

Name: _____

Key

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A rod of proper length 1.0 m is at rest in a reference frame S' . It lies in the (x', y') plane and makes an angle of 30° with the x' axis. If S' moves with a constant velocity v parallel to the x -axis of another frame S , what is the value of v if, as measured in S , the rod makes an angle 45° with the x -axis.

See your notes $\tan \theta = \gamma \tan \theta_p$ $\theta = 45^\circ$
 $\theta_p = 30^\circ$

$$\gamma = \frac{\tan 45^\circ}{\tan 30^\circ} = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = 1.732$$

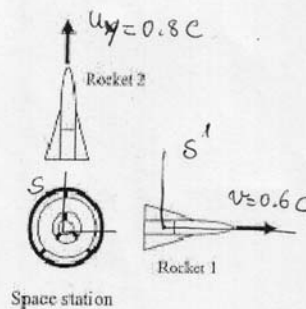
$$1 - \frac{v^2}{c^2} = \frac{1}{(1.732)^2} \Rightarrow \frac{v^2}{c^2} = 1 - \frac{1}{(1.732)^2} = 0.67$$

$$v = \sqrt{0.67} c = \boxed{0.816 c} \text{ m/s}$$

Two rockets are leaving their space station along perpendicular paths, as seen measured by an observer on a stationary space station. Rocket 1 moves at $0.60c$ and rocket 2 moves at $0.80c$, both relative to the space station. What is the velocity of rocket 2 as observed by rocket 1?

Rocket 1 $u_x = 0.6c$ $u_y = 0$

Rocket 2 $u_x = 0$ $u_y = 0.8c$



velocity of rocket 2 as observed by rocket 1:

$$u'_x = \frac{u_x - v}{1 - \frac{u_x v}{c^2}} = \frac{0 - 0.6c}{1 - 0} = -0.6c$$

$$u'_y = \frac{u_y}{\gamma \left[1 - \frac{u_x v}{c^2} \right]} = \frac{0.8c}{(1 - 0) \sqrt{1 - \frac{v^2}{c^2}}}$$

$$= 0.8c \sqrt{1 - (0.6)^2} = 0.64c$$

$$u' = \sqrt{(-0.6c)^2 + (0.64c)^2} = \boxed{0.877c} \text{ m/s}$$