqrt{\frac{2W}{m}} = \sqrt{\frac{2 \times 12}{2}} = 3.5 \text{ m/s}$$