

Physics 102Rec

Quiz # 8

Chapter 28

Name:

Key

Id#:

Sect#:

1. A capacitor in an RC circuit is charged to 75% of its maximum value in $1.4 \mu\text{sec}$.

(a) If $R = 7 \text{ k}\Omega$ and $\varepsilon = 12 \text{ V}$, what is the value of the time constant for the circuit?

$$q = q_{\text{max}} \left(1 - e^{-\frac{t}{\tau}} \right)$$

$$0.75 q_{\text{max}} = q_{\text{max}} \left(1 - e^{-\frac{1.4 \times 10^{-6}}{\tau}} \right) \Rightarrow e^{-\frac{1.4 \times 10^{-6}}{\tau}} = 0.25$$

$$-\frac{1.4 \times 10^{-6}}{\tau} = \ln(0.25) \Rightarrow \tau = \frac{-1.4 \times 10^{-6}}{\ln(0.25)} = \frac{-1.4 \times 10^{-6}}{\ln(0.25)}$$

$$\tau = 1 \times 10^{-6} \text{ s}$$

(b) What is the current in the resistor after $1.4 \mu\text{sec}$?

$$I = \frac{\varepsilon}{R} e^{-\frac{t}{\tau}}$$

at $t = 1.4 \mu\text{s}$

$$I = \frac{12}{7 \times 10^3} e^{-\frac{1.4 \times 10^{-6}}{1 \times 10^{-6}}} = 4.2 \times 10^{-7} \text{ A}$$

(c) What is the voltage across the resistor after $1.4 \mu\text{sec}$?

$$V = RI = 7 \times 10^3 \times 4.2 \times 10^{-7} = 2.96 \times 10^{-3} \text{ V}$$