

Quiz # 2 (Ch. 3)

Name:

Key

ID #

1- A vector in the xy plane has a magnitude of 25 m, an x-component of 8.0 m and a negative y-component. What is the **angle** between this vector and the **positive x-axis**?

$$|A| = 25 \text{ m}$$

$$A_x = 8 \text{ m}$$

A_y is -ve \Rightarrow vector A is in the 4th quadrant.

$$\text{We know that } |A| = \sqrt{A_x^2 + A_y^2} = 25 \text{ m}$$

$$\Rightarrow A_y = -23.7 \text{ m}$$

$$\text{now } A = 8 \mathbf{i} - 23.7 \mathbf{j}$$

the angle that A makes with +ve x-axis can be found using:

$$\tan \theta = \frac{A_y}{A_x} = \frac{-23}{8}$$

$$\theta = \tan^{-1}\left(\frac{-23}{8}\right) = -71^\circ \text{ or } (360 - 71) = 389^\circ$$

2- Vector $\mathbf{a} = 4 \mathbf{i} + \mathbf{j}$,

and vector $\mathbf{b} = -\mathbf{i} + 3 \mathbf{j}$

Find the angle between \mathbf{a} and \mathbf{R} where $\mathbf{R} = \mathbf{a} + \mathbf{b}$.

$$\mathbf{R} = 3 \mathbf{i} + 4 \mathbf{j}$$

Use the dot product to find the angle between the two vectors \mathbf{a} and \mathbf{R} :

$$\mathbf{a} \cdot \mathbf{R} = |\mathbf{a}| |\mathbf{R}| \cos \theta$$

$$12 + 4 = \sqrt{17} \sqrt{25} \cos \theta$$

$$\theta = \cos^{-1}\left(\frac{16}{5\sqrt{17}}\right) = 39^\circ$$